

Please write clearly, in block capitals.

Centre number

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Candidate number

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Surname

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Forename(s)

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Candidate signature

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# A-level FURTHER MATHEMATICS

## Paper 3 - Statistics

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Exam Date

Morning

Time allowed: 2 hours

### Materials

For this paper you must have:

- You must ensure you have the other optional question paper/answer booklet for which you are entered (**either** Mechanics **or** Discrete). You will have 2 hours to complete both papers.
- The AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

### Instructions

- Use black ink or black ball-point pen. Pencil should be used for drawing.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 50.

### Advice

Unless stated otherwise, you may quote formulae, without proof, from the booklet.  
You do not necessarily need to use all the space provided.

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Answer **all** questions in the spaces provided.

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- 1** A  $\chi^2$ -test for association is carried out on frequency data given in a  $5 \times 3$  contingency table using the 5% level of significance. All expected frequencies are greater than 5
- State the number of degrees of freedom for this test.

Circle your answer.

**[1 mark]**

6

8

14

15

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- 2 The continuous random variable  $Y$  has cumulative distribution function defined by

$$F(y) = \begin{cases} 0 & y < 0 \\ \frac{y^2}{36} & 0 \leq y \leq 6 \\ 1 & y > 6 \end{cases}$$

Find the value of  $P(Y > 4)$

Circle your answer.

[1 mark]

$$\frac{4}{9}$$

$$\frac{5}{9}$$

$$\frac{16}{27}$$

$$\frac{11}{27}$$

- 3 The continuous random variable  $R$  follows a rectangular distribution with probability density function given by

$$f(r) = \begin{cases} k & -a \leq r \leq b \\ 0 & \text{otherwise} \end{cases}$$

Prove, using integration, that  $E(R) = \frac{1}{2}(b - a)$

[4 marks]

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- 4 David, a zoologist, is investigating a particular species of monitor lizard. He measures the lengths, in centimetres, of a random sample of this particular species of lizard. His measured lengths are

53.2 57.8 55.3 58.9 59.0 60.2 61.8 62.3 65.4 66.5

The lengths may be assumed to be normally distributed.

David correctly constructed a 90% confidence interval for the mean length of lizard

using the measured lengths given and the formula  $\bar{x} \pm \left( b \times \frac{s}{\sqrt{n}} \right)$

This interval had limits of 57.63 and 62.45, correct to two decimal places.

- 4 (a) State the value for  $b$  used in David's formula.

[1 mark]

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- 4 (b) David interprets his interval and states,

"My confidence interval indicates that exactly 90% of the population of lizard lengths for this particular species lies between 57.63 cm and 62.45 cm".

Do you think David's statement is true? Explain your reasoning.

[2 marks]

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- 4 (c)** David's assistant, Amina, correctly constructs a  $\beta\%$  confidence interval from David's random sample of measured lengths.

Amina informs David that the width of her confidence interval is 8.54.

Find the value of  $\beta$ .

**[3 marks]**

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**Turn over for the next question**









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**6 (a) (ii)** Given that  $c = 0.1$ , find the value of  $E(T)$

**[3 marks]**

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**6 (b)** Show that  $E(\sqrt{|T|}) = \frac{5\sqrt{2} + 52\sqrt{3}}{50}$

**[3 marks]**

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7 (a) (ii) State the assumption that it was necessary for you to make in order for the test in part (a)(i) to be valid.

[1 mark]

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7 (b) State the changes that would be required to your test in part (a) if you were told that the standard deviation of the level of impurity is known to be 0.25 per cent.

[2 marks]

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Turn over for the next question

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**8** The time in hours to failure of a component may be modelled by an exponential distribution with parameter  $\lambda = 0.025$

In a manufacturing process, the machine involved uses one of these components continuously until it fails.

The component is then immediately replaced.

**8 (a)** Write down the mean time to failure for a component.

**[1 mark]**

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**8 (b)** Find the probability that a component will fail during a 12-hour shift.

**[1 mark]**

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**8 (c)** A component has not failed for 30 hours. Find the probability that this component lasts for at least another 30 hours.

**[2 marks]**

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**8 (d)** Find the probability that a component does **not** fail during 4 consecutive 12-hour shifts. **[3 marks]**

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**8 (e) (i)** State the distribution that can be used to model the number of components that fail during one hour of the manufacturing process. **[2 marks]**

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**8 (e) (ii)** Hence, or otherwise, find the probability that no components fail during 5 consecutive 12-hour shifts. **[2 marks]**

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**END OF QUESTIONS**