





2. The time,  $t$  hours, that a typist can sit before incurring back pain is modelled by  $N(\mu, \sigma^2)$ . A random sample of 30 typists gave unbiased estimates for  $\mu$  and  $\sigma^2$  as shown below.

$$\hat{\mu} = 2.5 \quad s^2 = 0.36$$

(a) Find a 95% confidence interval for  $\sigma^2$  **(5)**

(b) State with a reason whether or not the confidence interval supports the assertion that  $\sigma^2 = 0.495$  **(2)**

Horizontal lines for writing answers to questions (a) and (b).

**(Total 7 marks)**

Q2



3. The number of houses sold per week by a firm of estate agents follows a Poisson distribution with mean 2. The firm believes that the appointment of a new salesman will increase the number of houses sold. The firm tests its belief by recording the number of houses sold,  $x$ , in the week following the appointment. The firm sets up the hypotheses  $H_0: \lambda = 2$  and  $H_1: \lambda > 2$ , where  $\lambda$  is the mean number of houses sold per week, and rejects the null hypothesis if  $x \geq 3$

(a) Find the size of the test. (2)

(b) Show that the power function for this test is

$$1 - \frac{1}{2}e^{-\lambda}(2 + 2\lambda + \lambda^2)$$

(3)

The table below gives the values of the power function to 2 decimal places.

$\lambda$	2.5	3.0	3.5	4.0	5.0	7.0
Power	0.46	$r$	0.68	$s$	0.88	0.97

**Table 1**

(c) Calculate the values of  $r$  and  $s$ . (2)

(d) Draw a graph of the power function on the graph paper provided on page 6 (2)

(e) Find the range of values of  $\lambda$  for which the power of this test is greater than 0.6 (1)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---



