## GCE 2004 June Series

## Mark Scheme

## Mathematics and Statistics B <br> MBS1

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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## Key to Mark Scheme

| M | mark is for | method |
| :---: | :---: | :---: |
| m | mark is dependent on one or more M marks and is for | method |
| A | mark is dependent on M or m marks and is for | accuracy |
| B | mark is independent of M or m marks and is for | accuracy |
| E | mark is for | explanation |
| $\checkmark$ or ft or F |  | follow through from previous incorrect result |
| cao |  | correct answer only |
| cso |  | correct solution only |
| awfw |  | anything which falls within |
| awrt |  | anything which rounds to |
| acf |  | any correct form |
| ag |  | answer given |
| sc |  | special case |
| oe |  | or equivalent |
| sf |  | significant figure(s) |
| dp |  | decimal place(s) |
| A2,1 |  | 2 or 1 (or 0 ) accuracy marks |
| $-x$ ee |  | deduct $x$ marks for each error |
| pi |  | possibly implied |
| sca |  | substantially correct approach |

## Abbreviations used in Marking

| MC $-\boldsymbol{x}$ | deducted $x$ marks for mis-copy |
| :--- | :--- |
| MR $-\boldsymbol{x}$ | deducted $x$ marks for mis-read |
| isw | ignored subsequent working |
| bod | given benefit of doubt |
| wr | work replaced by candidate |
| fb | formulae book |

## Application of Mark Scheme

No method shown:
Correct answer without working
Incorrect answer without working
More than one method / choice of solution:
2 or more complete attempts, neither/none crossed out
1 complete and 1 partial attempt, neither crossed out

Crossed out work

Alternative solution using a correct or partially correct method
mark as in scheme zero marks unless specified otherwise
mark both/all fully and award the mean mark rounded down
award credit for the complete solution only
do not mark unless it has not been replaced
award method and accuracy marks as appropriate

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| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 1(a) | Poisson | B1 | 1 | cao |
| (b)(i) | $\mathrm{P}(2$ or fewer $)=0.570$ | B1 |  | 0.570 (0.569 to 0.57) |
| (ii) | $\mathrm{P}(4)=0.9041-0.7787$ | M1 |  | $\mathrm{P}(4)=\mathrm{P}(4$ or fewer $)-\mathrm{P}(3$ or fewer $)$ or correct use of Poisson formula |
|  | $=0.125$ | A1 | 3 | 0.125 (0.125 to 0.126) |
| (c)(i) | Poisson, mean 12 | M1 |  | Poisson, mean $5 \times 2.4$ (may be implied) |
|  |  | A1 |  | Poisson mean 12 (may be implied) |
|  | $\mathrm{P}($ fewer than 6) $=0.0203$ | B1 |  | 0.0203 (0.02 to 0.021) |
| (ii) | $\mathrm{P}(>17)=1-0.9370=0.0630$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | 5 | $\mathrm{P}(>17)=1-\mathrm{P}(17$ or fewer $)$ 0.063 ( 0.0625 to 0.0635 ) |
|  | Total |  | 9 |  |
| 2(a)(i) | 171 | B1 |  | cao ignore units |
| (ii) | 4.1 | B1 |  | cao ignore units |
| (iii) | 0.831 | B1 | 3 | cao dimensionless, disallow if units included |
| (b) | Heights of all students in the class | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ | 2 | All students in the class Heights |
|  | Total |  | 5 |  |



MBS1 (cont)

| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 4(a) | $z_{1}=\frac{3.5-5.0}{1.5}=-1$ | M1 |  | Method for z-ignore sign |
|  | $z_{2}=\frac{7.25-5.0}{1.5}=1.5$ | m1 |  | Both signs correct or correct diagram |
|  | $P(3.50<X<7.25)$ | M1 |  | Any correct use of normal tables generous |
|  | $=0.93319-(1-0.84134)=0.775$ | m1 | 5 | Completely correct method - not Dependent on previous m1 0.775 ( 0.774 to 0.775 ) |
| (b) | $z=\frac{4-5}{\frac{1.5}{\sqrt{6}}}=-1.633$ | M1 |  | $\text { Use of } \frac{1.5}{\sqrt{6}}$ |
|  |  | m1 |  | Correct method for $z$ ignore sign |
|  | $\mathrm{P}($ mean $<4)=1-0.9488=0.0512$ | $\begin{aligned} & \text { m1 } \\ & \text { A1 } \end{aligned}$ | 4 | Completely correct method 0.0512 ( 0.051 to 0.052 ) |
| (c) | To finish before 11.00 pm band will need to play 6 pieces in $29-5=24$ minutes i.e. mean 4 minutes. Low probability as shown in (b). | $\begin{gathered} \text { E1 } \\ \text { E1 } \\ \text { E1 } \checkmark \end{gathered}$ | 3 | Attempt to find necessary mean, or verify Correct mean found Correct conclusion, generous |
| (d) | After playing a long piece the band may choose to play a short piece. | E1 | 1 | Reason |
|  | Total |  | 13 |  |
| 5(a)(i) | $0.2 \times 0.2=0.04$ | M1 |  | Method |
|  |  | A1 |  | 0.04 cao acf |
| (ii) | $2 \times 0.2 \times 0.8=0.32$ | B1 |  | 2 |
|  |  | M1 |  | $0.2 \times 0.8$ used |
|  |  | A1 | 5 | 0.32 cao acf |
| (b)(i) | $0.65^{3}=0.275$ | B1 |  | 0.275 (0.274 to 0.275 ) acf |
| (ii) | $3 \times 0.2^{2} \times 0.8=0.096$ | B1 |  | 3 |
|  |  | M1 |  | $0.2^{2} \times 0.8$ |
| (iii) | $6 \times 0.15 \times 0.65 \times 0.2=0.117$ | B1 |  |  |
|  |  | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 7 | Correct method (allow 3 instead of 6 ) 0.117 cao acf |
|  | Total |  | 12 |  |

