## GCE 2004 June Series

## Mark Scheme

## Mathematics A <br> MAP3

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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## Key to Mark Scheme



## Abbreviations used in Marking



## Application of Mark Scheme

## No method shown:

Correct answer without working..........................................................................mark as in scheme
Incorrect answer without working zero marks unless specified otherwise

## More than one method/choice of solution:

2 or more complete attempts, neither/none crossed out
1 complete and 1 partial attempt, neither crossed out
Crossed out work

## Alternative solution using a correct or partially correct method

mark both/all fully and award the mean mark rounded down award credit for the complete solution only do not mark unless it has not been replaced
award method and accuracy marks as appropriate

MAP3


## MAP3 (Cont)

\begin{tabular}{|c|c|c|c|c|}
\hline Q \& Solution \& Marks \& Total \& Comments \\
\hline 1 cont \& \begin{tabular}{l}
Special Cases (cont) \\
Ins in \(\frac{\mathrm{d} y}{\mathrm{~d} x}\)
\[
\begin{aligned}
\& x=2 t-1 \quad y=\frac{1}{2 \mathrm{t}} \\
\& \frac{\mathrm{~d} x}{\mathrm{~d} t}=2 \quad \frac{\mathrm{~d} y}{\mathrm{~d} t}=\frac{\ln t}{2}
\end{aligned}
\]
\[
\frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{\ln t}{2} \cdot \frac{1}{2}=\frac{\ln t}{4}
\]
\[
t=1, \frac{\mathrm{~d} y}{\mathrm{~d} x}=0
\] \\
B1F
\[
m_{T}=0, \quad m_{N}=\infty
\]
\[
\begin{equation*}
\text { (normal is) } x=1 \tag{3/4}
\end{equation*}
\]
\[
\begin{equation*}
\binom{\text { tangent is }}{\text { normal is }} y=\frac{1}{2} \tag{2/4}
\end{equation*}
\]
\end{tabular} \& \& \& \[
\begin{align*}
\& \frac{\mathrm{d} x}{\mathrm{~d} t}=\ln 2 t \\
\& \frac{\mathrm{~d} y}{\mathrm{~d} x}=\frac{\ln 2 t}{2} \\
\& \frac{\mathrm{~d} y}{\mathrm{~d} x}=\frac{\ln 2}{2} \\
\& m_{T}=\frac{\ln 2}{2}, m_{N}=\frac{-2}{\ln 2} \quad \text { B1F1F } \\
\& \frac{1}{2}=\frac{-2}{\ln 2}+c \quad \text { M1 }  \tag{M1}\\
\& y=\frac{-2}{\ln 2} x+\frac{1}{2}+\frac{2}{\ln 2} \quad \text { A1F }
\end{align*}
\] \\
\hline \& Total \& \& 6 \& \\
\hline \begin{tabular}{l}
2(a) \\
(b)
\end{tabular} \& \[
\begin{aligned}
\& (1+x)^{\frac{1}{3}}=1+\frac{1}{3} x+\frac{1}{3}\left(\frac{1}{3}-1\right) \frac{x^{2}}{2} \\
\& =1+\frac{1}{3} x-\frac{1}{9} x^{2} \\
\& (8+4 x)^{\frac{1}{3}}=\left(8\left(1+\frac{1}{2} x\right)\right)^{\frac{1}{3}} \\
\& =2\left(1+\frac{1}{3} \frac{1}{2} x-\frac{1}{9}\left(\frac{1}{2} x\right)^{2}+\ldots\right)
\end{aligned}
\]
\[
=2+\frac{1}{3} x-\frac{1}{18} x^{2}+\ldots
\] \& \begin{tabular}{l}
M1 \\
A1 \\
B1 \\
M1 \\
A1
\end{tabular} \& 2

