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Mark Scheme (Results)
Summer 2014

Pearson Edexcel International A Level in Further Pure Mathematics F2
(WFM02/01)

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.


## EDEXCEL I AL MATHEMATI CS

## General I nstructions for Marking

1. The total number of marks for the paper is 75 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod - benefit of doubt
- ft - follow through
- the symbol $\sqrt{ }$ will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
- $\quad$ The answer is printed on the paper
- $\quad$ The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.

## General Principles for Further Pure Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

## Method mark for solving 3 term quadratic:

## 1. Factorisation

$\left(x^{2}+b x+c\right)=(x+p)(x+q)$, where $|p q|=|c|$, leading to $x=\ldots$
$\left(a x^{2}+b x+c\right)=(m x+p)(n x+q)$, where $|p q|=|c|$ and $|m n|=|a|$, leading to $\mathrm{x}=\ldots$

## 2. Formula

Attempt to use the correct formula (with values for $a, b$ and $c$ ).

## 3. Completing the square

Solving $x^{2}+b x+c=0:\left(x \pm \frac{b}{2}\right)^{2} \pm q \pm c=0, \quad q \neq 0$, leading to $x=\ldots$

## Method marks for differentiation and integration:

## 1. Differentiation

Power of at least one term decreased by 1. $\left(x^{n} \rightarrow x^{n-1}\right)$

## 2. Integration

Power of at least one term increased by 1. $\left(x^{n} \rightarrow x^{n+1}\right)$

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

Method mark for quoting a correct formula and attempting to use it, even if there are small errors in the substitution of values.

Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

## Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

## Answers without working

The rubric says that these may not gain full credit. Individual mark schemes will give details of what happens in particular cases. General policy is that if it could be done "in your head", detailed working would not be required.



| Question Number | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| 3. |  |  |  |
|  | $r^{5}=\sqrt{16^{2}+(16 \sqrt{3})^{2}}=32 \Rightarrow r=32^{\frac{1}{5}}(=2)$ | Correct value for $r$ | B1 |
|  | $\arg (16-16 i \sqrt{3})=\frac{5 \pi}{3}$ | Allow $\frac{5 \pi}{3}$ or $-\frac{\pi}{3}$ | B1 |
|  | $5 \theta=\frac{11 \pi}{3}, \frac{17 \pi}{3}, \frac{23 \pi}{3}, \frac{29 \pi}{3}$ | $\left(\frac{5 \pi}{3}\right)+2 n \pi, n=1,2,3,4$ <br> At least 2 values which must be positive. May be implied by correct final answers. | M1 |
|  | $z=2 \mathrm{e}^{\frac{\pi i}{3} \mathrm{i}}, 2 \mathrm{e}^{\frac{11 \pi i}{15} \mathrm{i}}, 2 \mathrm{e}^{\frac{17 \pi}{15} \mathrm{i}}, 2 \mathrm{e}^{\frac{23 \pi i}{15} \mathrm{i}}, 2 \mathrm{e}^{\frac{29 \pi i}{15}}$ | 2 or $32^{\frac{1}{5}}$, $\mathrm{e}^{\frac{5 \pi}{15} \mathrm{i}}$ or $\mathrm{e}^{\frac{\pi}{3 i}}$ | $\begin{aligned} & \text { B1 A1(all } 4 \\ & \underline{\underline{\text { values) }}} \end{aligned}$ |
|  |  |  | (5) |
|  |  |  | Total 5 |



| Question Number | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| 5 | $\frac{\mathrm{d}^{2} y}{\mathrm{~d} x^{2}}-2 x \frac{\mathrm{~d} y}{\mathrm{~d} x}+2 y=0$ |  |  |
| (a) | $y^{\prime \prime \prime}-2 y^{\prime}-2 x y^{\prime \prime}+2 y^{\prime}(=0)\left(y^{\prime \prime \prime}=2 x y^{\prime \prime}\right)$ | M1: Attempt to differentiate including use of the product rule $\text { on } 2 x \frac{\mathrm{~d} y}{\mathrm{~d} x}$ <br> Equation may have been rewritten as $y^{\prime \prime}=\ldots$ before differentiating | M1A1 |
|  |  | A1: Correct differentiation |  |
|  | $y^{\prime \prime \prime \prime}-2 y^{\prime \prime}-2 x y^{\prime \prime \prime}-2 y^{\prime \prime}+2 y^{\prime \prime}(=0)$ | M1: Second use of product rule. Dependent on first M1. | dM1A1 |
|  |  | A1: Correct differentiation NB A simpler form is obtained if $y^{\prime \prime \prime}-2 x y^{\prime \prime}=0$ is used. |  |
|  | $\begin{aligned} & y^{\prime \prime \prime \prime}=2 x y^{\prime \prime \prime}+2 y^{\prime \prime} \\ & =2 x\left(2 x y^{\prime \prime}\right)+2 y^{\prime \prime}=\left(4 x^{2}+2\right) y^{\prime \prime} \end{aligned}$ | Cao and cso | A1 |
|  |  |  | (5) |
| (b) | $y_{0}^{\prime \prime}=-2, \quad y_{0}^{\prime \prime \prime}=0 \quad y_{0}^{\prime \prime}=-4$ | B1: $y_{0}^{\prime \prime}=-2$ | B1, M1A1 |
|  |  | M1: Attempts $y_{0}^{\prime \prime \prime}$ and $y_{0}^{\prime \prime}$ |  |
|  |  | A1: All correct and obtained from correct expressions |  |
|  | $(y=) 1+3 x-x^{2}-\frac{x^{4}}{6}$ | M1: Correct use of Maclaurin series | M1A1 |
|  |  | A1: Fully correct expansion. |  |
|  |  |  | (5) |
| (c) | $(y=) 1+3(-0.2)-(-0.2)^{2}-\frac{(-0.2)^{4}}{6}$ | Use of the correct Maclaurin series and substitution of $x=-0.2$ | M1 |
|  | $(y=0.3597$ | Allow awrt | A1 |
|  |  |  | Total 12) |
|  |  |  |  |






