## GCE 2004 June Series

ASSESSMENT and OUALIFICATIONS

## Mark Scheme

## Mathematics and Statistics B MBS3

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## Key to Mark Scheme

| M | mark is for | method |
| :---: | :---: | :---: |
| m | mark is dependent on one or more M marks and is for | method |
| A | mark is dependent on M or m marks and is for | accuracy |
| B | mark is independent of M or m marks and is for | accuracy |
| E | mark is for | explanation |
| $\checkmark$ or ft or F |  | follow through from previous incorrect result |
| cao |  | correct answer only |
| cso |  | correct solution only |
| awfw |  | anything which falls within |
| awrt |  | anything which rounds to |
| acf |  | any correct form |
| ag |  | answer given |
| sc |  | special case |
| oe |  | or equivalent |
| sf |  | significant figure(s) |
| dp |  | decimal place(s) |
| A2,1 |  | 2 or 1 (or 0 ) accuracy marks |
| $-x$ ee |  | deduct $x$ marks for each error |
| pi |  | possibly implied |
| sca |  | substantially correct approach |

## Abbreviations used in Marking

| MC $-\boldsymbol{x}$ | deducted $x$ marks for mis-copy |
| :--- | :--- |
| MR $-\boldsymbol{x}$ | deducted $x$ marks for mis-read |
| isw | ignored subsequent working |
| bod | given benefit of doubt |
| wr | work replaced by candidate |
| fb | formulae book |

## Application of Mark Scheme

No method shown:
Correct answer without working
Incorrect answer without working
More than one method / choice of solution:
2 or more complete attempts, neither/none crossed out
1 complete and 1 partial attempt, neither crossed out

Crossed out work

Alternative solution using a correct or partially correct method
mark as in scheme zero marks unless specified otherwise
mark both/all fully and award the mean mark rounded down
award credit for the complete solution only
do not mark unless it has not been replaced
award method and accuracy marks as appropriate

Mathematics and Statistics B Statistics 3 MBS3 June 2004

\begin{tabular}{|c|c|c|c|c|}
\hline Question Number and Part \& Solution \& Marks \& Total \& Comments \\
\hline 1(a) \& \begin{tabular}{l}
\(r=0.860\) (calculator) \\
(allow 0.8599, 0.85988 etc) \\
Or
\[
r=\frac{95293-\left(\frac{1441 \times 635}{10}\right)}{\sqrt{211745-\frac{1441^{2}}{10}} \times \sqrt{45063-\frac{635^{2}}{10}}}
\] \\
\(\mathrm{H}_{0} \rho=0\)
\[
\mathrm{H}_{1} \rho>01 \text { tail } 1 \% \text { sig level }
\]
\[
\mathrm{cv}=0.7155
\]
\[
\text { ts }=r=0.860
\] \\
since ts \(>0.7155\) Reject \(\mathrm{H}_{0}\) \\
Significant evidence to suggest that there is a positive association between height and pulmonary anatomical dead space as the doctor believed.
\end{tabular} \& \begin{tabular}{l}
B4 \\
B1 \\
B1 \\
M1 \\
A1
\end{tabular} \& 4

4 \& | sc awrt 0.86 $\begin{aligned} & \sum x=1441 \quad \sum x^{2}=211745 \\ & \sum y=635 \quad \sum y^{2}=45063 \\ & \sum x y=95293 \end{aligned}$ $\text { numerator }=3789.5$ $\text { denominator }=64.01 \times 68.85$ |
| :--- |
| Not $\mathrm{H}_{0}: r=0$ $\mathrm{H}_{1}: r>0$ |
| If in words must mention correlation in population |
| For cv |
| Condone 0.86 |
| For comparison $\mathrm{ts} / \mathrm{cv} \mathrm{ft}$ if cv from pmcc tables and close (eg 0.76462 tail) |
| Conclusion in context |
| sc SRCC |
| (a) B0 |
| (b) B1, B1 $(0.7333 \mathrm{cv})$ | <br>

