UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level and GCE Advanced Level

MARK SCHEME for the May/June 2010 question paper for the guidance of teachers

9709 MATHEMATICS

9709/23

Paper 23, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• CIE will not enter into discussions or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the May/June 2010 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.

Page 2	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2010	9709	23

Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
 B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

Page 3	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2010	9709	23

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only - often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
sos	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR -1 A penalty of MR -1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR-2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA -1 This is deducted from A or B marks in the case of premature approximation. The PA -1 penalty is usually discussed at the meeting.

	Page 4	ı	Mark Scheme: Teachers' version	Syllabus	Paper	•
			GCE AS/A LEVEL – May/June 2010	9709	23	
1			$y \log 2.8 = x \log 13$		B1	
	Rearrang	ge into	form $y = \frac{\log 13}{\log 2.8} x$ or equivalent		B1	
	Obtain aı	nswer	k = 2.49		B1	[3]
2	(i)	Use o	or imply correct ordinates 0.27067, 0.20521, 0.14936 correct formula, or equivalent, correctly with $h = 0.5$ and the in answer 0.21 with no errors seen		B1 M1 A1	[3]
	(ii)	Justif	fy statement that the trapezium rule gives an over-estimate		B1	[1]
3	EITHER OR	or p Ma Obt Star Obt from Obt	te or imply non-modular inequality $(2x-1)^2 < (x+4)^2$, or coair of linear equations ke reasonable solution attempt at a 3-term quadratic, or solvtain critical values -1 and 5 te correct answer $-1 < x < 5$ tain one critical value, e.g. $x = 5$, by solving a linear equation a graphical method or by inspection tain the other critical value similarly te correct answer $-1 < x < 5$	re two linear equati	M1 ions M1 A1 A1	[4]
4			egral $a \sin 2x$ with $a = \pm \left(1, 2 \text{ or } \frac{1}{2}\right)$ s and obtain $\frac{1}{2}$ (AG)		M1 A1	[2]
	Obta Atte	ain 3ta empt to	$x = \sec^2 x - 1$ and attempt to integrate both terms an $x - 3x$ to substitute limits, using exact values swer $2\sqrt{3} - \frac{\pi}{2}$		M1 A1 M1	[4]
5	(i)	Obta	product rule in correct derivative in any form y that derivative is equal to zero when $x = 3$		M1 A1 A1	[3]
	(ii)	State Form	titute $x = 1$ into gradient function, obtaining $2e^{-1}$ or equivale or imply required y-coordinate is e^{-1} equation of line through (l, e^{-1}) with gradient found (NOT in equation in any correct form		M1 B1 M1 A1	[4]
6	(i)		e a recognisable sketch of a relevant graph, e.g. $y = \ln x$ or y ch a second relevant graph and justify the given statement	$=2-x^2$	B1 B1	[2]
	(ii)		ider sign of In $x - (2 - x^2)$ at $x = 1.3$ and $x = 1.4$, or equivalently plete the argument correctly with appropriate calculations	ent	M1 A1	[2]

	Page 5		Mark Scheme: Teachers' version	Syllabus	Paper	•
			GCE AS/A LEVEL – May/June 2010 9709		23	
	(iii)	Show that given equation is equivalent to $x = \sqrt{(2 - \ln x)}$ or <i>vice</i>		versa	B1	[1]
	(iv)	Obta	the iterative formula correctly at least once in final answer 1.31 v sufficient iterations to justify its accuracy to 2 d.p. or show	y there is a sign ch	M1 A1	
			e interval (1.305, 1.315)	there is a sign en	B1	[3]
7	(i)	Subs Obta Solve	titute $x = 3$ and equate to 30 titute $x = -1$ and equate to 18 in a correct equation in any form e a relevant pair of equations for a or for b in $a = 1$ and $b = -13$		M1 M1 A1 M1	[5]
	(ii)	Eithe Obta Obta Obta [Con	er show that $f(2) = 0$ or divide by $(x - 2)$, obtaining a remain in quadratic factor $2x^2 + 5x - 3$ in linear factor $2x - 1$ in linear factor $x + 3$ idone omission of repetition that $x - 2$ is a factor.] near factors $2x - 1$, $x + 3$ obtained by remainder theorem or		B1 B1 B1 B1	[4]
8	(i)	Subs	correct $sin(A - B)$ and $cos(A - B)$ formulae titute exact values for $sin 30^{\circ}$ etc. in given answer correctly		M1 M1 A1	[3]
	(ii)	State	$2\sqrt{3}\sin x = \frac{1}{2}\sec x$		B1	
		Rear	range to $\sin 2x = k$, where k is a non-zero constant		M1	
		Carr	y out evaluation of $\frac{1}{2}\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$		M1	
		Carr	in answer 17.6° y out correct method for second answer		A1 M1	
		Obta range	in remaining 3 answers from 17.6°, 72.4°, 197.6°, 252.4° are	nd no others in the	A1	[6]

[Ignore answers outside the given range]