Centre Number			Candidate Number		
Surname					
Other Names					
Candidate Signature					



General Certificate of Education Advanced Subsidiary Examination June 2014

Mathematics

MFP1

Unit Further Pure 1

Tuesday 10 June 2014 9.00 am to 10.30 am

For this paper you must have:

• the blue AQA booklet of formulae and statistical tables. You may use a graphics calculator.

Time allowed

• 1 hour 30 minutes

Instructions

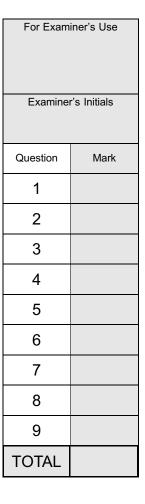
- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer all questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do not use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.





Answer all questions.

Answer each question in the space provided for that question.

1 A curve passes through the point (9, 6) and satisfies the differential equation

$$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{1}{2 + \sqrt{x}}$$

Use a step-by-step method with a step length of 0.25 to estimate the value of y at x=9.5. Give your answer to four decimal places.

QUESTION PART REFERENCE	Answer space for question 1



QUESTION PART REFERENCE	Answer space for question 1
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•••••	



2 The quadratic equation

$$2x^2 + 8x + 1 = 0$$

has roots α and β .

(a) Write down the value of $\alpha + \beta$ and the value of $\alpha\beta$.

[2 marks]

(b) (i) Find the value of $\alpha^2 + \beta^2$.

[2 marks]

(ii) Hence, or otherwise, show that $\alpha^4 + \beta^4 = \frac{449}{2}$.

[2 marks]

(c) Find a quadratic equation, with integer coefficients, which has roots

$$2\alpha^4 + \frac{1}{\beta^2} \text{ and } 2\beta^4 + \frac{1}{\alpha^2}$$

QUESTION PART REFERENCE	Answer space for question 2



QUESTION PART REFERENCE	Answer space for question 2



3	Use the formulae for $\sum_{r=1}^{n} r^3$ and $\sum_{r=1}^{n} r^2$ to find the value of
	$\sum_{r=3}^{60} r^2(r-6)$

[4 marks]

QUESTION	Annual and for supplier 2
QUESTION PART REFERENCE	Answer space for question 3
REFERENCE	



QUESTION PART REFERENCE	Answer space for question 3



4 Find the complex number *z* such that

$$5iz + 3z^* + 16 = 8i$$

Give your answer in the form $\,a+b{\rm i}\,,$ where a and b are real.

[6 marks]

QUESTION PART REFERENCE	Answer space for question 4



QUESTION PART REFERENCE	Answer space for question 4



3		A curve C has equation $y = x(x + 3)$.	
(a	1)	Find the gradient of the line passing through the point $(-5, 10)$ and the point with <i>x</i> -coordinate $-5 + h$. Give your answer in its simplest form.	
			[3 marks]
(b)	Show how the answer to part (a) can be used to find the gradient of the curve the point $(-5, 10)$. State the value of this gradient.	ve C at
			[2 marks]
QUESTION PART REFERENCE	Ansv	wer space for question 5	



QUESTION PART REFERENCE	Answer space for question 5



6 A curve C has equation $y = \frac{1}{x(x+2)}$.

(a) Write down the equations of all the asymptotes of C.

[2 marks]

- (b) The curve C has exactly one stationary point. The x-coordinate of the stationary point is -1.
 - (i) Find the *y*-coordinate of the stationary point.

[1 mark]

(ii) Sketch the curve C.

[2 marks]

(c) Solve the inequality

$$\frac{1}{x(x+2)} \leqslant \frac{1}{8}$$

QUESTION PART REFERENCE	Answer space for question 6



QUESTION PART REFERENCE	Answer space for question 6



QUESTION PART REFERENCE	Answer space for question 6



QUESTION PART REFERENCE	Answer space for question 6



- 7 (a) Write down the 2×2 matrix corresponding to each of the following transformations:
 - (i) a reflection in the line y = -x;

[1 mark]

(ii) a stretch parallel to the y-axis of scale factor 7.

[1 mark]

(b) Hence find the matrix corresponding to the combined transformation of a reflection in the line y = -x followed by a stretch parallel to the *y*-axis of scale factor 7.

[2 marks]

- (c) The matrix ${\bf A}$ is defined by ${\bf A}=\begin{bmatrix} -3 & -\sqrt{3} \\ -\sqrt{3} & 3 \end{bmatrix}$.
 - (i) Show that $A^2 = kI$, where k is a constant and I is the 2×2 identity matrix.

[1 mark]

(ii) Show that the matrix ${\bf A}$ corresponds to a combination of an enlargement and a reflection. State the scale factor of the enlargement and state the equation of the line of reflection in the form $y=(\tan\theta)x$.

QUESTION PART REFERENCE	Answer space for question 7



QUESTION PART REFERENCE	Answer space for question 7



8 (a) Find the general solution of the equation

$$\cos\left(\frac{5}{4}x - \frac{\pi}{3}\right) = \frac{\sqrt{2}}{2}$$

giving your answer for x in terms of π .

[5 marks]

(b) Use your general solution to find the **sum** of all the solutions of the equation $\cos\left(\frac{5}{4}x-\frac{\pi}{3}\right)=\frac{\sqrt{2}}{2} \text{ that lie in the interval } 0\leqslant x\leqslant 20\pi \text{ . Give your answer in the form } k\pi \text{ , stating the exact value of } k.$

[4 marks]

QUESTION PART REFERENCE	Answer space for question 8



QUESTION PART REFERENCE	Answer space for question 8



9 An ellipse E has equation

$$\frac{x^2}{16} + \frac{y^2}{9} = 1$$

- (a) Sketch the ellipse E, showing the values of the intercepts on the coordinate axes. [2 marks]
- (b) Given that the line with equation y = x + k intersects the ellipse E at two distinct points, show that -5 < k < 5.

[5 marks]

(c) The ellipse E is translated by the vector $\begin{bmatrix} a \\ b \end{bmatrix}$ to form another ellipse whose equation is $9x^2 + 16y^2 + 18x - 64y = c$. Find the values of the constants a, b and c.

[5 marks]

(d) Hence find an equation for each of the two tangents to the ellipse $9x^2 + 16y^2 + 18x - 64y = c$ that are parallel to the line y = x.

[3 marks]

QUESTION PART REFERENCE	Answer space for question 9



QUESTION PART REFERENCE	Answer space for question 9



QUESTION PART REFERENCE	Answer space for question 9



QUESTION PART REFERENCE	Answer space for question 9
	END OF QUESTIONS