\hline \& Total \& \& 8 \& <br>
\hline
\end{tabular}

## MBS3 (cont)

| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 2 (a) | ```\(\mathrm{H}_{0}\) : Populations of amounts of carbon monoxide emissions from cars with and without catalytic systems are distributed identically. \(\mathrm{H}_{1}\) : Populations of amounts of carbon monoxide emissions from cars with and without catalytic systems are not distributed identically - emissions from cars with a catalytic system contain less carbon monoxide on average. Or \(\mathrm{H}_{0}\) : Pop average emissions from cars with and without catalytic systems are the same. \(\mathrm{H}_{1}\) : Pop average carbon monoxide emissions less for cars with catalytic system. Or \(\mathrm{H}_{0}\) : Samples taken from identical populations \(\mathrm{H}_{1}\) : Samples not taken from identical populations (-emissions less with catalytic converter) catalytic ranks \(\quad \begin{array}{lllll}1 & 2 & 7 & 5 & 3\end{array}\) \(\left(\begin{array}{lllll}11 & 10 & 5 & 7 & 9\end{array}\right)\) without catalytic ranks 688910114 \(\left(\begin{array}{lllll}6 & 4 & 3 & 2 & 1\end{array}\right)\) \(T_{\text {catalytic }}=18\) \(T_{\text {without catalytic }}=48\) \(U=18-\left(\frac{5 \times 6}{2}\right)=3\) test stat \(=3 \quad\) (or 27)``` | B1 <br> B1 <br> M1 <br> A1 <br> A1 <br> m1 <br> A1 <br> m1 <br> A1 |  | Must have population <br> For 1-tail <br> NB Many other methods acceptable <br> For ranks as one group (can be reversed) <br> For catalytic correct <br> For without catalytic correct <br> Totals <br> Either correct <br> Method consistent for test stat <br> Or $U=48-\left(\frac{6 \times 7}{2}\right)=27$ upper tail Either test stat OK, upper or lower <br> Alternatively rank items above other group $\begin{array}{lllllll} 6 & 6 & 4 & 5 & 6 & & \text { M2 } \\ 1 & 0 & 0 & 0 & 0 & 2 & \\ \text { ts } & = & 3 & (\text { or } & 27) & & \text { M1 }) \\ \end{array}$ |

MBS3 (cont)

| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 2(b) | $\mathrm{cv}=5(\text { or } 25)$ <br> Since $3<5$, reject $\mathrm{H}_{0}$ <br> Significant evidence to suggest that populations are not identical and that exhausts with a catalytic system contain less carbon monoxide on average <br> Minimum value for $T$ is $1+2+3+4+5=15$ <br> Minimum value for $U=15-\frac{5 \times 6}{2}$ $=0$ <br> Maximum value for $T$ is $6+7+8+9+10+11=51$ <br> Maximum value for $U=51-\frac{6 \times 7}{2}$ $=30$ | B1 <br> B1 <br> m1 <br> A1 <br> M1 <br> A1 <br> M1 <br> A1 | 13 | For either tail cv (or near from table) For consistent with test stat - allow B1 ft provided sensible/correct method For comparison test stat./cv (ft if cv sensible, cv $=4$ allowed M1) <br> For $\sum_{i=1}^{5} i$ <br> Or min $0+0+0+0+0($ or $0+0+0+0+0+0)$ $\text { for } \sum_{i=6}^{11} i$ <br> Or max $6+6+6+6+6($ or $5+5+5+5+5+5)$ |
|  | Total |  | 17 |  |
| 3(a)(i) <br> (ii) <br> (iii) <br> (iv) | $\begin{aligned} & \mathrm{P}(\mathrm{~S})=\frac{57}{174}=\frac{19}{58}=0.328 \\ & \mathrm{P}(\mathrm{~T})=\frac{18}{174}=\frac{3}{29}=0.103 \\ & \mathrm{P}(\mathrm{R} \cup \mathrm{~T})=\frac{64}{174}=\frac{32}{87}=0.368 \\ & \mathrm{P}\left(\mathrm{H} \cap \mathrm{R}^{\prime}\right)=\frac{16}{174}=\frac{8}{87}=0.0920 \end{aligned}$ | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { M1 } \\ \text { A1 } \\ \text { M1 } \\ \text { A1 } \end{gathered}$ | 1 1 2 2 | for attempt at $28+13+18+1+4$ for attempt at $1+4+4+7$ |
| (v) | $P(S \mid T)=\frac{1}{18}=0.0556$ | $\begin{aligned} & \mathrm{M} 1 \\ & \mathrm{M} 1 \\ & \text { A1 } \end{aligned}$ | 3 | $\begin{aligned} & \text { for } 1 \\ & \text { for } 18 \end{aligned}$ |
| (vi) | $\mathrm{P}\left(\mathrm{R} \mid \mathrm{H}^{\prime}\right)=\frac{28}{127}=0.220$ | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 3 | ```for 28 for }12 sc 0.221 M2A0``` |
| (b) | $\mathrm{P}(\mathrm{R} \cap \mathrm{H} \cap \mathrm{~T})=\frac{13}{174}=0.0747$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ |  | for 13 |
|  | Male aged $55-74$ years (with high blood pressure) who is undergoing treatment | B1 | 3 | Not "given" |
|  | Total |  | 15 |  |

