

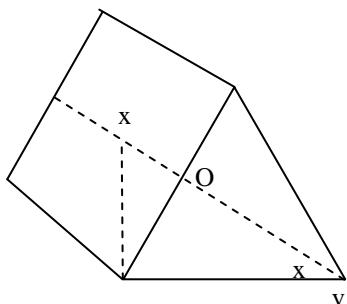
Question Number	Scheme	Marks
1.	$1000 \text{ r.p.m} = \frac{1000 \times 2\pi}{60} \text{ rad/s}$ $v = 0.035 \times \frac{1000 \times 2\pi}{60} = 3.67 \text{ ms}^{-1} \text{ (3 SF)}$	B1 M1 their $r \times$ their ω M1 A1 (3 marks)
2.	$\text{Extn at bottom} = \frac{a}{\cos \alpha} - a = \frac{2a}{3} \text{ (0.67a or better)}$ $\text{Energy: } mga \tan \alpha = \frac{2\lambda \left(\frac{2a}{3}\right)^2}{2a}$ $3mg = \lambda$	M1 A1 M1 A1 A1 ft Second M0 if treated as equilibrium Third M1 for solving for λ M1 A1 (7 marks)
3. (a)	$mg \sin 30^\circ - mx^2 = ma$ $\frac{g}{2} - x^2 = v \frac{dv}{dx} \text{ or } \frac{d\left(\frac{1}{2}v^2\right)}{dx}$ $\frac{gx}{2} - \frac{x^3}{3} (+C) = \frac{v^2}{2}$ $x = 2 : g - \frac{8}{3} = \frac{v^2}{2}$ $v = 3.8 \text{ms}^{-1} \text{ (3.78)}$	M1 A1 M1 M1 A1 M1 Third M1 for attempting to integrate A1 (7)
(b)	$v = 0: \frac{gx}{2} - \frac{x^3}{3} = 0$ $x^2 = \frac{3g}{2} \Rightarrow x = 3.8, (3.83), \sqrt{\frac{3g}{2}}$	M1 M1 A1 c.s.o must have integrated for first M1 (3) (10 marks)

(ft = follow through mark)

Question Number	Scheme	Marks	
4. (a)	$(\uparrow), R = mg$	B1	
	$m \frac{4a}{3} \omega^2$ (seen and used)	B1	
	$m \frac{4a}{3} \omega^2 \leq \frac{3}{5} mg$	M1	
	$\omega^2 \leq \frac{9g}{20a} *$	A1 c.s.o (4)	
	(b)	$T = \frac{2mg}{a} \frac{a}{3} = \frac{2mg}{3}$	B1
	$(\rightarrow), \frac{3}{5}mg + \frac{2mg}{3} \geq m \frac{4a}{3} \omega_{\max}^2$	M1 A1 f.t	
	$\frac{19g}{20a} = \omega_{\max}^2$	A1	
$(\rightarrow), -\frac{3}{5}mg + \frac{2mg}{3} \leq m \frac{4a}{3} \omega_{\min}^2$	M1 A1 f.t		
$\frac{g}{20a} = \omega_{\min}^2$	A1 (7)		
	If only one answer, must be clear whether max or min for final A1	(11 marks)	

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Question Number	Scheme			Marks		
5. (a)	Cylinder $(36\pi r^3)$	Cone $(12\pi r^3)$	Toy $(48\pi r^3)$			
	mass ratio	3	1	4	B1	
	dist. From O	$2r$	$(-r)$	\bar{x}	B1	
		$(3 \times 2r) - r = 4\bar{x}$			M1 A1	
		$\frac{5r}{4} = \bar{x}$			A1	(5)
		M1 for clear attempt at $\Sigma mx = \bar{x} \Sigma m$ – correct no. of terms.				
		If distances not measured from O , B1B1M1A1 available.				
	(b)	AG vertical, seen or implied			M1	
		$\tan \theta = \frac{3r}{4r-x}$			M1 A1	
		$\theta = 47.5^\circ$ (1 d.p.)	second M1 for use of tan		A1	(4)
	(c)	Sim Δ 's: $\frac{OX}{3r} = \frac{3r}{4r}$ ($= \tan \alpha$)			M1	
		$\Rightarrow OX = \frac{9r}{4}$			A1	
		$\bar{x} < OX$			M1	
		\Rightarrow won't topple			A1 c.s.o	(4)
		Note that second M1 is independent, for the general idea.				
						(13 marks)



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Question Number	Scheme	Marks
6.	All M marks require correct number of terms with appropriate terms resolved	
	(a) B to C : $\frac{1}{2}mv^2 - \frac{1}{2}m20^2 = mg \times 50(1 - \sin 30^\circ)$ $v = 30 \text{ ms}^{-1}$ (29.8)	M1 A1 A1 (3)
	(b) (\uparrow) at C , $R - mg = m \frac{890}{50}$ $R = 1900 \text{ N}$ (1930 N)	M1 A1 ft A1 (3)
	(c) C to D : $\frac{1}{2}m890 - \frac{1}{2}mw^2 = mg \times 50(1 - \cos 30^\circ)$ $w = 28 \text{ ms}^{-1}$ (27.5)	M1 A1 ft A1 (3)
	(d) Before: $R = mg \cos \theta$ After: $R = mg \cos \theta + m \frac{20^2}{50}$ Change = $70 \times \frac{20^2}{50} = 560 \text{ N}$	B1 M1 A1 A1 c.s.o (4)
(e) Lower speed at $C \Rightarrow R$ reduced	M1 A1 (2) (15 marks)	

(ft = follow through mark)

Question Number	Scheme	Marks
7. (a)	$(-) \frac{21.6x}{2} = 0.3\ddot{x}$ $-36x = \ddot{x}$ $\text{S.H.M., period} = \frac{2\pi}{\sqrt{36}} = \frac{\pi}{3} *$	M1 A1 M1 A1 c.s.o. (4)
(b)	At A: $v = aw = 1.5 \times 6 = 9 \text{ ms}^{-1}$	M1 A1 (2)
(c)	$x = a \cos \omega t$ $0.75 = 1.5 \cos 6t$ $\frac{\pi}{3} = 6t \Rightarrow t = \frac{\pi}{18} \text{ (no decimals)}$	M1 M1 A1 (3)
(d)	$(-) \frac{21.6x}{2} = 0.5\ddot{x}$ $-21.6x = \ddot{x} \Rightarrow \text{S.H.M., } \omega = \sqrt{21.6}$ <p>At collision: CLM: $0.3 \times 9 = 0.5v \Rightarrow v = 5.4$</p> $a \times \sqrt{21.6} = 5.4$ $a = 1.16 \text{ m (3SF)}$	M1 A1 A1 M1 A1 ft M1 A1 (7)
		(16 marks)

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