

General Certificate of Education
June 2007
Advanced Level Examination



MATHEMATICS
Unit Mechanics 2B

MM2B

Thursday 7 June 2007 9.00 am to 10.30 am

For this paper you must have:

- an 8-page answer book
- the **blue** AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed: 1 hour 30 minutes

Instructions

- Use blue or black ink or ball-point pen. Pencil should only be used for drawing.
- Write the information required on the front of your answer book. The *Examining Body* for this paper is AQA. The *Paper Reference* is MM2B.
- Answer **all** questions.
- Show all necessary working; otherwise marks for method may be lost.
- The **final** answer to questions requiring the use of calculators should be given to three significant figures, unless stated otherwise.
- Take $g = 9.8 \text{ m s}^{-2}$, unless stated otherwise.

Information

- The maximum mark for this paper is 75.
- The marks for questions are shown in brackets.
- Unit Mechanics 2B has a **written paper only**.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.

Answer **all** questions.

- 1 A hot air balloon moves vertically upwards with a constant velocity. When the balloon is at a height of 30 metres above ground level, a box of mass 5 kg is released from the balloon.

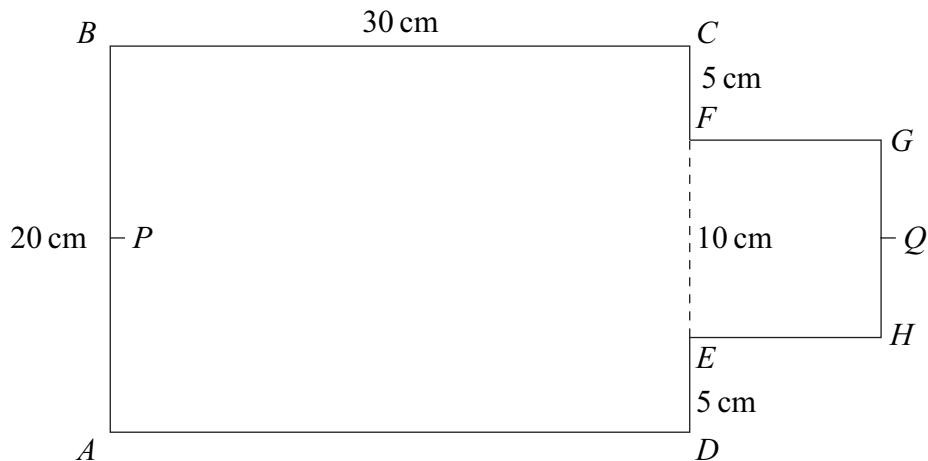
After the box is released, it initially moves vertically upwards with speed 10 m s^{-1} .

- (a) Find the initial kinetic energy of the box. (2 marks)
- (b) Show that the kinetic energy of the box when it hits the ground is 1720 J. (3 marks)
- (c) Hence find the speed of the box when it hits the ground. (3 marks)
- (d) State **two** modelling assumptions which you have made. (2 marks)

- 2 A uniform lamina is in the shape of a rectangle $ABCD$ and a square $EFGH$, as shown in the diagram.

The length AB is 20 cm, the length BC is 30 cm, the length DE is 5 cm and the length EF is 10 cm.

The point P is the midpoint of AB and the point Q is the midpoint of HG .



- (a) Explain why the centre of mass of the lamina lies on PQ . (1 mark)
- (b) Find the distance of the centre of mass of the lamina from AB . (4 marks)
- (c) The lamina is freely suspended from A .

Find, to the nearest degree, the angle between AD and the vertical when the lamina is in equilibrium. (4 marks)

- 3 A particle has mass 800 kg. A single force of $(2400\mathbf{i} - 4800t\mathbf{j})$ newtons acts on the particle at time t seconds. No other forces act on the particle.

- (a) Find the acceleration of the particle at time t . *(2 marks)*
- (b) At time $t = 0$, the velocity of the particle is $(6\mathbf{i} + 30\mathbf{j})\text{ m s}^{-1}$. The velocity of the particle at time t is $\mathbf{v}\text{ m s}^{-1}$.