## MBS3 (cont)

| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 4(a) | $\mathrm{H}_{0}$ : Population median $=6.6$ hours $\mathrm{H}_{1}$ : Population median $\neq 6.6$ hours 2 tail test $10 \%$ sig level <br> Signs $\begin{aligned} & --++++++.+++- \\ & \text { t.s. } 9+\text { or } 3-\quad \text { (or } 9-, 3+\text { ) } \end{aligned}$ <br> $\mathrm{B}(12,0.5)$ model $\begin{aligned} & \mathrm{P}(9 \text { or more }+)=\mathrm{P}(3 \text { or less }-) \\ & =0.0730>0.05 \quad(\text { not } 0.5) \end{aligned}$ <br> Accept $\mathrm{H}_{0}$ No sig evidence to suggest patients taking new tablet have a different median number of hours sleep | B1 <br> M1 <br> A1 <br> M1 <br> m1 <br> m1 <br> A1 | 7 | $\eta$ acceptable <br> Signs <br> for 3 <br> If differences found, M1A1 still OK <br> Model with evidence of use <br> correct probability <br> compare probability and 5\% <br> Or cr $=\{0,1,2,10,11,12\}$ <br> $\mathrm{P}(0,1,2)=0.0193<0.05$ <br> or $\mathrm{P}(0,1,2,10,11,12)=0.0386<0.10$ <br> Or cr $=\{0,1,2\}$ and ts $=3$ clearly <br> identified and compared <br> sc $p=0.05 \quad$ M1 m0 m0 <br> sc $n=13$ <br> $\mathrm{P}(\leq 3)=0.0461 \quad \mathrm{M} 0 \mathrm{~m} 0 \mathrm{~m} 1$ <br> or $\mathrm{P}(\leq 4)=0.1234 \quad 3 / 7 \max$ <br> sc Wilcoxon signed-rank <br> B1 M1 A1 as above <br> M1 ranks $\max 4 / 7$ |

MBS3 (cont)

| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| (b)(i) | $\mathrm{H}_{0}$ : Population average hours sleep same for new and existing tablet $\mathrm{H}_{1}$ : Population average hours sleep greater for new tablet. <br> 1 tail test <br> $5 \%$ sig level | B1 B1 |  | For population $\mathrm{H}_{0}: \mu_{d}=0\left(\text { or } \eta_{d}=0\right)$ <br> $\mathrm{H}_{1}: \mu_{d}>0$ (or $\eta_{d}>0$ ) consistent For 1 tail |
|  | Differences $.8, .1,-.1,-.4, .7,1.0, .3, .9, .5, .2$ | M1 |  | For differences |
|  | Ranks $8,11 / 2,-11 / 2,-5,7,10,4,9,6,3$ | M1 A1 |  | For ranks (smallest = rank 1 allow even if no differences found) <br> Ranks correct |
|  | $\begin{aligned} & T_{-}=61 / 2 \\ & T_{+}=481 / 2 \end{aligned}$ | $\begin{aligned} & \text { m1 } \\ & \text { A1 } \end{aligned}$ |  | For attempting totals For either correct |
|  |  |  |  | sc rank $1=-4, T=3$ M1 A0 m1 A0 |
|  | critical value 11 <br> test statistic $=61 / 2$ | B1 |  |  |
|  | $\text { test statistic }<11$ | m1 |  | For comparison ts/cv |
|  | Significant evidence to reject $\mathrm{H}_{0}$ and conclude that the average number of hours slept is greater with the new tablet | A1 | 10 | Not necessarily in context |
| (ii) | So that any effect of taking one of the tablets before or after the other is fairly dealt with and the effect of the tablets taken can be detected. | B1 | 1 | Concept of 'fair' order enabling any difference to be detected. <br> Need idea of order. <br> Not 'bias' |
| (iii) | A paired design is preferred because it | B1 |  | generous |
|  | that a difference in tablets taken can be detected. <br> Or (It is a more powerful test) (increased precision) | B1 | 2 | Explained well <br> Not 'accurate' unless fully in context |
|  | Total |  | 20 |  |
|  | TOTAL |  | 60 |  |

