ASSESSMENT and
OUALIFICATIONS
ALLIANCE

## General Certificate of Education

## Mathematics 6300 Specification A

MASI/W Statistics 1

## Mark Scheme

## 2005 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

## MAS1/W

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 1(a) | $\begin{aligned} & \text { Length } X \sim \mathrm{~N}\left(48,8^{2}\right) \\ & \mathrm{P}(X=60)=0 \end{aligned}$ | B1 | 1 | CAO |
| (b) | $\mathrm{P}(X<60)=\mathrm{P}\left(Z<\frac{60-48}{8}\right)$ | M1 |  | standardising (59.5, 60 or 60.5 ) with 48 and $\left(\sqrt{8}, 8\right.$ or $\left.8^{2}\right)$ and/or $(48-x)$ |
|  | $=\mathrm{P}(\mathrm{Z}<1.5)=0.933$ | A1 | 2 | AWRT (0.93319) |
| (c) | $5 \%$ of $48=2.4$ | B1 |  | CAO; OE |
|  | $\mathrm{P}(48-x<X<48+x)$ | M1 |  | attempt at the probability of an interval, symmetric about 48 |
|  | $=\mathrm{P}(-0.3<Z<0.3)$ | A1 |  | CAO 0.3 |
|  | $=\Phi(0.3)-(1-\Phi(0.3))$ | m1 |  | area change |
|  | $=2 \times 0.61791-1$ |  |  |  |
|  | $=0.235$ to 0.236 | A1 | 5 | AWFW (0.23582) |
|  | Total |  | 8 |  |

## MAS1/W (cont)



## MAS1/W (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 3(a) | $A \sim \mathrm{~B}(15,0.68)$ |  |  | binomial only |
|  | $\mathrm{P}(A=10)=\binom{15}{10}(p)^{10}(1-p)^{5}$ | M1 |  | any $p$ providing $0<p<1$ |
|  | $=\binom{15}{10}(0.68)^{10}(0.32)^{5}$ | A1 |  | fully correct expression |
|  | $=3003 \times 0.021139 \times 0.003355=0.213$ | A1 | 3 | AWRT |
| (b) | $B \sim \mathrm{~B}(40,0.45)$ |  |  | binomial only |
|  | $\mathrm{P}(15 \leq B \leq 20)=\mathrm{P}(B \leq 20 \text { or } 19)$ | M1 |  |  |
|  | $-\mathrm{P}(B \leq 14$ or 15$)$ | A1 |  | must include minus |
|  | $=0.7870-0.1326=0.654$ to 0.655 | A1 | 3 | AWFW (0.6844 / 0.2142) |
|  | OR at least 3 terms for $\mathrm{B}(40,0.45)$ answer | (M1) <br> (A2) |  |  |
| (c) | $C \sim \mathrm{~B}(2700,0.25)$ |  |  | Normal approx only |
|  | Mean $(\mu)=675$ | B1 |  | CAO |
|  | Variance ( $\sigma^{2}$ ) $=506(.25)$ | B1 |  | AWRT; SD $=22.5 \mathrm{CAO}$ |
|  | $\mathrm{P}\left(C_{\mathrm{B}}<700\right)=\mathrm{P}\left(C_{\mathrm{N}}<699.5\right)$ | B1 |  | CAO |
|  | $=\mathrm{P}\left(Z<\frac{699.5-675}{22.5}\right)$ | M1 |  | using $\checkmark(\mu \& \sigma)$; not $\sigma^{2}$ <br> allow $(675-x)$ |
|  | $=\mathrm{P}(Z<1.09)=0.861$ to 0.863 | A1 | 5 | AWFW |
| (d) | For each of the 15 times Walk $\mathbf{A}$ is offered select | B1 |  | CAO |
|  | 6 numbers covering at least range 1 to 60 | B1 |  | 1 to 60 ; may be implied by e.g. 2 -digit or (calc value) $\times 60$ |
|  | Ignore repeats and numbers outside range | B1 | 3 | either point |
|  |  |  |  | Note: <br> Use of (a) 0.45 , (b) 0.25 , (c) $0.30 \Rightarrow$ max of M1 A1 A0, M1 A1 A0, B1 B1 B1 M1 A0, 3 |
|  | Total |  | 14 |  |


