GCE 2004 June Series



Mark Scheme

Mathematics and Statistics B MBP4

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Key to Mark Scheme

| Μ | mark is for | method |
|-------------|---|--------------------------------------|
| m | mark is dependent on one or more M marks and is for | method |
| Α | mark is dependent on M or m marks and is for | accuracy |
| В | mark is independent of M or m marks and is for | accuracy |
| Ε | mark is for | explanation |
| or ft or F | | follow through from previous |
| | | incorrect result |
| cao | | correct answer only |
| cso | | correct solution only |
| awfw | | anything which falls within |
| awrt | | anything which rounds to |
| acf | | any correct form |
| ag | | answer given |
| sc | | special case |
| oe | | or equivalent |
| sf | | significant figure(s) |
| dp | | decimal place(s) |
| A2,1 | | 2 or 1 (or 0) accuracy marks |
| <i>x</i> ee | | deduct <i>x</i> marks for each error |
| pi | | possibly implied |
| sca | | substantially correct approach |

Abbreviations used in Marking

| MR - xdeducted x marks for mis-readiswignored subsequent working |
|--|
| isw ignored subsequent working |
| isit ignored subsequent working |
| bod given benefit of doubt |
| wr work replaced by candidate |
| fb formulae book |

Application of Mark Scheme

| No method shown: | |
|---|--|
| Correct answer without working | mark as in scheme |
| Incorrect answer without working | zero marks unless specified otherwise |
| More than one method / choice of solution: | |
| 2 or more complete attempts, neither/none crossed out | mark both/all fully and award the mean mark rounded down |
| 1 complete and 1 partial attempt, neither crossed out | award credit for the complete solution only |
| Crossed out work | do not mark unless it has not been replaced |
| Alternative solution using a correct or partially correct method | award method and accuracy marks as appropriate |

| Question | Solution | Marks | Total | Comments |
|----------|--|----------|-------|--|
| Number | | | | |
| and Part | - | 2.64 | | - |
| l(a) | $16x(1+x^2)^7$ | M1 A1 | 2 | *** $(1+x^2)^7$ for M1 |
| (b) | $\frac{5(x^3+2)-5x(3x^2)}{5(x^3+2)-5x(3x^2)} = \frac{10(1-x^3)}{5(x^3+2)-5x(3x^2)}$ | M1 | | Quotient rule or product rule with |
| | $\left(x^{3}+2\right)^{2} \qquad \left\lfloor \left(x^{3}+2\right)^{2}\right\rfloor$ | A1 | 2 | Correct unsimplified |
| | Total | | 4 | |
| 2 (a) | £ 100 | B1 | 1 | |
| (b) | £121.55 | B1 | 1 | $P = 100 \times 1.215506$ |
| (c) | $1.05^{t} = 1.5$ | B1 | | |
| | $\Rightarrow t \ln 1.05 = \ln 1.5$ | M1 | | Taking logs to base e or 10 |
| | $\Rightarrow t = 8.31$ | A1 | 3 | Condone more SF rounding to 8.31 |
| | Total | | 5 | |
| 3(a) | $\underline{A} + \underline{B}$ | M1 | | Compact anlit |
| | x+4 $2x+1$ | IVI I | | |
| | | ml | 2 | Comparing coeffs, sub'n etc |
| | A = -3, B = 4 | AI | 3 | One correct value may imply m1 |
| (b) | $A\ln(x+4)$ | B1√ | | ft their A and B |
| | $+\frac{1}{2}B\ln(2x+1)$ | B1√ | | ft $-3\ln(x+4) + 2\ln(2x+1)$ |
| | $(-3\ln 8 + 2\ln 9) - (-3\ln 4)$ | M1 | | Sub of limits 0 and 4, |
| | | | | (must have more than 2 ln terms for M1) |
| | $= 4 \ln 3 - 3 \ln 2$ | A1 | 4 | (p = 4, q = 3) |
| | Total | | 7 | |
| 4(a) | p(3) = 27 - 54 + 36 - 11 | M1 | | Must consider p(3) or full long division to remainder |
| | =-2 (is remainder) | A1 | 2 | |
| (b)(i) | p(4) = 64 - 96 + 48 - 11 = 5 | D1 | 1 | |
| | [Change of sign] $\Rightarrow \alpha$ lies between 3 and 4 | BI | 1 | Both $p(3)$ and $p(4)$ must be correct and there must be some statement/conclusion |
| (ii) | p(3.5) used first (=0.375) | M1 | | \Rightarrow root lies between 3 and 3.5 |
| | p(3.25) = -1.046875 | m1 | | |
| | \Rightarrow root lies between 3.25 and 3.5 | B1 | 3 | |
| (c)(i) | $x^{3} + 3 \times (-2)x^{2} + 3 \times (-2)^{2}x + (-2)^{3}$ | M1 | | Attempt at row 1 3 of Pascal's triangle or (binomial) expansion |
| | $= x^3 - 6x^2 + 12x - 8$ | A1 | 2 | All correct and simplified |
| (ii) | $p(x) = (x-2)^3 - 3$ | B1 | 1 | (<i>k</i> = 3) |
| (iii) | $x - 2 = \sqrt[3]{3}$ | M1 | | Attempt to isolate x |
| | $\Rightarrow x = 2 + \sqrt[3]{3}$ | A1√ | 2 | ft from (ii) |
| | Total | | 11 | |

