

Mark Scheme (Results)

Summer 2014

Pearson Edexcel GCE in Statistics 3R
(6691/01R)

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Publications Code UA040138

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

PEARSON EDEXCEL GCE MATHEMATICS

General Instructions for Marking

1. The total number of marks for the paper is 75
2. The Edexcel Mathematics mark schemes use the following types of marks:
 - **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
 - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
 - **B** marks are unconditional accuracy marks (independent of M marks)
 - Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod – benefit of doubt
 - ft – follow through
 - the symbol \surd will be used for correct ft
 - cao – correct answer only
 - cso - correct solution only. There must be no errors in this part of the question to obtain this mark
 - isw – ignore subsequent working
 - awrt – answers which round to
 - SC: special case
 - oe – or equivalent (and appropriate)
 - d... or dep – dependent
 - indep – independent
 - dp decimal places
 - sf significant figures
 - * The answer is printed on the paper or ag- answer given
 - \square or d... The second mark is dependent on gaining the first mark
4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
7. Ignore wrong working or incorrect statements following a correct answer.

Question Number	Scheme									Marks	
<p>1.</p> <p>a)</p> <p>b)</p> <p>c)</p> <p>d)</p>	Car model	A	B	C	D	E	F	G	H	<p>M1</p> <p>M1A1</p> <p>M1</p> <p>A1</p> <p>(5)</p> <p>B1</p> <p>B1</p> <p>M1A1ft</p> <p>(4)</p> <p>B1</p> <p>(1)</p> <p>B1</p> <p>(1)</p> <p>(11 marks)</p>	
	Sales rank	8	6	1	5	4	7	2	3		
	Fuel efficiency rank	8	1	5	6	2	7	4	3		
	d^2	0	25	16	1	4	0	4	0		
	$\sum d^2 = 50$										
	$r_s = 1 - \frac{6 \sum d^2}{8(64 - 1)} = 1 - \frac{6 \times 50}{8 \times 63}$										
	$r_s = \frac{204}{504} = 0.40476 \dots$										
	awrt 0.405										
	$H_0: \rho_s = 0 \quad H_1: \rho_s > 0 \quad (\text{accept } \rho_s \text{ or } \rho)$										
1 tail critical value $\rho = 0.6429$											
Test value is not in critical region so insufficient evidence to reject H_0											
No significant evidence at 5% level to support journalist's belief											
Underlying (bivariate) Normal distribution											
Evidence does not support Normal distribution since mean < median or (negative) skew, oe											

Notes

- a)** M1 for attempting to rank at least one set of data
A1 for at least one set of data ranked correctly (NB this mark comes after 2nd M1)
M1 for attempting Σd^2
M1 for correct use of formula for r_s
- b)** B1 for H_0 **and** H_1 correct (condone \leq for H_0)
2nd B1 allow 0.7381 if their $H_1: \rho_s \neq 0$
M1 for correct statement relating their test statistic and critical value
A1ft their test statistic, H_1 and critical value but must be in context.
- c)** B1 require **Normal** distribution, ignore additional assumptions
- d)** B1 require not Normal **and** valid reason

Question Number	Scheme	Marks
<p>2)</p> <p>(a)</p> <p>(i)</p> <p>(ii)</p> <p>(b)</p>	<p>Expected value = $\frac{50 \times 74}{200} = 18.5$</p> <p>$\chi^2$ contribution = $\frac{(27-18.5)^2}{18.5} = 3.905405405 = 3.91$ to 3sfs</p> <p>H_0: users age and main mobile phone use are independent/ no association between users age and main mobile phone use H_1: users age and main mobile phone use are not independent/ some association between users age and main mobile phone use</p> <p>$\nu = 4$</p> <p>Critical value $\chi^2 = 9.488$</p> <p>Test statistic is in critical region therefore significant evidence to reject H_0 and accept H_1. Evidence at 5% level that age and main phone use are not independent.</p>	<p>B1 cso</p> <p>B1 cso</p> <p>(2)</p> <p>B1</p> <p>B1</p> <p>B1ft</p> <p>M1</p> <p>A1ft</p> <p>(5)</p> <p>(7 marks)</p>
Notes		
(b)	<p>3rd B1 ft on their value of ν</p> <p>M1 for attempt to compare test statistic and their critical value</p> <p>A1 ft on test statistic and critical value but must be comment in context. (A0 if hypotheses are the wrong way around)</p>	

