



Rewarding Learning

ADVANCED  
General Certificate of Education  
January 2014

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## Mathematics

### Assessment Unit C3

*assessing*

Module C3: Core Mathematics 3

[AMC31]

MONDAY 20 JANUARY, MORNING

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#### TIME

1 hour 30 minutes.

#### INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number on the Answer Booklet provided.

Answer **all eight** questions.

Show clearly the full development of your answers.

Answers should be given to three significant figures unless otherwise stated.

You are permitted to use a graphic or scientific calculator in this paper.

#### INFORMATION FOR CANDIDATES

The total mark for this paper is 75

Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.

A copy of the **Mathematical Formulae and Tables booklet** is provided.

Throughout the paper the logarithmic notation used is  $\ln z$  where it is noted that  $\ln z \equiv \log_e z$

**Answer all eight questions.**

**Show clearly the full development of your answers.**

**Answers should be given to three significant figures unless otherwise stated.**

**1** Solve  $|3x + 7| \geq 2$  [4]

**2 (i)** By completing the square, write  $x^2 - 4x + 12$  in the form

$$(x + a)^2 + b$$
 [2]

**(ii)** Hence describe two successive transformations which map the graph of the function  $y = x^2$  to the graph of the function  $y = x^2 - 4x + 12$  [2]

**3** Expand

$$\frac{1}{(4 - x)^2}$$

in a binomial series up to and including the term in  $x^3$  [7]

**4** Express

$$\frac{4x^2 - x + 7}{(2x - 1)(x + 2)}$$

in partial fractions. [8]

5 (a) A curve is described by the parametric equations

$$x = 2 \cot \theta \quad y = 3 - \sin \theta$$

(i) Find a Cartesian equation connecting  $x$  and  $y$ . [5]

(ii) Find the points where the curve crosses the  $y$ -axis. [2]

(b) (i) Differentiate

$$\frac{\ln x - 1}{3x^2}$$

simplifying your answer. [4]

(ii) Find

$$\int \frac{(e^{2x} - e^{-x})^2}{e^x} dx \quad [6]$$

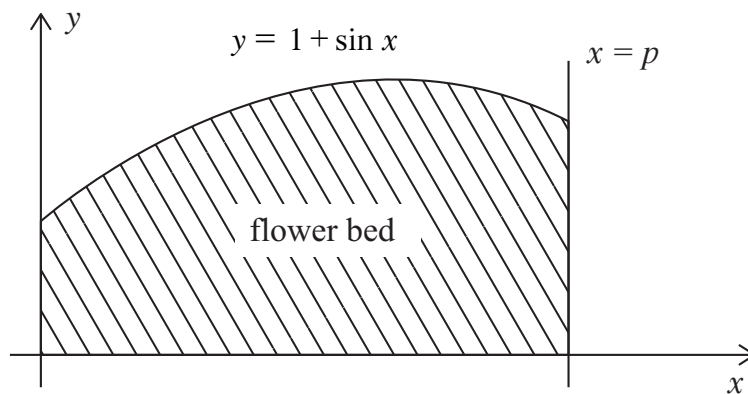
6 (a) Evaluate

$$\sec^2 x + \sin^2 x + \operatorname{cosec}^2 x + \cos^2 x - \tan^2 x - \cot^2 x \quad [2]$$

(b) Solve

$$7 \sec \theta - 8 = \frac{2}{\cot^2 \theta} \quad -\pi \leq \theta \leq \pi \quad [8]$$

- 7 A flower bed is modelled as the area bounded by the curve  $y = 1 + \sin x$ , the axes and the line  $x = p$  as shown shaded in **Fig. 1** below:



**Fig. 1**

- (i) Show that the area of this flower bed is

$$p - \cos p + 1 \quad [6]$$

- (ii) The flower bed is to have an area of 4 units<sup>2</sup>

Using the Newton–Raphson method, taking the starting value of  $p_0 = 2$ , find an improved value for  $p$  after two applications of the method. [6]

- 8 Consider the function  $y = \operatorname{cosec}^2 x$ .

- (i) Find  $\frac{d^2 y}{dx^2}$ , giving your answer in terms of  $\operatorname{cosec} x$ . [8]

- (ii) Hence find the turning points of the curve

$$y = \operatorname{cosec}^2 x \quad 0 \leq x \leq 2\pi$$

and determine their nature. [5]

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**THIS IS THE END OF THE QUESTION PAPER**

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