## June 2005 <br> 6664 Core Mathematics C2 Mark Scheme



| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 2. | (a) $x \log 5=\log 8, \quad x=\frac{\log 8}{\log 5}, \quad=1.29$ <br> (b) $\log _{2} \frac{x+1}{x} \quad\left(\right.$ or $\left.\log _{2} 7 x\right)$ <br> $\frac{x+1}{x}=7 \quad x=\ldots, \quad \frac{1}{6} \quad$ (Allow 0.167 or better) | M1, A1, A1 (3) <br> B1 <br> M1, A1 <br> (3) |
|  | (a) Answer only 1.29 : Full marks. <br> Answer only, which rounds to 1.29 (e.g. 1.292): M1 A1 A0 <br> Answer only, which rounds to 1.3 : M1 A0 A0 <br> Trial and improvement: Award marks as for "answer only". <br> (b) M1: Form (by legitimate log work) and solve an equation in $x$. <br> Answer only: No marks unless verified (then full marks are available). |  |


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| 3. | (a) Attempt to evaluate $\mathrm{f}(-4)$ or $\mathrm{f}(4)$ $f(-4)=2(-4)^{3}+(-4)^{2}-25(-4)+12 \quad(=128+16+100+12)=0$ <br> so $\ldots .$. is a factor. <br> (b) $(x+4)\left(2 x^{2}-7 x+3\right)$ $\ldots \ldots \ldots .(2 x-1)(x-3)$ | M1 <br> A1 <br> (2) <br> M1 A1 <br> M1 A1 <br> (4) |
|  | (b) First M requires $\left(2 x^{2}+a x+b\right), a \neq 0, b \neq 0$. <br> Second $M$ for the attempt to factorise the quadratic. <br> Alternative: <br> $(x+4)\left(2 x^{2}+a x+b\right)=2 x^{3}+(8+a) x^{2}+(4 a+b) x+4 b=0$, then compare coefficients to find values of $a$ and $b$. [M1] $\begin{equation*} \overline{a=-7}, b=3 \tag{A1} \end{equation*}$ <br> Alternative: <br> Factor theorem: Finding that $\mathrm{f}\left(\frac{1}{2}\right)=0, \therefore(2 x-1)$ is a factor $\quad[\mathrm{M} 1, \mathrm{~A} 1]$ n.b. Finding that $\mathrm{f}\left(\frac{1}{2}\right)=0, \therefore\left(x-\frac{1}{2}\right)$ is a factor scores M1, A 0 , unless the factor 2 subsequently appears. <br> Finding that $\mathrm{f}(3)=0, \therefore(x-3)$ is a factor <br> [M1, A1] |  |


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| 4. | (a) $1+12 p x,+\frac{12 \times 11}{2}(p x)^{2}$ <br> (b) $12 p(x)=-q(x) \quad 66 p^{2}\left(x^{2}\right)=11 q\left(x^{2}\right)$ <br> (Equate terms, or coefficients) $\Rightarrow \quad 66 p^{2}=-132 p$ <br> (Eqn. in $p$ or $q$ only) | B1, B1 <br> M1 <br> M1 <br> A1, A1 <br> (4) |
|  | (a) Terms can be listed rather than added. <br> First B1: Simplified form must be seen, but may be in (b). <br> (b) First M: May still have $\binom{12}{2}$ or ${ }^{12} C_{2}$ <br> Second M: Not with $\binom{12}{2}$ or ${ }^{12} C_{2}$. Dependent upon having $p$ 's in each term. Zero solutions must be rejected for the final A mark. |  |


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| 5. |  | B1  <br> M1  <br> M1 A1 (4) <br> B1  <br> M1  <br> M1 A1 (4) <br>  $\mathbf{8}$ |
|  | (a) First M: Must be subtracting from 180 before subtracting 10. <br> (b) First M: Must be subtracting from 360 before dividing by 2, or dividing by 2 then subtracting from 180. <br> In each part: <br> Extra solutions outside 0 to 180 : Ignore. <br> Extra solutions between 0 and 180 : A0. $\begin{array}{lrl} \text { Alternative for (b): (double angle formula) } & \\ \hline 1-2 \sin ^{2} x=-0.9 & 2 \sin ^{2} x=1.9 & \text { B1 } \\ \sin x=\sqrt{0.95} & \text { M1 } \\ x=77.1 & \\ & x=180-77.1=102.9 & \text { M1 A1 } \end{array}$ |  |


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| 6. | (a) Missing $y$ values: $1.6(00) \quad 3.3(00)$ <br> (b) $(A=) \frac{1}{2} \times 4,\{(0+0)+2(1.6+2.771+3.394+3.2)\}$ $=43.86(\text { or a more accurate value }) \quad(\text { or } 43.9, \text { or } 44)$ $\begin{aligned} \text { (c) Volume } & =A \times 2 \times 60 \\ & \left.=5260\left(\mathrm{~m}^{3}\right) \quad \text { (or } 5270, \text { or } 5280\right) \end{aligned}$ | B1   <br> B1   <br>    <br> B1, M1 A1ft     <br>   A1 (4) <br> M1    <br> A1  $(2)$  <br>   $\mathbf{8}$  |
|  | (b) Answer only: No marks. <br> (c) Answer only: Allow. (The M mark in this part can be "implied"). |  |