3 \& | M1 for expression inside bracket $\begin{aligned} & \text { SC: }(8+4 x)^{\frac{1}{3}} \\ & =8^{\frac{1}{3}}+\frac{1}{3} 8^{-\frac{2}{3}} \cdot 4 x+\frac{1}{3}\left(-\frac{2}{3}\right) 8^{-\frac{5}{3}} \frac{(4 \mathrm{x})^{2}}{2} \\ & \text { M1 for } 8^{\frac{1}{3}} 8^{-\frac{2}{3}}, 8^{-\frac{5}{3}} \\ & \text { M1 for } \left.4 x, \frac{(4 x)^{2}}{2}\right] \\ & =2+\frac{1}{3} x-\frac{1}{18} x^{2} \end{aligned}$ |
| :--- |
| Accept recurring decimals or equiv fractions | <br>

\hline \& Total \& \& 5 \& <br>
\hline
\end{tabular}

MAP3 (Cont)


MAP3 (Cont)

\begin{tabular}{|c|c|c|c|c|}
\hline Q \& Solution \& Marks \& Total \& Comments <br>
\hline 4(a)

(b) \& \[
$$
\begin{aligned}
& 9(y+2)^{2}=5+4(x-1)^{2} \\
& x=2 \quad 9(y+2)^{2}=5+4 \\
& y+2= \pm 1 \quad y=-1,-3 \\
& \frac{\mathrm{~d}}{\mathrm{~d} x}\left(9(y+2)^{2}\right)=\frac{\mathrm{d}}{\mathrm{~d} x}\left(5+4(x-1)^{2}\right) \\
& 18(y+2) \frac{\mathrm{d} y}{\mathrm{~d} x}=0+8(x-1) \\
& (2,-1) \quad(2,-3) \\
& \frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{4}{9} \quad \frac{\mathrm{~d} y}{\mathrm{~d} x}=-\frac{4}{9}
\end{aligned}
$$

\] \& | M1 |
| :--- |
| m1A1 |
| M1 |
| A1A1 |
| m1 |
| A1 | \& 38 \& | Substitute $x=2$ $9(y+2)^{2}=5+4 \times 3^{2} \text { i.e. }(x+1)^{2}$ |
| :--- |
| Find two $y$ values. Coords not required $(y+2)^{2}=\frac{41}{9}, y+2= \pm \frac{\sqrt{41}}{3} \quad$ M1A0 Attempt implicit differentiation with use of chain rule: $\frac{\mathrm{d} y}{\mathrm{~d} x}$ attached to $y$ term, not $x$ term |
| Use $x=2$ and candidate's $y$ values |
| OE; CAO |
| Alternative: explicit differentiation $\begin{aligned} & y=\sqrt{\frac{5+4(x-1)^{2}}{9}}-2 \\ & \frac{\mathrm{~d} y}{\mathrm{~d} x}=\frac{1}{2}\left(\frac{5+4(x-1)^{2}}{9}\right)^{-\frac{1}{2}} \frac{8}{9}(x-1) \end{aligned}$ |
| (M1A2 fully correct; M1A1 if 9 of $\frac{8}{9}$ missing $x=2: \frac{\mathrm{d} y}{\mathrm{~d} x}= \pm \frac{1}{2} \text { (1) } \frac{8}{9}= \pm \frac{4}{9}$ | <br>

\hline \& Total \& \& 8 \& <br>
\hline 5(a)

(b) \& \[
$$
\begin{aligned}
& V=\frac{1}{3} \pi r^{2} h \text { and } r=h(\text { both }) \\
& \Rightarrow V=\frac{1}{3} \pi h^{3} \\
& \frac{\mathrm{~d} V}{\mathrm{~d} t}=3 \\
& 3=\pi h^{2} \frac{\mathrm{~d} h}{\mathrm{~d} t} \\
& h=2 \quad \frac{\mathrm{~d} h}{\mathrm{~d} t}=0.24(\mathrm{~cm} / \mathrm{min})
\end{aligned}
$$

\] \& | B1 |
| :--- |
| B1 |
| M1 |
| A1 | \& 1

3 \& | AG |
| :--- |
| Use $\frac{\mathrm{d} V}{\mathrm{~d} h}$ in chain rule |
| CAO; Condone omission of units unless candidate converts to some other units. | <br>

\hline \& Total \& \& 4 \& <br>
\hline
\end{tabular}



## MAP3 (Cont)



MAP3 (Cont)