Question Number	Scheme	Marks
<p>3) (a)</p> <p>(b)</p>	$P(S > 2C) = P(S - 2C > 0)$ $E[S - 2C] = 4.9 - 2 \times 2.5 = -0.1$ $\text{Var}(S - 2C) = 0.64 + 4 \times 0.16 = 1.28$ $P(S - 2C > 0), = P\left(Z > \frac{0 - (-0.1)}{\sqrt{1.28}}\right)$ $= P(Z > 0.08838\dots)$ $= 0.4641 \quad (\text{tables}), \text{ or } 0.4648\dots \text{ (calculator)}$ <p style="text-align: right;">accept awrt 0.464 or 0.465</p> <p>Let $T = S_1 + S_2 + \dots + S_{100}$</p> $E[T] = 100 \times 4.9 = 490$ $\text{Var}(T) = 100 \times 0.64 = 64$ $P(T < 500) = P\left(Z < \frac{500 - 490}{\sqrt{64}}\right)$ $= P(Z < 1.25)$ $= 0.8944$	<p>B1</p> <p>M1A1</p> <p>M1, M1</p> <p>A1</p> <p>(6)</p> <p>M1A1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>(5)</p> <p>(11 marks)</p>
Notes		
<p>(a)</p> <p>(b)</p>	<p>1st M1 for $\dots \pm 4\text{Var}(C)$ 2nd M1 for $P(S - 2C > 0)$ 3rd M1 ft their expectation and variance but not if $\text{Var}(S - 2C)$ is negative. (Should lead to $P(Z > +ve)$)</p> <p>1st M1 for attempt to find mean or variance of total</p> <p>1st A1 either correct</p> <p>2nd A1 both correct 2nd M1 for standardising using 500, their mean and their sd leading to $P(Z < +ve)$ o.e.</p> <p>Sample mean, $\bar{x} = \frac{660 + \alpha}{5} = 132 + \frac{\alpha}{5}$</p>	

Question Number	Scheme	Marks
4)	<p>Test statistic, $z = \frac{132 + \frac{\alpha}{5} - 160}{\frac{6}{\sqrt{5}}}$</p> <p>Critical z values is 1.6449</p> <p>Therefore the test statistic is significant if</p> $\frac{132 + \frac{\alpha}{5} - 160}{\frac{6}{\sqrt{5}}} > 1.6449$ <p>Therefore</p> $132 + \frac{\alpha}{5} - 160 > 1.6449 \times \frac{6}{\sqrt{5}}$ $\alpha > 5 \left(1.6449 \times \frac{6}{\sqrt{5}} + 28 \right)$ $\alpha > 162.0686493 \dots$ <p>Accept awrt 162.1</p>	<p>M1A1ft</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>(6)</p> <p>(6 marks)</p>
Notes		
	<p>1st A1 ft on their \bar{x}</p> <p>1st B1 given for 1.6449 seen (condone sign)</p> <p>3rd M1 <u>inequality</u> using their test statistic, accept incorrect signs for M1</p>	

Question Number	Scheme	Marks
5)	$S_E^2 = \frac{1}{n-1} \left(\sum x^2 - \frac{(\sum x)^2}{n} \right) = \frac{1}{119} \left(956909 - \frac{10650^2}{120} \right)$	M1
(a)	$= \frac{11721.5}{119} = 98.5$	A1 (2)
(b)	<p>$H_0: \mu_F = \mu_E,$ $H_1: \mu_F \neq \mu_E,$</p> <p>$\bar{x}_E = \frac{10650}{120} = 88.75$ and $\bar{x}_F = \frac{6510}{70} = 93$</p> <p>Test statistic, $z = \frac{93-88.75-0}{\sqrt{\frac{151}{70} + \frac{98.5}{120}}} = 2.4627 \dots$</p> <p>Critical values, $z = (\pm)2.5758$</p> <p>Test stat is not in critical region</p> <p>Insufficient evidence to reject H_0 at 1% level</p> <p>No significant evidence of a difference in mean lengths of English and French films</p>	B1 M1 M1A1 B1ft M1 A1ft (7)
(c)	By CLT we can assume that the mean of a large sample has a Normal distribution	B1 (1)
(d)	<p>On a list, label English films 1 – 724 and French films 1-473 (oe)</p> <p>Use random number table/generator to select</p> <p>$\frac{724}{724+473} \times 190 = 115$ English films and</p> <p>$\frac{473}{1197} \times 190 = 75$ French films</p>	B1 M1A1 (3) (13 marks)

Notes

	Alternative	
(a)	$S_E^2 = \frac{n}{n-1} \left(\frac{\sum x^2}{n} - \bar{x}^2 \right) = \frac{120}{119} \left(\frac{956909}{120} - 88.75^2 \right) = 98.5$	
(b)	<p>1st B1 needs both H₀ and H₁, can be in words</p> <p>2nd B1 ft on their H₁</p> <p>1st M1 for attempt @ both means (\bar{x}_E may be in (a))</p> <p>2nd M1 for attempt at correct test statistic, ft their values</p> <p>3rd M1 for attempt to compare their test stat and critical values</p> <p>A1 ft on their test and critical values but must include comment in context</p>	
(c)	Require mention of mean of <i>E</i> or <i>F</i> and normal distribution	
(d)	<p>M1 requires use of <u>random numbers</u> and attempt to find correct sample sizes</p> <p>A1 both 115 and 75 found.</p>	