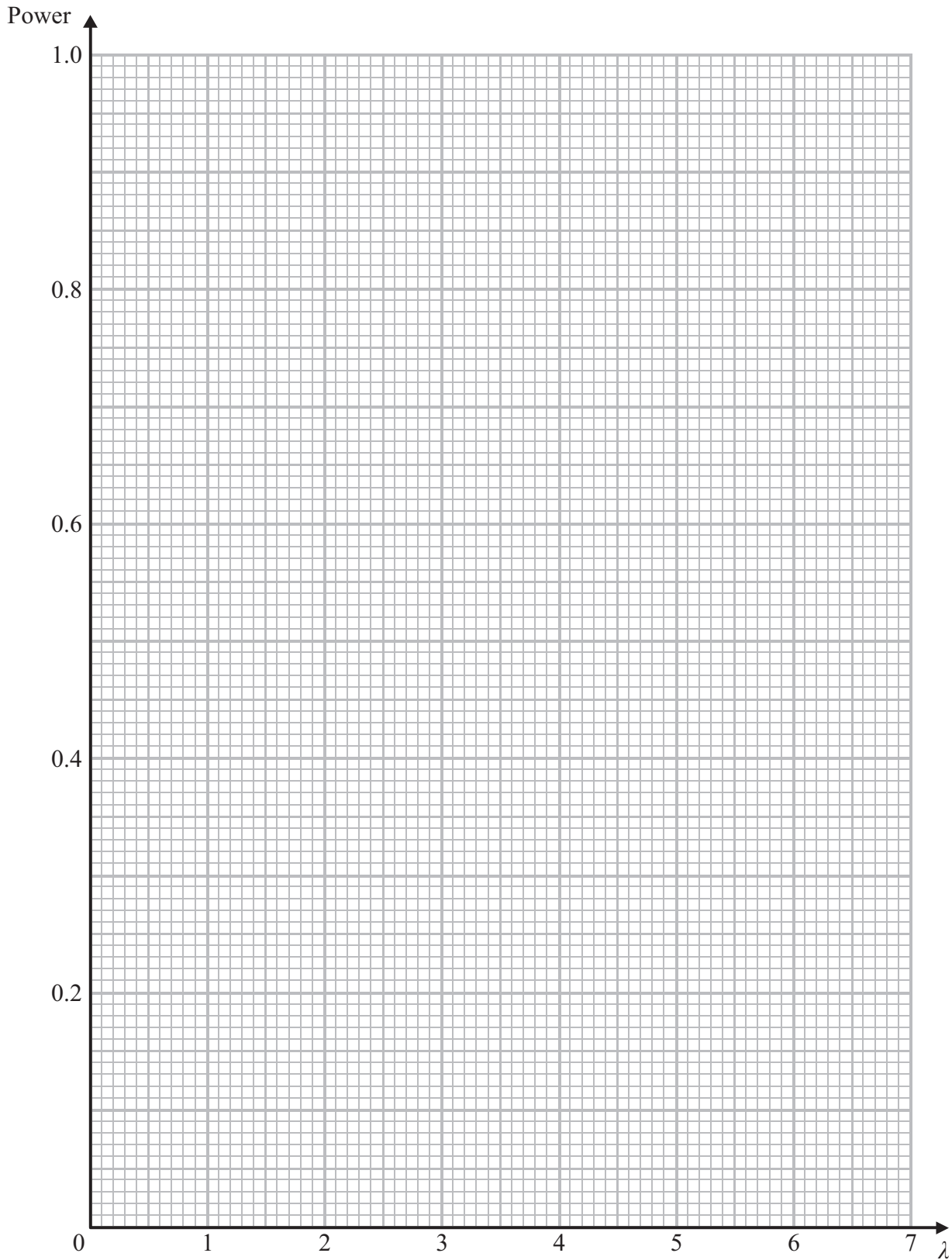


**Question 3 continued**

For your convenience Table 1 is repeated here.

$\lambda$	2.5	3.0	3.5	4.0	5.0	7.0
Power	0.46	$r$	0.68	$s$	0.88	0.97

**Table 1**



Leave  
blank

### Question 3 continued

Lined area for writing the answer to Question 3. The area contains 30 horizontal lines.

**Q3**

**(Total 10 marks)**



4. A company carries out an investigation into the strengths of rods from two different suppliers, Ardo and Bards. Independent random samples of rods were taken from each supplier and the force,  $x$  kN, needed to break each rod was recorded. The company wrote the results on a piece of paper but unfortunately spilt ink on it so some of the results can not be seen.

The paper with the results on is shown below.

Ardo:	13.1	13.6	13.2	13.8	12.8	13.5	13.8	
Bards:	15.3	15.5	14.1	15.4	14.2	15.4		
Ardo	$n_A = 7$		$\bar{x}_A = 13.4$					$s_A^2$
Bards	$n_B = 9$		$\bar{x}_B = 14.8$					$s_B^2$
Pooled estimate of variance = 0.261								

- (a) (i) Use the data from Ardo to calculate an unbiased estimate,  $s_A^2$ , of the variance.  
 (ii) Hence find an unbiased estimate,  $s_B^2$ , of the variance for the sample of 9 values from Bards. (4)

- (b) Stating your hypotheses clearly, test at the 10% level of significance whether or not there is a difference in variability of strength between the rods from Ardo and the rods from Bards.  
 (You may assume the two samples come from independent normal distributions.) (5)

- (c) Use a 5% level of significance to test whether the mean strength of rods from Bards is more than 0.9 kN greater than the mean strength of rods from Ardo. (6)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---









**Question 4 continued**

Ruled area for writing the answer to Question 4.

**Q4**

**(Total 15 marks)**



5. Students studying for their Mathematics GCSE are assessed by two examination papers. A teacher believes that on average the score on paper I is more than 1 mark higher than the score on paper II. To test this belief the scores of 8 randomly selected students are recorded. The results are given in the table below.

Student	<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>	<i>F</i>	<i>G</i>	<i>H</i>
Score on paper I	57	63	68	81	43	65	52	31
Score on paper II	53	62	61	78	44	64	43	29

Assuming that the scores are normally distributed and stating your hypotheses clearly, test at the 5% level of significance whether or not there is evidence to support the teacher's belief.

(8)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---





6. A machine fills bottles with water. The amount of water in each bottle is normally distributed. To check the machine is working properly, a random sample of 12 bottles is selected and the amount of water, in ml, in each bottle is recorded. Unbiased estimates for the mean and variance are

$$\hat{\mu} = 502 \quad s^2 = 5.6$$

Stating your hypotheses clearly, test at the 1% level of significance

- (a) whether or not the mean amount of water in a bottle is more than 500 ml, **(5)**
- (b) whether or not the standard deviation of the amount of water in a bottle is less than 3 ml. **(5)**

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---













**Question 7 continued**

Lined writing area for the question response.

**(Total 9 marks)**

**Q7**



8. A random sample  $W_1, W_2, \dots, W_n$  is taken from a distribution with mean  $\mu$  and variance  $\sigma^2$

(a) Write down  $E\left(\sum_{i=1}^n W_i\right)$  and show that  $E\left(\sum_{i=1}^n W_i^2\right) = n(\sigma^2 + \mu^2)$  (4)

An estimator for  $\mu$  is

$$\bar{X} = \frac{1}{n} \sum_{i=1}^n W_i$$

(b) Show that  $\bar{X}$  is a consistent estimator for  $\mu$ . (3)

An estimator of  $\sigma^2$  is

$$U = \frac{1}{n} \sum_{i=1}^n W_i^2 - \left(\frac{1}{n} \sum_{i=1}^n W_i\right)^2$$

(c) Find the bias of  $U$ . (4)

(d) Write down an unbiased estimator of  $\sigma^2$  in the form  $kU$ , where  $k$  is in terms of  $n$ . (1)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---





**Question 8 continued**

A series of horizontal lines for writing.



**Question 8 continued**

Lined area for writing the answer to Question 8.



