

ADVANCED General Certificate of Education January 2014

Mathematics

Assessment Unit M2 assessing Module M2: Mechanics 2



[AMM21]

TUESDAY 28 JANUARY, MORNING

TIME

1 hour 30 minutes.

INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number on the Answer Booklet provided. Answer **all seven** questions.

Show clearly the full development of your answers.

Answers should be given to three significant figures unless otherwise stated.

You are permitted to use a graphic or a scientific calculator in this paper.

INFORMATION FOR CANDIDATES

The total mark for this paper is 75

Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.

Answers should include diagrams where appropriate and marks may be awarded for them. Take $g = 9.8 \text{ m s}^{-2}$, unless specified otherwise.

A copy of the **Mathematical Formulae and Tables booklet** is provided.

Throughout the paper the logarithmic notation used is $\ln z$ where it is noted that $\ln z \equiv \log_e z$

Answer all seven questions.

Show clearly the full development of your answers.

Answers should be given to three significant figures unless otherwise stated.

- 1 At time t = 0 seconds, a particle of mass 2 kg is at rest at the origin. A constant force **F** of magnitude 27 N acts on the particle in the direction of the vector $\mathbf{d} = 4\mathbf{i} + 7\mathbf{j} - 4\mathbf{k}$
 - (i) Find the magnitude of d [2]
 - (ii) Find F
 - (iii) Find the speed of the particle when t = 4 [6]

[1]

2 A particle moves in a plane so that its position vector **r** metres at time *t* seconds ($t \ge 0$) is given by

$$\mathbf{r} = \begin{pmatrix} 4t^2 - 6t + 1\\ 3t^2 + 4 \end{pmatrix}$$

- (i) Find an expression for the velocity of the particle at any time *t*. [3]
- (ii) Find t when the particle is moving parallel to the vector $\begin{pmatrix} 1 \\ 2 \end{pmatrix}$ [4]
- (iii) Show that the acceleration of the particle is constant, and find its magnitude. [3]

- 3 A car of mass 1800 kg is travelling along a straight horizontal road. When the car is travelling at a speed of $v \text{ m s}^{-1}$, it experiences a resistance of 42 v newtons.
 - (i) Find the power produced by the car's engine when the car is travelling at its maximum speed of $45 \,\mathrm{m \, s^{-1}}$
 - (ii) With the engine working at the same rate, find the acceleration of the car when its speed is $35 \,\mathrm{m \, s^{-1}}$ [4]
- **4** Fig. 1 below shows the cross section of a baggage chute composed of three sections, AB, BC and CD.

AB is vertical and of length *x* metres.

BC is a quarter circle of radius 2x metres.

- CD is horizontal and of length d metres.
- AB and BC are smooth.

CD is rough.

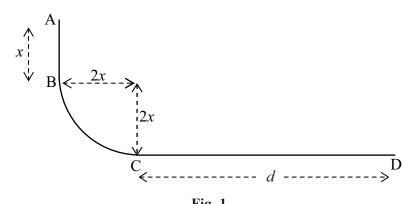


Fig. 1

A bag of mass $m \, \text{kg}$ is released from rest at the point A and slides down the chute. Assume gravitational potential energy to be zero at C.

(i) Find, in terms of g, m and x, an expression for the potential energy of the bag at A.

[2]

[4]

The coefficient of friction between the bag and CD is μ . The bag comes to rest at the point D.

(ii) Using the work–energy principle, or otherwise, find d in terms of μ and x. [5]

(iii) Find, in terms of g and x, the speed $v \text{ m s}^{-1}$ of the bag when it is halfway along CD. [5]

- 5 A racing car of mass 1200 kg moves along a straight horizontal road. The engine of the car develops a constant power of 80 kW. The constant resistances to the motion of the car total 1600 N.
 - (i) Show that the acceleration of the car can be modelled by

$$\frac{200-4v}{3v}$$

where $v \text{ m s}^{-1}$ is the velocity of the car at time *t* seconds. [4]

At t = 0 seconds, the car is travelling at a speed of 20 m s^{-1}

- (ii) Find the time taken for the car to accelerate from $20 \,\mathrm{m\,s^{-1}}$ to $30 \,\mathrm{m\,s^{-1}}$ [11]
- 6 At time t = 0 seconds, a missile is fired from a point O on horizontal ground with a velocity of $u \text{ m s}^{-1}$ at an angle of θ above the horizontal. When the missile is at a point P which is 200 m vertically above the ground, it has a velocity

of 50 m s⁻¹ at an angle of 30° above the horizontal, as shown in Fig. 2 below.

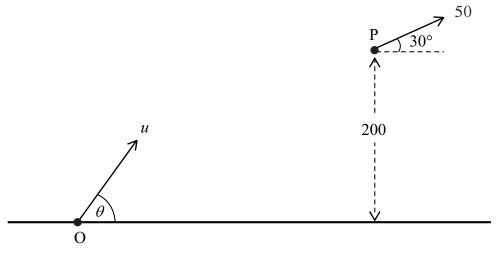


Fig. 2

- (i) Find u and θ .
- (ii) Hence, find the value of t at which the missile is 200 m vertically above the ground for the second time. [4]
- (iii) State one modelling assumption you have made when answering this question. [1]

[7]

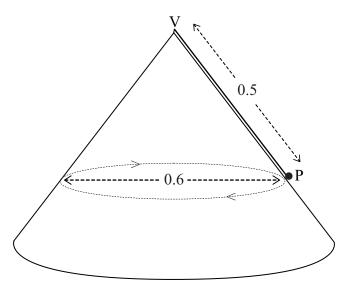
7 [Take $g = 10 \text{ m s}^{-2}$ in this question]

One end of a light inextensible string of length 0.5 m is attached to the vertex, V, of a smooth right circular cone.

A particle P of mass 2 kg is attached to the other end.

P rotates as a conical pendulum in a horizontal circle of diameter 0.6 m on the smooth outer surface of the cone, as shown in **Fig. 3** below.

The string remains parallel to the surface of the cone and P remains in contact with the cone at all times.





(i) Draw a diagram showing the external forces acting on P.

P travels with an angular velocity of 3 rad s^{-1}

(ii) Find the tension in the string.

THIS IS THE END OF THE QUESTION PAPER

[7]

[2]