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1. Given that

$$y = 4x^3 - 1 + 2x^{\frac{1}{2}}, \quad x > 0,$$

find  $\frac{dy}{dx}$ .

**(4)**

Q1

**(Total 4 marks)**





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3. Given that  $f(x) = \frac{1}{x}, x \neq 0,$

(a) sketch the graph of  $y = f(x) + 3$  and state the equations of the asymptotes.

(4)

(b) Find the coordinates of the point where  $y = f(x) + 3$  crosses a coordinate axis.

(2)

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**Question 4 continued**

Lined area for writing the answer to Question 4.

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**Q4**

**(Total 7 marks)**

7

**Turn over**



N 2 3 5 6 1 A 0 7 2 0





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6. (a) Show that  $(4+3\sqrt{x})^2$  can be written as  $16+k\sqrt{x}+9x$ , where  $k$  is a constant to be found.

(2)

(b) Find  $\int(4+3\sqrt{x})^2 dx$ .

(3)

Blank lined area for student work.

Q6

(Total 5 marks)

9

Turn over





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**Question 7 continued**

[Lined area for writing the answer to Question 7 continued]

**(Total 9 marks)**

**Q7**

[Small rectangular box for marking Q7]



**Turn over**

8. The curve  $C$  has equation  $y = 4x + 3x^{\frac{3}{2}} - 2x^2$ ,  $x > 0$ .

(a) Find an expression for  $\frac{dy}{dx}$ . (3)

(b) Show that the point  $P(4, 8)$  lies on  $C$ . (1)

(c) Show that an equation of the normal to  $C$  at the point  $P$  is  
$$3y = x + 20.$$
 (4)

The normal to  $C$  at  $P$  cuts the  $x$ -axis at the point  $Q$ .

(d) Find the length  $PQ$ , giving your answer in a simplified surd form. (3)

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9. Ann has some sticks that are all of the same length. She arranges them in squares and has made the following 3 rows of patterns:

Row 1     □

Row 2     □□

Row 3     □□□

She notices that 4 sticks are required to make the single square in the first row, 7 sticks to make 2 squares in the second row and in the third row she needs 10 sticks to make 3 squares.

- (a) Find an expression, in terms of  $n$ , for the number of sticks required to make a similar arrangement of  $n$  squares in the  $n$ th row. (3)

Ann continues to make squares following the same pattern. She makes 4 squares in the 4th row and so on until she has completed 10 rows.

- (b) Find the total number of sticks Ann uses in making these 10 rows. (3)

Ann started with 1750 sticks. Given that Ann continues the pattern to complete  $k$  rows but does not have sufficient sticks to complete the  $(k + 1)$ th row,

- (c) show that  $k$  satisfies  $(3k - 100)(k + 35) < 0$ . (4)

- (d) Find the value of  $k$ . (2)

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**Question 9 continued**

Handwriting practice area consisting of multiple horizontal lines.

**Q9**

**(Total 12 marks)**



10. (a) On the same axes sketch the graphs of the curves with equations

(i)  $y = x^2(x - 2)$ ,

(3)

(ii)  $y = x(6 - x)$ ,

(3)

and indicate on your sketches the coordinates of all the points where the curves cross the  $x$ -axis.

(b) Use algebra to find the coordinates of the points where the graphs intersect.

(7)

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