GCE 2004 June Series



# Mark Scheme

## Mathematics and Statistics B MBS1

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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### Key to Mark Scheme

Μ	mark is for	method
m	mark is dependent on one or more M marks and is for	method
Α	mark is dependent on M or m marks and is for	accuracy
В	mark is independent of M or m marks and is for	accuracy
Ε	mark is for	explanation
or ft or F		follow through from previous
		incorrect result
cao		correct answer only
cso		correct solution only
awfw		anything which falls within
awrt		anything which rounds to
acf		any correct form
ag		answer given
sc		special case
oe		or equivalent
sf		significant figure(s)
dp		decimal place(s)
A2,1		2 or 1 (or 0) accuracy marks
<i>x</i> ee		deduct <i>x</i> marks for each error
pi		possibly implied
sca		substantially correct approach

#### Abbreviations used in Marking

MR - xdeducted x marks for mis-readiswignored subsequent working	MC - x	deducted x marks for mis-copy
isw ignored subsequent working	MR - x	deducted x marks for mis-read
isit ignored subsequent working	isw	ignored subsequent working
bod given benefit of doubt	bod	given benefit of doubt
wr work replaced by candidate	wr	work replaced by candidate
<b>fb</b> formulae book	fb	formulae book

#### **Application of Mark Scheme**

No method shown:	
Correct answer without working	mark as in scheme
Incorrect answer without working	zero marks unless specified otherwise
More than one method / choice of solution:	
2 or more complete attempts, neither/none crossed out	mark both/all fully and award the mean mark rounded down
1 complete and 1 partial attempt, neither crossed out	award credit for the complete solution only
Crossed out work	do not mark unless it has not been replaced
Alternative solution <b>using a correct or partially correct</b> <b>method</b>	award method and accuracy marks as appropriate

Question	Solution	Marks	Total	Comments
Number				
and Part				
1(a)	Poisson	B1	1	cao
(b)(i)	P(2  or fewer) = 0.570	B1		0.570 (0.569 to 0.57)
(ii)	P(4) = 0.9041 - 0.7787	M1		P(4) = P(4  or fewer) - P(3  or fewer)  or correct use of Poisson formula
	= 0.125	A1	3	0.125 (0.125 to 0.126)
(c)(i)	Poisson mean 12	M1		Poisson, mean $5 \times 2.4$ (may be implied)
	1 0155011, 110un 12	A1		Poisson mean 12 (may be implied)
	P(fewer than  6) = 0.0203	B1		0.0203 (0.02 to 0.021)
(ii)	P(>17) = 1 - 0.9370 = 0.0630	M1 A1	5	P(>17) = 1 - P(17  or fewer) 0.063 (0.0625 to 0.0635)
	Total		9	
2(a)(i)	171	B1		cao ignore units
(ii)	4.1	B1		cao ignore units
(iii)	0.831	B1	3	cao dimensionless, disallow if units included
(b)	Heights of all students in the class	B1 B1	2	All students in the class Heights
	Total		5	

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Question Number and Part	Solution	Marks	Total	Comments
3(a)(i)	Frequency 30	Drders F: T	axed to a `akeaway	a Chinese y
	20			
	0	. 2	3 4	Number of faxed orders
	(see above)	M1		Method for line diagram – disallow Histogram, allow bar chart
		B1		Scales and labels
		A1	3	Reasonably accurate plot – by eye Disallow if line for 0 coincides with axis
(ii)	mode 0	B1	1	cao
(iii)	total frequency is 85,	M1		Method
	median is 43rd i.e. 1	A1	2	cao ignore method if answer correct
(b)	median – more representative of data	E1	1	More representative of data – allow mode if plausible reason given
(c)(i)	pie chart	B1		cao
(ii)	Bar chart / line diagram Total	B1	2 9	сао

Question	Solution	Marks	Total	Comments
Number				
and Part				
4(a)	$z_1 = \frac{3.5 - 5.0}{1.5} = -1$	M1		Method for $z$ – ignore sign
	$z_2 = \frac{7.25 - 5.0}{1.5} = 1.5$	ml		Both signs correct or correct diagram
	P(3.50 < X < 7.25)	M1		Any correct use of normal tables - generous
	= 0.93319 - (1 - 0.84134) = 0.775	m1		Completely correct method – not
		A1	5	0.775 (0.774 to 0.775)
(b)	$z = \frac{4-5}{\frac{1.5}{\sqrt{c}}} = -1.633$	M1		Use of $\frac{1.5}{\sqrt{6}}$
	νσ	m1		Correct method for z ignore sign
	P(mean < 4) = 1 - 0.9488 = 0.0512	m1 A1	4	Completely correct method 0.0512 (0.051 to 0.052)
(c)	To finish before 11.00pm band will need to play 6 pieces in $29 - 5 = 24$	E1 E1		Attempt to find necessary mean, or verify Correct mean found
	minutes i.e. mean 4 minutes. Low probability as shown in (b).	E1√	3	Correct conclusion, generous
(d)	After playing a long piece the band may choose to play a short piece.	E1	1	Reason
	Total		13	
5(a)(i)	$0.2 \times 0.2 = 0.04$	M1		Method
		A1		0.04 cao acf
(ii)	$2 \times 0.2 \times 0.8 = 0.32$	D1		2
(11)	2×0.2×0.8 - 0.32	M1		2 0.2 × 0.8 used
		A1	5	0.32 cao acf
(b)(i)	$0.65^3 = 0.275$	B1		0.275 (0.274 to 0.275) acf
(ii)	$3 \times 0.2^2 \times 0.8 = 0.096$	B1		3
		M1		$0.2^{-} \times 0.8$
	$6 \times 0.15 \times 0.65 \times 0.2 = 0.117$	Al D1		0.096 cao act
(111)	$0 \times 0.13 \times 0.03 \times 0.2 = 0.117$	M1		U Correct method (allow 3 instead of 6)
		A1	7	0.117 cao acf
	Total		12	

