

3.

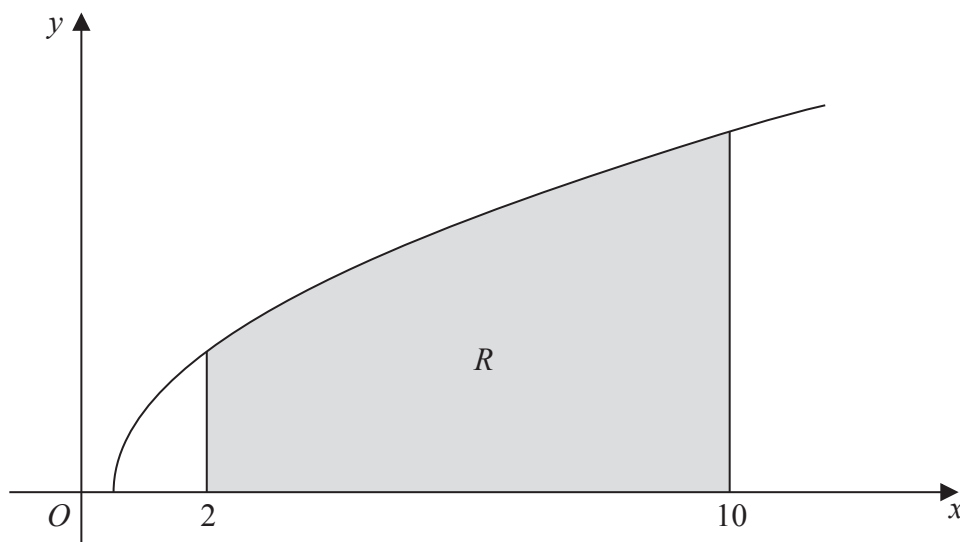


Figure 1

Figure 1 shows a sketch of part of the curve with equation $y = \sqrt{2x - 1}$, $x \geq 0.5$

The finite region R , shown shaded in Figure 1, is bounded by the curve, the x -axis and the lines with equations $x = 2$ and $x = 10$.

The table below shows corresponding values of x and y for $y = \sqrt{2x - 1}$.

x	2	4	6	8	10
y	$\sqrt{3}$		$\sqrt{11}$		$\sqrt{19}$

- (a) Complete the table with the values of y corresponding to $x = 4$ and $x = 8$. **(1)**
- (b) Use the trapezium rule, with all the values of y in the completed table, to find an approximate value for the area of R , giving your answer to 2 decimal places. **(3)**
- (c) State whether your approximate value in part (b) is an overestimate or an underestimate for the area of R . **(1)**



9.

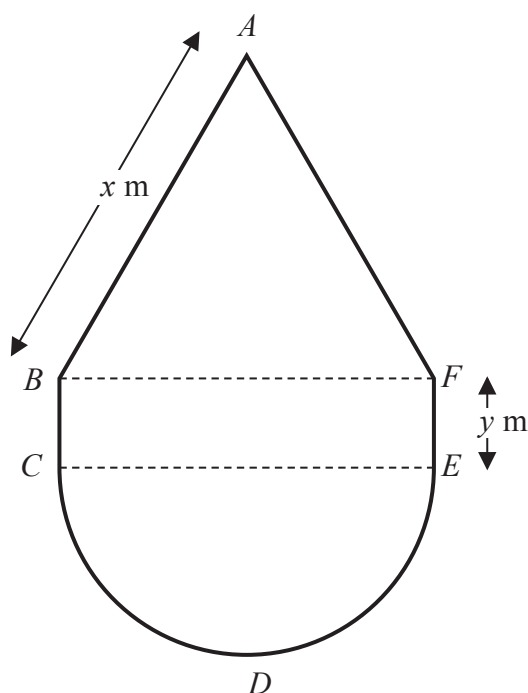


Figure 4

Figure 4 shows the plan of a pool.

The shape of the pool $ABCDEF$ consists of a rectangle $BCEF$ joined to an equilateral triangle BFA and a semi-circle CDE , as shown in Figure 4.

Given that $AB = x$ metres, $EF = y$ metres, and the area of the pool is 50 m^2 ,

(a) show that

$$y = \frac{50}{x} - \frac{x}{8}(\pi + 2\sqrt{3}) \quad (3)$$

(b) Hence show that the perimeter, P metres, of the pool is given by

$$P = \frac{100}{x} + \frac{x}{4}(\pi + 8 - 2\sqrt{3}) \quad (3)$$

(c) Use calculus to find the minimum value of P , giving your answer to 3 significant figures.

(5)

(d) Justify, by further differentiation, that the value of P that you have found is a minimum.

(2)