Question Number	Scheme	Marks						
<p>6)</p> <p>(a)</p> <p>(b)</p> <p>(c)</p>	<p>Independence of each occurrence (of a fake coin)</p> <p>Constant probability for each occurrence (of a fake)</p> $r = 150 \times P(X = 2) = 150 \times \binom{20}{2} \times 0.05^2 \times 0.95^{18}$ <p>$r = 28.3015\dots$</p> <p style="text-align: right;">awrt 28.3</p> <p>$s = 150 - (53.8 + 56.6 + 28.3 + 8.9) = 2.4$</p> <p>$H_0$: Bin(20, 0.05) is a suitable model H_1: Bin(20, 0.05) is not a suitable model</p> <p>Combining last two groups</p> <table border="1" data-bbox="370 997 1242 1108"> <tr> <td></td> <td style="text-align: center;">≥ 3</td> </tr> <tr> <td style="text-align: center;">Observed frequency</td> <td style="text-align: center;">19</td> </tr> <tr> <td style="text-align: center;">Expected frequency</td> <td style="text-align: center;">11.3</td> </tr> </table> <p>$\nu = 4 - 1 = 3$</p> <p>Critical value, $\chi^2(0.05) = 7.815$ (accept 9.488 if their $\nu = 4$)</p> <p>Test statistic, $\sum \frac{(O-E)^2}{E} = \frac{(43-53.8)^2}{53.8} + \frac{(62-56.6)^2}{56.6} + \dots$</p> <p style="text-align: center;">$= 2.168\dots + 0.515\dots + 0.186\dots + 5.246\dots$</p> <p style="text-align: center;">$= 8.117$ (accept 10.16 if groups not combined)</p> <p>In critical region, sufficient evidence to reject H_0, accept H_1</p> <p>Significant evidence at 5% level to reject the manager's model</p>		≥ 3	Observed frequency	19	Expected frequency	11.3	<p>B1</p> <p>B1</p> <p>(2)</p> <p>M1</p> <p>A1</p> <p>A1ft</p> <p>(3)</p> <p>B1</p> <p>M1</p> <p>B1</p> <p>B1ft</p> <p>M1</p> <p>A1ft</p> <p>A1ft</p> <p>(7)</p>
	≥ 3							
Observed frequency	19							
Expected frequency	11.3							

Question Number	Scheme	Marks
(d)	$\nu = 4 - 2 = 2$ 4 classes due to pooling 2 restrictions (equal total and mean/proportion)	B1 B1 (2)
(e)	H_0 : Binomial distribution is a good model H_1 : Binomial distribution is not a good model	B1
	Critical value, $\chi^2(0.05) = 5.991$	B1
	Test statistic is not in critical region, insufficient evidence to reject H_0	B1
	Accept the assistant manager's model for the number of fake coins per bag.	(3)
Notes		
(b)	M1A1 for one of r or s correct A1ft for other value if using 150 - ... and answer must be >0	
(c)	1 st B1 can be in words but must include $p = 0.05$	
	3 rd B1 ft on their ν	
	Test statistic alternative method	
	Test stat = $\sum \frac{O^2}{E} - 150 = \frac{43^2}{53.8} + \frac{62^2}{56.6} + \dots - 150 = 8.117 \dots$	
	1 st A1 ft if their groups not combined	
	2 nd A1 ft their test and critical values but must be comment in context e.g. mention of "manager's model" <u>or</u> "fake coins"	
(d)	1 st B1 evidence that pooling is required	
	2 nd B1 must have correct reasons for restrictions.	

Question Number	Scheme	Marks
<p>7) (a) (i)</p>	$\bar{x} = \frac{10.01+9.97+9.93+\dots}{8} = 9.9775$ <p>95% CI $\bar{x} \pm 1.96 \times \frac{0.08}{\sqrt{8}}$</p> <p>95% CI for μ (9.92, 10.03)</p>	<p>M1</p> <p>B1M1</p> <p>A1</p> <p>(4)</p>
(ii)	<p>10.00 is within confidence interval so accept that pump may be performing correctly (although sample mean is low).</p>	<p>B1</p> <p>(1)</p>
(b)	<p>Upper limit of CI is</p> $9.96 + 1.6449 \times \frac{0.08}{\sqrt{n}} < 10.00$ $\frac{1.6449 \times 0.08}{\sqrt{n}} < 0.04$ $\sqrt{n} > \frac{1.6449 \times 0.08}{0.04}$ <p>$n > 10.82\dots$ therefore minimum $n = 11$</p>	<p>B1, M1A1ft</p> <p>M1</p> <p>A1 cao</p> <p>(5)</p> <p>(10 marks)</p>

Notes		
(a)		
(i)	1 st M1 attempt to find sample mean B1 for correct z value A1 limits correct to 2 decimal places (or more)	
(b)	B1 for correct z value 1 st M1A1, ft their z value	