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| 7. | (a) $\frac{\sin x}{8}=\frac{\sin 0.5}{7}$ or $\frac{8}{\sin x}=\frac{7}{\sin 0.5}, \quad \sin x=\frac{8 \sin 0.5}{7}$ $\sin x=0.548$ <br> (b) $\begin{aligned} & x=0.58 \quad(\alpha) \\ & \pi-\alpha=2.56 \end{aligned}$ <br> (This mark may be earned in (a)). |  |
|  | (a) M: Sine rule attempt (sides/angles possibly the "wrong way round"). A1ft: follow through from sides/angles are the "wrong way round". <br> Too many d.p. given: <br> Maximum 1 mark penalty in the complete question. (Deduct on first occurrence). |  |


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| 8. | (a) Centre $(5,0) \quad($ or $x=5, y=0)$ <br> (b) $(x \pm a)^{2} \pm b \pm 9+(y \pm c)^{2}=0 \Rightarrow r^{2}=\ldots$ or $r=\ldots, \quad$ Radius $=4$ <br> (c) $(1,0),(9,0) \quad$ Allow just $x=1, x=9$ <br> (d) Gradient of $A T=-\frac{2}{7}$ $y=-\frac{2}{7}(x-5)$ | B 1 B 1 $(2)$ <br> $\mathrm{M} 1, \mathrm{~A} 1$ $(2)$ <br> $\mathrm{B} 1 \mathrm{ft}, \mathrm{B} 1 \mathrm{ft}$ $(2)$ <br> B 1  <br> M1 A1ft $(3)$ <br>   |
|  | (a) $(0,5)$ scores B1 B0. <br> (d) M1: Equation of straight line through centre, any gradient (except 0 or $\infty$ ) (The equation can be in any form). <br> A1ft: Follow through from centre, but gradient must be $-\frac{2}{7}$. |  |


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| 9. |  | B1 <br> M1 <br> M1 A1cso (4) <br> M1 A1 <br> (2) <br> B1 <br> M1 A1ft |
|  | (a) B1: At least the 3 terms shown above, and no extra terms. <br> A1: Requires a completely correct solution. <br> Alternative for the 2 M marks: <br> M1: Multiply numerator and denominator by $1-r$. <br> M1: Multiply out numerator convincingly, and factorise. <br> (b) M1 can also be scored by a "year by year" method. Answer only: 39400 scores full marks, 39370 scores M1 A0. <br> (c) M1 can also be scored by a "year by year" method, with terms added. In this case the B 1 will be scored if the correct number of years is considered. Answer only: Special case: 1042000 scores 2 B marks, scored as $1,0,0,1$ (Other answers score no marks). <br> Failure to round correctly in (b) and (c): <br> Penalise once only (first occurrence). |  |


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| 10. | (a) <br> $\int\left(2 x+8 x^{-2}-5\right) \mathrm{d} x=x^{2}+\frac{8 x^{-1}}{-1}-5 x$ <br> $\left[x^{2}+\frac{8 x^{-1}}{-1}-5 x\right]_{1}^{4}=(16-2-20)-(1-8-5)$ <br> $x=1: y=5$ and $x=4: y=3.5$ <br> Area of trapezium $=\frac{1}{2}(5+3.5)(4-1) \quad(=12.75)$ <br> Shaded area $=12.75-6=6.75$ <br> (M: Subtract either way round) <br> (b) $\frac{\mathrm{d} y}{\mathrm{~d} x}=2-16 x^{-3}$ <br> (Increasing where) $\frac{\mathrm{d} y}{\mathrm{~d} x}>0$; For $x>2, \frac{16}{x^{3}}<2, \therefore \frac{\mathrm{~d} y}{\mathrm{~d} x}>0$ <br> (Allow $\geq$ ) | M1 A1 A1 <br> M1 <br> B1 <br> M1 <br> M1 A1 <br> (8) <br> M1 A1 <br> dM1; A1 <br> (4) |
|  | (a) Integration: One term wrong M1 A1 A0; two terms wrong M1 A0 A0. Limits: M1 for substituting limits 4 and 1 into a changed function, and subtracting the right way round. <br> Alternative: $x=1: y=5 \text { and } x=4: y=3.5$ <br> Equation of line: $y-5=-\frac{1}{2}(x-1) \quad y=\frac{11}{2}-\frac{1}{2} x$, subsequently used in integration with limits. $\begin{aligned} & \left(\frac{11}{2}-\frac{1}{2} x\right)-\left(2 x+\frac{8}{x^{2}}-5\right) \\ & \int\left(\frac{21}{2}-\frac{5 x}{2}-8 x^{-2}\right) \mathrm{d} x=\frac{21 x}{2}-\frac{5 x^{2}}{4}-\frac{8 x^{-1}}{-1} \end{aligned}$ <br> (M: Subtract either way round) <br> (Penalise integration mistakes, not algebra for the ft marks) $\left[\frac{21 x}{2}-\frac{5 x^{2}}{4}-\frac{8 x^{-1}}{-1}\right]_{1}^{4}=(42-20+2)-\left(\frac{21}{2}-\frac{5}{4}+8\right)$ <br> (M: Right way round) <br> Shaded area $=6.75$ <br> (The follow through marks are for the subtracted version, and again deduct an accuracy mark for a wrong term: One wrong M1 A1 A0; two wrong M1 A0 A0.) <br> Alternative for the last 2 marks in (b): <br> M1: Show that $x=2$ is a minimum, using, e.g., $2^{\text {nd }}$ derivative. <br> A1: Conclusion showing understanding of "increasing", with accurate working. | $\begin{aligned} & 3^{\text {rd }} \mathrm{M} 1 \\ & 4^{\text {th }} \mathrm{M} 1 \\ & 1^{\text {st }} \mathrm{M} 1 \mathrm{~A} 1 \mathrm{ft} \text { A1ft } \end{aligned}$ $2^{\text {nd }} \mathrm{M} 1$ <br> A1 |