| $\begin{gathered} \text { MAS1/W (cont } \\ \hline \mathbf{Q} \\ \hline \end{gathered}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Solution | Marks | Total | Comments |
| 4(a)(i) | Weight, $X \sim \mathrm{~N}\left(\mu, 1.6^{2}\right)$ |  |  |  |
|  | $95 \% \Rightarrow z=1.96$ | B1 |  | CAO |
|  | CI for $\mu$ is $\bar{x}(\mu) \pm z \times \frac{\sigma(s)}{\sqrt{n}}$ | M1 |  | use of; must have $(\div \sqrt{n})$ with $n>1$ |
|  | Thus $49.2 \pm 1.96 \times \frac{1.6}{\sqrt{10}}$ | A1 $\checkmark$ |  | $\checkmark$ on $z$ only |
|  | (48.2, 50.2) | A1 | 4 | AWRT; dependent on fully correct expression |
| (ii) | CI includes 50 or UCL > 50 | B1 $\checkmark$ |  | $\checkmark$ on CI |
|  | so suspicion is not supported | B1 $\checkmark$ | 2 | $\checkmark$ on CI; dependent on first B1 |
| (b) | Require $z \frac{\sigma}{\sqrt{n}}=$ or $\leq$ or $<\frac{0.75}{2}$ or 0.75 | M1 |  | use of $z \frac{\sigma}{\sqrt{n}}$ with $n$ unknown |
|  | Thus $1.96 \times \frac{1.6}{\sqrt{n}}=\frac{0.75}{2}=0.375$ or 0.75 | A1 $\checkmark$ |  | $\checkmark$ on $z$; ignore signs |
|  | Thus $n=\left(\frac{1.96 \times 1.6}{0.375}\right)^{2}$ | m1 |  | attempt at solving for $n$ |
|  | Thus $n=70$ | A1 | 4 | CAO (18 with no $\div 2$ ) |
|  |  |  |  | Note: |
|  |  |  |  | Method of 'trial and improvement': $\begin{array}{ll} \text { Answer }=18 \text { CAO } & \text { B2 } \\ \text { Answer }=70 \text { CAO } & \text { B4 } \end{array}$ |
|  | Total |  | 10 |  |

MAS1/W (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 5(a) | $L \sim(580,1600) \quad G=\frac{L}{2}+80$ |  |  |  |
|  | $\mathrm{E}(G)=\frac{580}{2}+80=370$ | B1 |  | CAO |
|  | $\mathrm{V}(G)=\frac{\mathrm{V}(L)}{4}$ | M1 |  | use of $\mathrm{V}(a X+b)=a^{2} \times \mathrm{V}(X)$ with $a \neq 1$ and $b>0$ |
|  | $=400$ | A1 | 3 | CAO |
| (b)(i) | $R=1000-L-G$ | M1 |  | use of |
|  | $=920-\frac{3 L}{2}$ | A1 | 2 | CAO; OE |
| (ii) | $\mathrm{E}(R)=920-\frac{3 \times 580}{2}=50$ | B1 |  | CAO |
|  | $\mathrm{V}(R)=\frac{9 \times \mathrm{V}(L)}{4}$ | M1 |  | Use of $\mathrm{V}(a X+b)=a^{2} \times \mathrm{V}(X)$ with $a \neq \pm 1$ and $b>0$ <br> applied to expression for $R$ |
|  | $=3600$ | A1 | 3 | CAO |
|  |  |  |  | Note: $\begin{aligned} & \sqrt{1600}+\sqrt{400}=40+20=60 \\ & \text { and } 60^{2}=3600 \end{aligned}$ |
|  | Total |  | 8 |  |

## MAS1/W (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 6(a)(i) | $X \sim \mathrm{R}(a, a+k)$ |  |  |  |
|  | $\mathrm{V}(X)=\frac{(a+k-a)^{2}}{12}=\frac{k^{2}}{12}$ | B1 |  | CAO <br> use of $(b-a)$ must include $=k$ |
|  | $\begin{aligned} & =48 \Rightarrow k^{2}=576 \Rightarrow k=24 \\ & \text { or } k=24 \Rightarrow \frac{k^{2}}{12}=\frac{24^{2}}{12}=48 \end{aligned}$ | B1 | 2 | CAO; AG |
| (ii) | $\mathrm{E}(X)=\frac{a+k+a}{2}=a+\frac{k}{2}$ | B1 |  | CAO; OE <br> use of $(a+b)$ must include $=(2 a+k)$ OE |
|  | $=6 \Rightarrow a+12=6 \Rightarrow a=-6$ <br> or $a=-6 \Rightarrow a+\frac{k}{2}=-6+12=6$ | B1 | 2 | CAO; AG |
| (b) | $\mathrm{P}(X>0)=\frac{a+k-0}{a+k-a}=\frac{a+k}{k}$ | M1 |  | attempt at area of a rectangle of height $\frac{1}{k}$ |
|  | $=\frac{3}{4} \text { or } 0.75$ | A1 | 2 | CAO |
| (c)(i) | $\operatorname{Mean}(\bar{X})=6$ | B1 |  | CAO |
|  | $\mathrm{SE}(\bar{X})=\sqrt{\frac{\mathrm{V}(X)}{n}}$ | M1 |  | use of; allow no $\sqrt{ }$ |
|  | $=0.8$ | A1 | 3 | CAO |
| (ii) | Sample size is large $(n>30)$ or Central Limit Theorem | B1 | 1 |  |
| (iii) | $\mathrm{P}(\bar{X}>7)=\mathrm{P}\left(Z>\frac{7-6}{0.8}\right)$ | M1 |  | standardising 7 with answers to (i) and/or ( $6-x$ ) |
|  | $=\mathrm{P}(Z>1.25)=1-\Phi(1.25)$ | m1 |  | area change |
|  | $=0.105 \text { to } 0.106$ | A1 | 3 | AWFW (0.10565) |
|  | Total |  | 13 |  |
|  | TOTAL |  | 60 |  |