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MBP4 (cont)

| Question | Solution | Marks | Total | Comments |
|----------|---|----------|-------|--|
| Number | | | | |
| 5(a)(i) | $(x - 2)^2 + (x + 5)^2 - x^2$ | M1 | | Or attempt to complete square etc. |
| J(d)(1) | (x-2) + (y+3) = r | | 2 | Correct answer implies M1 |
| (ii) | $u^2 - 7 + 2^2 + 5^2 - 26$ | | 2 | Attempt at x^2 from formula or equation |
| (11) | r = 7 + 2 + 3 = 30 $\Rightarrow r = 6$ | A 1 | 2 | Attempt at r from formula or equation \mathbf{ag} be convinced – watch circular arg't |
| (b) (i) | $ 24 \times 2 + 7 \times (-5) - (5k + 3) $ | | - | |
| | $d = \frac{ 10-5k }{\sqrt{7^2 + 24^2}}$ | IVI I | | sign slip or omission of brackets or mod signs |
| | 25 2-k | A1 | 2 | ag (algebra must follow correctly) |
| | $=\frac{1}{5}$ | | | condone no modulus signs |
| (ii) | $\frac{ 2-k }{5} \le 6 \Rightarrow 2-k \le 30$ | B1 | | ag be convinced they are using radius of circle |
| | Boundaries for k are -28 | B1 | | |
| | and 32 | B1 | 4 | |
| | $\frac{-28 \le k \le 32}{\text{Total}}$ | BI | 4 | Allow -28 < k < 32 |
| 6(a) | $9\sin^2 r \pm 30\sin r\cos r \pm 25\cos^2 r$ | D1 | 10 | |
| | $30 \sin x \cos x + 25 \cos x$ | B1 B1 | | ag be convinced |
| | Use of $\cos 2x = 2\cos^2 x - 1$ (or $1 - 2\sin^2 x$) | M1 | | |
| | $9 + 16\cos^2 x = 17 + 8\cos 2x$ | A1 | 4 | ag be convinced |
| (b)(1) | $17x + 4\sin 2x - \frac{15}{2}\cos 2x$ (+C) | M1 | | Attempt to integrate a trig term |
| | 2 | Al | | One trig term correct |
| | | A1 | 3 | All correct (condone no $+C$) |
| (ii) | $\pi \int_{0}^{\frac{\pi}{4}} y^2 dx$ | B1 | | May be simply stated and not used |
| | $=\pi\left(\frac{17}{4}\pi+\frac{23}{2}\right)$ | M1 | | Sub limits into their (i) answer (condone missing π for M1 |
| | (4 2) | A1 | 3 | Or equivalent 78.07, 24.85 π , etc |
| (c)(i) | $(3\sin x + 5\cos x)^2 = 4\cos^2 x$ | | | |
| | $\Rightarrow \left(3\frac{\sin x}{\cos x} + 5\right)^2 = 4 \Rightarrow \left(3\tan x + 5\right)^2 = 4$ | B1 | 1 | ag be convinced |
| (ii) | $3\tan x + 5 = 2$ | M1 | | |
| | $\Rightarrow \tan x = -1$ | A1 | | |
| | $\Rightarrow x = \frac{3\pi}{4}$ | A1 | | Condone 2.356 radians or 135° |
| | $3\tan x + 5 = -2 \implies \tan x = -\frac{7}{2}$ | M1 | | Use of negative root |
| | $\Rightarrow x = 1.976^{c}$ | A1 | 5 | Withhold final A1 if both answers not in radians or extra solutions given |
| | Total | | 16 | |
| L | 10001 | 1 | 10 | |

MBP4 (cont)

| Question | Solution | Marks | Total | Comments |
|----------|---|----------|-------|--|
| Number | | | | |
| and Part | | | | |
| /(a) | $\csc\theta = \frac{1}{\sin\theta}$ | M1 | | Evidenced by $\operatorname{cosec}\left(\frac{3\pi}{4}\right) = \sqrt{2}$ (or |
| | | | | 1.414) or final answer 7.07106 |
| | $f\left(\frac{\pi}{4}\right) = 5\sqrt{2}$ | A1 | 2 | Must be exactly this |
| (b) (i) | $f'(x) = -15 \operatorname{cosec} 3x \operatorname{cot} 3x$ | M1 A1 | 2 | k cosec***cot*** |
| (ii) | either $\csc\left(\frac{3\pi}{4}\right) = \sqrt{2}$ | | | |
| | or $\cot\left(\frac{3\pi}{4}\right) = -1$ | M1 | | |
| | $f'(x) = -15 \times \sqrt{2} \times (-1) = 15\sqrt{2}$ | A1 | 2 | Must be exactly this |
| (c) | $y - 5\sqrt{2} = 15\sqrt{2}\left(x - \frac{\pi}{4}\right)$ | B1√ | 1 | ft y - their f' $\left(\frac{\pi}{4}\right)$ = their f' $\left(\frac{\pi}{4}\right)\left(x - \frac{\pi}{4}\right)$ Must involve surds |
| | Tota | 1 | 7 | |
| | ΤΟΤΑΙ | 4 | 60 | |