6671 Pure Mathematics P1

Mark Scheme

Question Number	Scheme	Marks	
1.	Forming equation in x or y by attempt to eliminate one variable $(3-y)^2 + y = 15 \text{ or } x^2 + (3-x) = 15$ $y^2 - 5y - 6 = 0 \text{ or } x^2 - x - 12 = 0 \text{ (Correct 3 term version)}$ Attempt at solution i.e. solving 3 term quadratic: $(y-6)(y+1) = 0$, $y = \dots$ or $(x-4)(x+3) = 0$, $x = \dots$ or correct use of formula or correct use of completing the square	M1 A1	
	x = 4 and $x = -3$ or $y = -1$ and $y = 6$	A1	
	Finding the values of the other coordinates (M attempt one, A both)	M1 A1 ft	(6)
2.	Using $\sin^2 \theta + \cos^2 \theta = 1$ to give a quadratic in $\cos \theta$. Attempt to solve $\cos^2 \theta + \cos \theta = 0$ $(\cos \theta = 0) \Rightarrow \theta = \frac{\pi}{2}, \frac{3\pi}{2}$	M1 M1 B1, B1	
	(cos θ = -1) $\Rightarrow \theta = \pi$ (Candidate who writes down 3 answers only with no working scores a maximum of 3)	B1	(5)
3. (a) (b)	Attempt f (2); = $16-4+4-16=0 \Rightarrow (x-2)$ is a factor must be statement for A1 $c=8$	M1; A1 B1	(2)
	A complete method to find b Either compare coefficients of x or x^2 : $-2b + 8 = 2$, or $-4 + b = -1$ Or substitute value of x (may be implied): e.g. $(x = 1) \Rightarrow -13 = (-1)(10 + b)$	M1	
(0)	$\underline{b} = \underline{3}$	A1	(3)
(c)	Checking $b^2 - 8c$; -55 \Rightarrow no real roots to the quadratic $\Rightarrow x = 2$ is the only solution	M1; A1 A1	(3)

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4 (a)	Correct strategy for differentiation e.g. $y = 4x^2 + (5x-1)x^{-1}$ multiplied out with correct differentiation method, or product or quotient rules applied correctly to $\frac{5x-1}{x}$.	M1	
	$\frac{dy}{dx} = 8x, + \frac{1}{x^2}$ B1 for 8x seen anywhere.	B1, A1	(3)
(b)	Putting $\frac{dy}{dx} = 0$	M1	
	So $8x^3 + 1 = 0$ $\Rightarrow x = -\frac{1}{2}$. M1 requires multiplication by denominator and use of a root in the solution	M1 A1	(3)
(c)	Complete method: Either $\frac{d^2y}{dx^2} = 8 - \frac{2}{x^3}$, with x value substituted, or gradient either side checked	M1	
	Completely correct argument, either > 0 with no error seen,(24)or –ve to +ve gradient, then minimum stated	A1	(2)
5(a)	$p=15,\ q=-3$ Special case if B0 B0, allow M1 for method, e.g. $8=\frac{1+p}{2}$	B1, B1	(2)
(b)	Gradient of line $ADC = -\frac{5}{7}$, gradient of perpendicular line $= -\frac{1}{\text{gradient }ADC} \left(\frac{7}{5}\right)$	B1, M1	
	Equation of l : $y-2=(\frac{7}{5})(x-8)$ $\Rightarrow 7x-5y-46=0$ (Allow rearrangements of this)	M1 A1ft A1cao	(5)
(c)	Substituting $y = 7$ and finding value for x ,	M1	
	$x = \frac{81}{7}$ or $11\frac{4}{7}$	A1	(2)

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6 (a)	$P = r\theta + 2r, \qquad A = \frac{1}{2}r^2\theta$	B1, B1	(2)
(b)	Substituting value for r and equating P to A . $[2\sqrt{2}(2+\theta) = \frac{1}{2}(2\sqrt{2})^2\theta]$ Correct process to find θ $[\theta(\sqrt{2}-1)=2]$ $\theta = \frac{2}{\sqrt{2}-1}$ * often see $\theta = \frac{4\sqrt{2}}{4-2\sqrt{2}}$	M1 M1 A1 c.s.o.	(3)
(c)	Multiply numerator and denominator by $(\sqrt{2}+1)$	M1	
	$2,+2\sqrt{2}$	A1, A1	(3)
7 (a)	Applying correct formula $[325 = 120 + 5(n-1)]$	M1	
(b)	Solving to give $n = 42$ * (or verifying in correct equation) Using formula for sum of AP: $S = \frac{42}{2} \{240 + 5(42 - 1)\}$ or use $\frac{n}{2} \{a + l\}$	A1 M1 A1	(2)
	= 9345	A1	(3)
(c)	Recognising GP with $r = 0.98$	M1	
	Value (in £) = $7200 (0.98)^{24}$	M1	
	= 4434 (only this value)	A1	(3)

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8 (a)	Substitute $x = 0$, $y = \sqrt{3}$ to give $\sqrt{3} = k \frac{\sqrt{3}}{2} \implies k = 2$ (or verify result) must see $\frac{\sqrt{3}}{2}$	B1 (1)
(b)	p = 120, $q = 300$ (f.t. on $p + 180$)	B1, B1ft (2)
(c)	$arc \sin(-0.8) = -53.1$ or $arc \sin(0.8) = 53.1$	B1
	$(x + 60) = 180 - \arcsin(-0.8)$ or equivalent $180 + \arcsin 0.8$	M1
	First value of $x = 233.1 - 60$, i.e. $x = 173.1$	A1
	OR $(x + 60) = 360 + \arcsin(-0.8)$ or equivalent 360 –arcsin 0.8, i.e. $x = 246.9$	M1, A1 (5)
9 (a)	$(x-3)^2$, +9 isw. $a = 3$ and $b = 9$ may just be written down with no method shown.	B1, M1 A1 (3)
(b)	P is (3, 9)	B1 ft, B1ft
(c)	A = (0, 18)	(2) B1
	$\frac{dy}{dx} = 2x - 6, \text{ at } A m = -6$ Equation of tangent is $y - 18 = -6x$ (in any form)	M1 A1 A1ft (4)
(d)	Showing that line meets x axis directly below P , i.e. at $x = 3$.	A1cso (1)
(e)	$A = \int x^2 - 6x + 18 dx = \left[\frac{1}{3}x^3 - 3x^2 + 18x\right]$	M1 A1
	Substituting $x = 3$ to find area A under curve $A = [-36]$	M1
	Area of $R = A$ – area of triangle= $A - \frac{1}{2} \times 18 \times 3$, = 9 Alternative: $\int x^2 - 6x + 18 - (18 - 6x) dx$ M1	M1 A1 (5)
	$= \frac{1}{3}x^3$ M1 A1 ft	
	Use $x = 3$ to give answer 9 M1 A1	