Question Number	Solution	Marks	Total	Comments
and Part				
6(a)	(see graph on next page)	M1	•	Method
		Al	2	Accurate plot by eye, allow one small slip
				(i.e. within 5×5 square)
				sc Allow M1A0 if 4020 plotted on <i>y</i> -axis
(b)	v = 4020 - 2.47x	B2		4020 (4000 to 4030)
		B2		-2.47(-2.46  to  -2.47)
	x = 50  y = 3900			
	x = 125  y = 3715  +  line	M1		Method, their line
		A1	6	Accurate line – by eye
	2000	M		
(C)(1)	3860			Method – their line $28(0)(2850 \pm 2870)$
	4000	AI D1	2	3800(3830103870) $4000(2000 \pm 4001)$
(11)	4000	BI	3	4000 (3999 10 4001)
(d)	Both predictions within observed			
	values so estimates should be			
	reasonable.	E1		Both reasonable
	Vuton residuals quite large $-$ up to 200			
	Bonti residuals smaller $-$ all $< 100$ so	F1		Bonti likely to be more accurate – must be
	Bonti prediction likely to be the more	21		some comment on variability
	accurate.	E1	3	Reason
	Dethermoles we have in the owned in t			Due listic and similar
(e)	Both graphs make similar predictions.	EI√		Predictions similar
	Autougn Bonti prediction likely to be	F1	2	No information which is likely to go
	as to which is likely to give greater	E1	4	further / Bonti preferred more predictable
	distance			/ other sensible comment (depends on
	aistanoo.			Price / if heavier. Vuton etc)
	Total		16	

Graph of Simulated Distance against Simulated Weight

#### **Graph for Question 6**



Question	Solution	Marks	Total	Comments
Number				
and Part $7(a)(i)$	Pinamial n = 5  n = 0.15	D1		Dinomial
/(a)(1)	Binomial $n = 5$ $p = 0.15$	BI D1		Binomial $n=5$ $n=0.15$
	P(2  or fower) = 0.072	DI D1	2	n = 5 $p = 0.150.072 (0.072 to 0.074)$
	$\Gamma(2 \text{ of rewer}) = 0.973$	DI	3	0.973 (0.973 to 0.974)
(ii)	P(more than 3) = 1 - 0.9978	M1		P(>3) = 1 - P (3  or fewer)
	= 0.0022	A1	2	0.0022(0.00215 to 0.002250) Allow 0.002
(iii)	mean = $5 \times 0.15 = 0.75$	B1		0.75 cao
	s.d = $\sqrt{5} \times 0.15 \times 0.85 = \sqrt{0.6375}$	M1		Method – allow variance if called variance even if incorrect late variance = $0.6375$
	= 0.798	A1	3	0.798 (0.798 to 0.8)
				sc Use of $n = 7$ in Q7 7(a)(i) Binomial $n = 7$ $p = 0.15$ 0.9262 3 (ii) 0.0121 2 MR=-1 (iii) 1.05 0.945 3 Total 7 No further allowance in (b) and (c) (if they continue with $n = 7$ this would be a second misread and only (b) (ii) is affected).
(b)(i)	mean = 0.75 s.d = 1.24 or 1.23	B1 B2	3	0.75 cao 1.24 (1.23 to 1.24) allow M1A1 if method shown
(ii)	Proportion = $\frac{0.75}{5} = 0.15$	E1√	1	Their mean divided by 5
(c) (i)	Not plausible s.d. much larger than for binomial	B1 E1√	2	s.d. too large – allow arguments based on probabilities calculated in (a)(i) and (ii)
(ii)	p not constant – some pupils more likely to be late than others	E1		p not constant / not independent
	late arrivals not independent – may be due to weather/transport difficulties etc	E1	2	For 2 marks, need 2 reasons with at least one in context.
	Total		16	
	TOTAL		80	