## GCE 2004 June Series

ASSESSMENT and OUALIFICATIONS ALLIANCE

## Mark Scheme

## Mathematics A Unit MAP2

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## Key to Mark Scheme



## Abbreviations used in Marking



## Application of Mark Scheme

## No method shown:

Correct answer without working..........................................................................mark as in scheme
Incorrect answer without working zero marks unless specified otherwise

## More than one method/choice of solution:

2 or more complete attempts, neither/none crossed out
1 complete and 1 partial attempt, neither crossed out
Crossed out work

> Alternative solution using a correct or partially correct method
mark both/all fully and award the mean mark rounded down award credit for the complete solution only do not mark unless it has not been replaced
award method and accuracy marks as appropriate

MAP2


MAP2 (Cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 2(a) | $\begin{aligned} & \sin (\alpha+\beta)=\sin \alpha \cos \beta+\cos \alpha \sin \beta \ldots \ldots \text { (i) } \\ & \sin (\alpha-\beta)=\sin \alpha \cos \beta-\cos \alpha \sin \beta \ldots \ldots \text { (ii) } \end{aligned}$ |  |  |  |
|  | add the two equations (i) \& (ii) together $\sin (\alpha+\beta)+\sin (\alpha-\beta)=2 \sin \alpha \cos \beta$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 2 | AG |
| (b)(i) | $\begin{aligned} 2 \sin 8 x \cos 2 x & =\sin (8 x+2 x)+\sin (8 x-2 x) \\ & =\sin 10 x+\sin 6 x \end{aligned}$ | M1 <br> A1 | 2 |  |
| (ii) | $\int 6 \sin 8 x \cos 2 x d x$ |  |  |  |
|  | $=3 \int(\sin 10 x+\sin 6 x) \mathrm{d} x$ | M1ft |  | Use their (i) |
|  | $=3\left(\frac{-\cos 10 x}{10}-\frac{\cos 6 x}{6}\right)+c$ | M1ft |  | Integration attempted |
|  | $=-\frac{3}{10} \cos 10 x-\frac{1}{2} \cos 6 x+c$ | A1ft | 3 | Any correct form |
|  | Total |  | 7 |  |

MAP2 (Cont)


MAP2 (Cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 4(a)(i) | $\frac{\mathrm{d} y}{\mathrm{~d} x}=\mathrm{e}^{x} \times 2 \cos 2 x+\mathrm{e}^{x} \times \sin 2 x$ | $\begin{gathered} \mathrm{M} 1 \\ \mathrm{~A} 1 \mathrm{~A} 1 \end{gathered}$ | 3 | Use of product rule <br> A1 for each part correct |
| (ii) | $\left.\frac{\mathrm{d} y}{\mathrm{~d} x}\right\|_{x=0}=2$ <br> $\therefore y=m x \Rightarrow$ equation of tangent at $(0,0)$ is $y=2 x$ | M1 |  |  |
| (b) | $\left.\frac{\mathrm{d} y}{\mathrm{~d} x}\right\|_{r=\pi}=2 \mathrm{e}^{\pi}$ |  |  |  |
|  | $\therefore$ gradient of normal at $x=\pi$ is $-\frac{1}{2 \mathrm{e}^{\pi}}$ | M1 |  | Use of $m_{1} \times m_{2}=-1$ $(-0.216)$ |
|  | $\therefore$ equation of normal at $(\pi, 0)$ is given by $y=-\frac{1}{2 \mathrm{e}^{\pi}}(x-\pi)$ | M1ft |  | on their gradient of normal |
|  | $\Rightarrow 2 \mathrm{e}^{\pi} y+x=\pi$ | A1 | 4 | AG (any correct form) |
|  | Total |  | 9 |  |

## MAP2 (Cont)



MAP2 (Cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 6(a)(i) | $C(4,3)$ | B1 |  |  |
| (ii) | $r=2$ | B1 | 2 |  |
| (b)(i) | $(x-4)^{2}+(y-3)^{2}=4 \quad \text { and } \quad y=x+1$ meet when $(x-4)^{2}+(x+1-3)^{2}=4$ $\Rightarrow \quad(x-4)^{2}+(x-2)^{2}=4$ | M1 |  | Substitution attempted or eliminating $x$ |
|  | $\begin{array}{r} \left(x^{2}-8 x+16\right)+\left(x^{2}-4 x+4\right)=4 \\ 2 x^{2}-12 x+20=4 \end{array}$ | M1 |  | Multiply out correctly and simplification attempted |
|  | $x^{2}-6 x+8=0$ | A1 |  | quadratic |
|  | $(x-4)(x-2)=0$ | M1 |  | factorise/other valid method attempted |
|  | $\begin{array}{rl}  & x=4 \text { or } x=2 \\ x=4 \Rightarrow \\ x=2 \Rightarrow y=5 \\ x & y(4,5) \& B(2,3) \end{array}$ | A1ft | 5 | Both points (cao) |
| (ii) | $\text { Area of segment }=\frac{1}{4} \pi(2)^{2}-\frac{1}{2}(2 \times 2)$ | M1 |  | $\frac{1}{4} \times$ circle - triangle |
|  |  | A1ft |  | (on their value of $r$ ) |
|  | $=\pi-2$ | A1 | 3 | AG (AWRT 1.14) |
|  | Total |  | 10 |  |
|  | Total |  | 60 |  |