## MBS1 (cont)

| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 6(a) | (see graph on next page) | $\begin{gathered} \mathrm{M} 1 \\ \text { A1 } \end{gathered}$ | 2 | Method <br> Accurate plot by eye, allow one small slip (i.e. within $5 \times 5$ square) <br> sc Allow M1A0 if 4020 plotted on $y$-axis |
| (b) | $y=4020-2.47 x$ | B2 |  | 4020 (4000 to 4030) |
|  |  | B2 |  | -2.47 (-2.46 to -2.47) |
|  | $\begin{aligned} & x=50 \quad y=3900 \\ & x=125 \quad y=3715 \end{aligned}$ | M1 |  | Method, their line |
|  |  | A1 | 6 | Accurate line - by eye |
| (c)(i) | 3860 | M1 |  | Method - their line |
|  |  | A1 |  | 3860 (3850 to 3870) |
| (ii) | 4000 | B1 | 3 | 4000 (3999 to 4001) |
| (d) | Both predictions within observed values so estimates should be reasonable. | E1 |  | Both reasonable |
|  | Vuton residuals quite large - up to 200, Bonti residuals smaller - all $<100$, so Bonti prediction likely to be the more accurate. | E1 E1 | 3 | Bonti likely to be more accurate - must be some comment on variability Reason |
| (e) | Both graphs make similar predictions. <br> Although Bonti prediction likely to be | E1 $\checkmark$ |  | Predictions similar |
|  | more accurate there is no information as to which is likely to give greater distance. | E1 | 2 | No information which is likely to go further / Bonti preferred more predictable / other sensible comment (depends on Price / if heavier, Vuton etc) |
|  | Total |  | 16 |  |

## MBS1 (cont)

## Graph for Question 6



## MBS1 (cont)

| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 7(a)(i) | Binomial $n=5 \quad p=0.15$ | B1 |  | Binomial |
|  | $\mathrm{P}(2 \text { or fewer })=0.973$ | B1 | 3 | $\begin{array}{ll} n=5 & p=0.15 \\ 0.973 & (0.973 \text { to } 0.974) \end{array}$ |
| (ii) | $\mathrm{P}($ more than 3$)=1-0.9978$ | M1 |  | $\mathrm{P}(>3)=1-\mathrm{P}(3$ or fewer $)$ |
|  | $=0.0022$ | A1 | 2 | $0.0022(0.00215$ to 0.002250$)$ Allow 0.002 |
| (iii) | mean $=5 \times 0.15=0.75$ | B1 |  | 0.75 cao |
|  | s.d $=\sqrt{5} \times 0.15 \times 0.85=\sqrt{0.6375}$ | M1 |  | Method - allow variance if called variance even if incorrect late variance $=0.6375$ |
|  | $=0.798$ | A1 | 3 | 0.798 (0.798 to 0.8$)$ |
|  |  |  |  | sc Use of $n=7$ in Q7 |
|  |  |  |  | $\begin{array}{cc} 7(\mathrm{a})(\mathrm{i}) \text { Binomial } n=7 p=0.15 \\ 0.9262 & 3 \end{array}$ |
|  |  |  |  | (ii) 0.0121 <br> (iii) 1.05 <br> 0.945 $\begin{array}{ll} 2 & \mathrm{MR}=-1 \\ 3 \end{array}$ |
|  |  |  |  | Total 7 |
|  |  |  |  | No further allowance in (b) and (c) (if they continue with $n=7$ this would be a second misread and only (b) (ii) is affected). |
| (b)(i) | mean $=0.75$ | B1 |  | 0.75 cao |
|  | s.d $=1.24$ or 1.23 | B2 | 3 | 1.24 (1.23 to 1.24 ) allow M1A1 if method shown |
| (ii) | $\text { Proportion }=\frac{0.75}{5}=0.15$ | E1J | 1 | Their mean divided by 5 |
| (c) (i) | Not plausible s.d. much larger than for binomial | $\begin{gathered} \mathrm{B} 1 \\ \mathrm{E} 1 \sqrt{ }{ }^{2} \end{gathered}$ | 2 |  |
|  | s.d. much larger than for binomial |  | 2 | on probabilities calculated in (a)(i) and (ii) |
| (ii) | p not constant - some pupils more likely to be late than others | E1 |  | $p$ not constant / not independent |
|  | late arrivals not independent - may be due to weather/transport difficulties etc | E1 | 2 | For 2 marks, need 2 reasons with at least one in context. |
|  | Total |  | 16 |  |
|  | TOTAL |  | 80 |  |

