## 6677

## Edexcel GCE

## Mechanics M1

## Advanced Subsidiary

# Tuesday 7 June 2005 - Afternoon <br> Time: 1 hour 30 minutes 

Materials required for examination

Items included with question papers
Mathematical Formulae (Lilac or Green)
Nil

Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and/or integration. Thus candidates may NOT use calculators such as the Texas Instruments TI 89, TI 92, Casio CFX 9970G, Hewlett Packard HP 48G.

## Instructions to Candidates

In the boxes on the answer book, write the name of the examining body (Edexcel), your centre number, candidate number, the unit title (Mechanics M1), the paper reference (6677), your surname, other name and signature.
Whenever a numerical value of $g$ is required, take $g=9.8 \mathrm{~m} \mathrm{~s}^{-2}$.
When a calculator is used, the answer should be given to an appropriate degree of accuracy.

## Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.
Full marks may be obtained for answers to ALL questions.
This paper has eight questions.
The total mark for this paper is 75 .

## Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.
You must show sufficient working to make your methods clear to the Examiner. Answers without working may gain no credit.

1. In taking off, an aircraft moves on a straight runway $A B$ of length 1.2 km . The aircraft moves from $A$ with initial speed $2 \mathrm{~m} \mathrm{~s}^{-1}$. It moves with constant acceleration and 20 s later it leaves the runway at $C$ with speed $74 \mathrm{~m} \mathrm{~s}^{-1}$. Find
(a) the acceleration of the aircraft,
(b) the distance $B C$.
2. Two small steel balls $A$ and $B$ have mass 0.6 kg and 0.2 kg respectively. They are moving towards each other in opposite directions on a smooth horizontal table when they collide directly. Immediately before the collision, the speed of $A$ is $8 \mathrm{~m} \mathrm{~s}^{-1}$ and the speed of $B$ is $2 \mathrm{~m} \mathrm{~s}^{-1}$. Immediately after the collision, the direction of motion of $A$ is unchanged and the speed of $B$ is twice the speed of $A$. Find
(a) the speed of $A$ immediately after the collision,
(b) the magnitude of the impulse exerted on $B$ in the collision.
3. Figure 1


A smooth bead $B$ is threaded on a light inextensible string. The ends of the string are attached to two fixed points $A$ and $C$ on the same horizontal level. The bead is held in equilibrium by a horizontal force of magnitude 6 N acting parallel to $A C$. The bead $B$ is vertically below $C$ and $\angle B A C=\alpha$, as shown in Figure 1. Given that $\tan \alpha=\frac{3}{4}$, find
(a) the tension in the string,
(b) the weight of the bead.


A box of mass 2 kg is pulled up a rough plane face by means of a light rope. The plane is inclined at an angle of $20^{\circ}$ to the horizontal, as shown in Figure 2. The rope is parallel to a line of greatest slope of the plane. The tension in the rope is 18 N . The coefficient of friction between the box and the plane is 0.6 . By modelling the box as a particle, find
(a) the normal reaction of the plane on the box,
(b) the acceleration of the box.
5. A train is travelling at $10 \mathrm{~m} \mathrm{~s}^{-1}$ on a straight horizontal track. The driver sees a red signal 135 m ahead and immediately applies the brakes. The train immediately decelerates with constant deceleration for 12 s , reducing its speed to $3 \mathrm{~m} \mathrm{~s}^{-1}$. The driver then releases the brakes and allows the train to travel at a constant speed of $3 \mathrm{~m} \mathrm{~s}^{-1}$ for a further 15 s . He then applies the brakes again and the train slows down with constant deceleration, coming to rest as it reaches the signal.
(a) Sketch a speed-time graph to show the motion of the train.
(b) Find the distance travelled by the train from the moment when the brakes are first applied to the moment when its speed first reaches $3 \mathrm{~m} \mathrm{~s}^{-1}$.
(c) Find the total time from the moment when the brakes are first applied to the moment when the train comes to rest.
6.

Figure 3


A uniform beam $A B$ has mass 12 kg and length 3 m . The beam rests in equilibrium in a horizontal position, resting on two smooth supports. One support is at end $A$, the other at a point $C$ on the beam, where $B C=1 \mathrm{~m}$, as shown in Figure 3. The beam is modelled as a uniform rod.
(a) Find the reaction on the beam at $C$.

A woman of mass 48 kg stands on the beam at the point $D$. The beam remains in equilibrium. The reactions on the beam at $A$ and $C$ are now equal.
(b) Find the distance $A D$.


Figure 4 shows a lorry of mass 1600 kg towing a car of mass 900 kg along a straight horizontal road. The two vehicles are joined by a light towbar which is at an angle of $15^{\circ}$ to the road. The lorry and the car experience constant resistances to motion of magnitude 600 N and 300 N respectively. The lorry's engine produces a constant horizontal force on the lorry of magnitude 1500 N . Find
(a) the acceleration of the lorry and the car,
(b) the tension in the towbar.

When the speed of the vehicles is $6 \mathrm{~m} \mathrm{~s}^{-1}$, the towbar breaks. Assuming that the resistance to the motion of the car remains of constant magnitude 300 N ,
(c) find the distance moved by the car from the moment the towbar breaks to the moment when the car comes to rest.
(d) State whether, when the towbar breaks, the normal reaction of the road on the car is increased, decreased or remains constant. Give a reason for your answer.
8. [In this question, the unit vectors $\mathbf{i}$ and $\mathbf{j}$ are horizontal vectors due east and north respectively.]

At time $t=0$, a football player kicks a ball from the point $A$ with position vector $(2 \mathbf{i}+\mathbf{j}) \mathrm{m}$ on a horizontal football field. The motion of the ball is modelled as that of a particle moving horizontally with constant velocity $(5 \mathbf{i}+8 \mathbf{j}) \mathrm{m} \mathrm{s}^{-1}$. Find
(a) the speed of the ball,
(b) the position vector of the ball after $t$ seconds.

The point $B$ on the field has position vector $(10 \mathbf{i}+7 \mathbf{j}) \mathrm{m}$.
(c) Find the time when the ball is due north of $B$.

At time $t=0$, another player starts running due north from $B$ and moves with constant speed $v \mathrm{~m} \mathrm{~s}^{-1}$. Given that he intercepts the ball,
(d) find the value of $v$.
(e) State one physical factor, other than air resistance, which would be needed in a refinement of the model of the ball's motion to make the model more realistic.

