 OUALIFICATIONS

## GCE

# Mathematics \& Statistics B 

## Unit MBP5

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## Key to mark scheme

| M | mark is for | method |
| :---: | :---: | :---: |
| m | mark is dependent on one or more M marks and is for | method |
| A | mark is dependent on M or m mark and is for | accuracy |
| B | mark is independent of M or m marks and is for | method and accuracy |
| E | mark is for | explanation |
| $\checkmark$ or ft or F |  | follow through from previous incorrect result |
| CAO |  | correct answer only |
| AWFW |  | anything which falls within |
| AWRT |  | anything which rounds to |
| AG |  | answer given |
| SC |  | special case |
| OE |  | or equivalent |
| A2,1 |  | 2 or 1 (or 0 ) accuracy marks |
| $-\boldsymbol{x}$ EE |  | Deduct $x$ marks for each error |
| NMS |  | No method shown |
| PI |  | Perhaps implied |
| c |  | Candidate |

## Abbreviations used in marking

| MC $-\boldsymbol{x}$ | deducted $x$ marks for miscopy |
| :--- | ---: |
| MR $-\boldsymbol{x}$ | deducted $x$ marks for misread |
| ISW | ignored subsequent working |
| BOD | gave benefit of doubt |
| WR | work replaced by candidate |

## Application of mark scheme

mark as in scheme
Incorrect answer without working zero marks unless specified otherwise

[^0]\begin{tabular}{|c|c|c|c|c|}
\hline Question Number and part \& Solution \& Marks \& Total \& Comments \\
\hline 1 \& \[
\begin{aligned}
\& h=0.5 \\
\& \text { Integral }=\frac{h}{2}\{\ldots\} \\
\& \{\ldots\}=\left[\frac{1}{4}+\frac{1}{30}+2\left(\frac{8}{51}+\frac{1}{11}+\frac{8}{149}\right)\right] \\
\& \text { Integral }=0.222 \\
\& \text { sc (for } 5 \text { strips) } h=0.4
\end{aligned}
\] \& \begin{tabular}{l}
B1 \\
M1 \\
A1 \\
A1
\end{tabular} \& 4 \& \begin{tabular}{l}
At least 3 terms correct 5 terms, at least 4 correct \\
cao must be 0.222 \\
B0 \\
M1 at least 4 terms correct A1 6 terms at least 5 correct A1cao
\end{tabular} \\
\hline \& Total \& \& 4 \& \\
\hline 2 \& \[
\begin{aligned}
\& 3 y^{2} \frac{\mathrm{~d} y}{\mathrm{~d} x}+3 \frac{\mathrm{~d} y}{\mathrm{~d} x}=3 x^{2} \\
\& 3\left(y^{2}+1\right) \frac{\mathrm{d} y}{\mathrm{~d} x}=3 x^{2} \\
\& \Rightarrow \frac{\mathrm{~d} y}{\mathrm{~d} x}=\frac{x^{2}}{y^{2}+1}
\end{aligned}
\] \& \begin{tabular}{l}
M1 \\
A1 \\
A1
\end{tabular} \& 3 \& \begin{tabular}{l}
2 terms correct \\
ag cso
\end{tabular} \\
\hline \& Total \& \& 3 \& \\
\hline \begin{tabular}{l}
3(a) \\
(b) \\
(c)
\end{tabular} \& \[
\begin{aligned}
\& \left(1+4 x^{2}\right)^{\frac{1}{2}} \approx 1+\left(\frac{1}{2}\right)\left(4 x^{2}\right)+\frac{\left(\frac{1}{2}\right)\left(\frac{1}{2}-1\right)\left(4 x^{2}\right)^{2}}{2!} \\
\& \ldots \ldots \ldots=1+2 x^{2}-2 x^{4}+\ldots \\
\& |x|<\frac{1}{2} \\
\& \text { Integral } \approx \int_{0}^{\frac{1}{4}} 1+2 x^{2}-2 x^{4} \mathrm{~d} x \\
\& =\left[x+\frac{2}{3} x^{3}-\frac{2}{5} x^{5}\right]_{0}^{\frac{1}{4}} \\
\& =\frac{1}{4}+\frac{1}{96}-\frac{1}{2560}-0=\frac{1997}{7680}=0.2600 \\
\& {[0.25+0.0104(16 . .)-0.00039(06 . .)]}
\end{aligned}
\] \& \begin{tabular}{l}
M1 \\
A2,1 \\
B2,1 \\
M1 \\
A1J \\
A1
\end{tabular} \& 3
2
2

3 \& | Valid attempt to at least 2 terms |
| :--- |
| A1 for correct expansion and at least 2 of 3 terms tidied correctly |
| B1 for $\left\|4 x^{2}\right\|<1$ or better |
| Integrating 3 terms at least two integrated correctly ft on (a) if equivalent difficulty |
| Accept 0.26 provided clear evidence with no error | <br>

\hline \& Total \& \& 8 \& <br>
\hline
\end{tabular}



| Question Number and part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 5(a) | $y=1$ | B1 | 1 | Must be the equation |
| (b)(i) | $(y-1) x^{2}+3 y x+3 y \quad\{=0\}$ | M1 |  | Attempt to form quadratic in $x$ |
|  |  | A1 |  | Correct quadratic in $x$ |
|  | $\Delta=(3 y)^{2}-4(y-1)(3 y)$ | m1 |  | Considers $b^{2}-4 a c$ |
|  | .... $-3 y^{2}+12 y$ | A1 |  |  |
|  | ..... $-3 y(y-4)$ | m1 |  | Attempt to factorise or solve |
|  | For real $x, \Delta \geq 0 \Rightarrow 0 \leq y \leq 4$ | A1 | 6 | ag cso |
| (ii) | $y=4 \Rightarrow 3 x^{2}+12 x+12=0$ | M1 |  | Substitute $y=4$ to form a 'valid' quadratic in $x$. (PI) |
|  | $\Rightarrow x=-2$, turning point $(-2,4)$ | A1 |  | If not using 'hence' then ( $-2,4$ ) is B1 max. |
|  | $\left\{y=0 \Rightarrow-x^{2}=0 \Rightarrow x=0\right\}$ |  |  |  |
|  | Turning point ( 0,0 ) | B1 | 3 |  |
| (c) | $\bigcap \begin{aligned} & y \uparrow . \\ & 4- \end{aligned}$ | B3,2,1 | 3 | B1 for shape |
|  |  |  |  | B1 for origin as only point where graph meets the axes |
|  |  |  |  | B1 for correct behaviour at the 'endpoints' |
|  | Total |  | 13 |  |





[^0]:    Award method and accuracy marks as appropriate to an alternative solution using a correct method or partially correct method.