Show that

$$\mathbf{v} = (6 + 3t)\mathbf{i} + (30 - 3t^2)\mathbf{j} \quad (4 \text{ marks})$$

- (c) Initially, the particle is at the point with position vector $(2\mathbf{i} + 5\mathbf{j})\text{ m}$.

Find the position vector, \mathbf{r} metres, of the particle at time t . *(5 marks)*

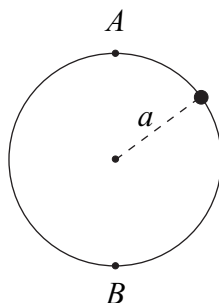
- 4 A uniform plank is 10 m long and has mass 15 kg. It is placed on horizontal ground at the edge of a vertical river bank, so that 2 m of the plank is projecting over the edge, as shown in the diagram below.



- (a) A woman of mass 50 kg stands on the part of the plank which projects over the river.
- Find the greatest distance from the river bank at which she can safely stand. *(3 marks)*
- (b) The woman wishes to stand safely at the end of the plank which projects over the river.
- Find the minimum mass which she should place on the other end of the plank so that she can do this. *(4 marks)*
- (c) State how you have used the fact that the plank is uniform in your solution. *(1 mark)*
- (d) State one other modelling assumption which you have made. *(1 mark)*

Turn over ►

- 5 A bead of mass m moves on a smooth circular ring of radius a which is fixed in a vertical plane, as shown in the diagram. Its speed at A , the highest point of its path, is v and its speed at B , the lowest point of its path, is $7v$.



- (a) Show that $v = \sqrt{\frac{ag}{12}}$. (5 marks)
- (b) Find the reaction of the ring on the bead, in terms of m and g , when the bead is at A . (4 marks)
- 6 An elastic string has one end attached to a point O , fixed on a horizontal table. The other end of the string is attached to a particle of mass 5 kilograms. The elastic string has natural length 2 metres and modulus of elasticity 200 newtons. The particle is pulled so that it is 2.5 metres from the point O and it is then released from rest on the table.
- (a) Calculate the elastic potential energy when the particle is 2.5 m from the point O . (2 marks)
- (b) If the table is smooth, show that the speed of the particle when the string becomes slack is $\sqrt{5} \text{ m s}^{-1}$. (3 marks)
- (c) The table is, in fact, rough and the coefficient of friction between the particle and the table is 0.4.
- Find the speed of the particle when the string becomes slack. (7 marks)

- 7 A stone of mass m is moving along the smooth horizontal floor of a tank which is filled with a viscous liquid. At time t , the stone has speed v . As the stone moves, it experiences a resistance force of magnitude λmv , where λ is a constant.

(a) Show that

$$\frac{dv}{dt} = -\lambda v \quad (2 \text{ marks})$$

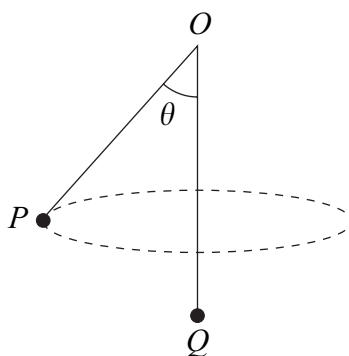
(b) The initial speed of the stone is U .

Show that

$$v = Ue^{-\lambda t} \quad (4 \text{ marks})$$

- 8 A particle, P , of mass 3 kg is attached to one end of a light inextensible string. The string passes through a smooth fixed ring, O , and a second particle, Q , of mass 5 kg is attached to the other end of the string. The particle Q hangs at rest vertically below the ring and the particle P moves with speed 4 m s^{-1} in a horizontal circle, as shown in the diagram.

The angle between OP and the vertical is θ .



- (a) Explain why the tension in the string is 49 N. (2 marks)
- (b) Find θ . (3 marks)
- (c) Find the radius of the horizontal circle. (4 marks)

END OF QUESTIONS

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