

## AS Level Further Mathematics B (MEI)

### Y410 Core Pure

#### Sample Question Paper

Version 2.1

## Date – Morning/Afternoon

Time allowed: 1 hour 15 minutes

#### You must have:

- Printed Answer Booklet
- Formulae Further Mathematics B (MEI)

#### You may use:

- a scientific or graphical calculator



### INSTRUCTIONS

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer **all** the questions.
- **Write your answer to each question in the space provided in the Printed Answer Booklet.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

### INFORMATION

- The total number of marks for this paper is **60**.
- The marks for each question or part question are shown in brackets [ ].
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is used. You should communicate your method with correct reasoning.
- The Printed Answer Booklet consists of **12** pages. The Question Paper consists of **4** pages.

Answer **all** the questions.

1 The complex number  $z_1$  is  $1+i$  and the complex number  $z_2$  has modulus 4 and argument  $\frac{\pi}{3}$ .

(i) Express  $z_2$  in the form  $a+bi$ , giving  $a$  and  $b$  in exact form. [2]

(ii) Express  $\frac{z_2}{z_1}$  in the form  $c+di$ , giving  $c$  and  $d$  in exact form. [2]

2 (i) Describe fully the transformation represented by the matrix  $\begin{pmatrix} 1 & 2 \\ 0 & 1 \end{pmatrix}$ . [2]

(ii) A triangle of area 5 square units undergoes the transformation represented by the matrix  $\begin{pmatrix} 1 & 2 \\ 0 & 1 \end{pmatrix}$ .

Explaining your reasoning, find the area of the image of the triangle following this transformation. [2]

3 (i) Write down, in complex form, the equation of the locus represented by the circle in the Argand diagram shown in Fig. 3. [2]

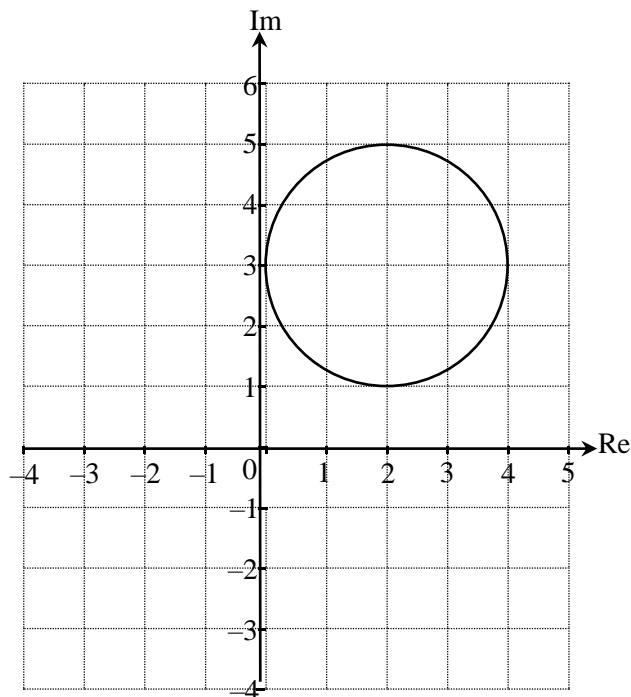


Fig. 3

(ii) On the copy of Fig. 3 in the Printed Answer Booklet mark with a cross any point(s) on the circle for which  $\arg(z-2i) = \frac{\pi}{4}$ . [2]

## 3

- 4 (i) Find the coordinates of the point where the following three planes intersect. Give your answers in terms of  $a$ .

$$\begin{aligned}x - 2y - z &= 6 \\3x + y + 5z &= -4 \\-4x + 2y - 3z &= a\end{aligned}$$

[4]

- (ii) Determine whether the intersection of the three planes could be on the  $z$ -axis.

[2]

- 5 The cubic equation  $x^3 - 4x^2 + px + q = 0$  has roots  $\alpha$ ,  $\frac{2}{\alpha}$  and  $\alpha + \frac{2}{\alpha}$ .

Find

- the values of the roots of the equation,
- the value of  $p$ .

[7]

- 6 (i) Show that, when  $n = 5$ ,  $\sum_{r=n+1}^{2n} r^2 = 330$ .

[1]

- (ii) Find, in terms of  $n$ , a fully factorised expression for  $\sum_{r=n+1}^{2n} r^2$ .

[4]

- 7 The plane  $\Pi$  has equation  $3x - 5y + z = 9$ .

- (i) Show that  $\Pi$  contains

- the point  $(4, 1, 2)$

and

- the vector  $\begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix}$ .

[4]

- (ii) Determine the equation of a plane which is perpendicular to  $\Pi$  and which passes through  $(4, 1, 2)$ . [3]

**8 In this question you must show detailed reasoning.**

(i) Explain why all cubic equations with real coefficients have at least one real root. [2]

(ii) Points representing the three roots of the equation  $z^3 + 9z^2 + 27z + 35 = 0$  are plotted on an Argand diagram.

Find the exact area of the triangle which has these three points as its vertices. [7]

**9** You are given that matrix  $\mathbf{M} = \begin{pmatrix} -3 & 8 \\ -2 & 5 \end{pmatrix}$ .

(i) Prove that, for all positive integers  $n$ ,  $\mathbf{M}^n = \begin{pmatrix} 1-4n & 8n \\ -2n & 1+4n \end{pmatrix}$ . [6]

(ii) Determine the equation of the line of invariant points of the transformation represented by the matrix  $\mathbf{M}$ . [3]

It is claimed that the answer to part (ii) is also a line of invariant points of the transformation represented by the matrix  $\mathbf{M}^n$ , for any positive integer  $n$ .

(iii) Explain *geometrically* why this claim is true. [2]

(iv) Verify *algebraically* that this claim is true. [3]

**END OF QUESTION PAPER**

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**...day June 20XX – Morning/Afternoon**

**AS Level Further Mathematics B (MEI)**

**Y410 Core Pure**

**SAMPLE MARK SCHEME**

**Duration:** 1 hour 15 minutes

**MAXIMUM MARK      60**

**This document consists of 16 pages**

## Text Instructions

## 1. Annotations and abbreviations

Annotation in scoris	Meaning
✓ and ✖	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark scheme	Meaning
E1	Mark for explaining a result or establishing a given result
U1	Mark for correct units
G1	Mark for a correct feature on a graph
dep*	Mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This indicates that the instruction <b>In this question you must show detailed reasoning</b> appears in the question.

**2. Subject-specific Marking Instructions for AS Level Further Mathematics B (MEI)**

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

**M**

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

**A**

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

**B**

Mark for a correct result or statement independent of Method marks.

**E**

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

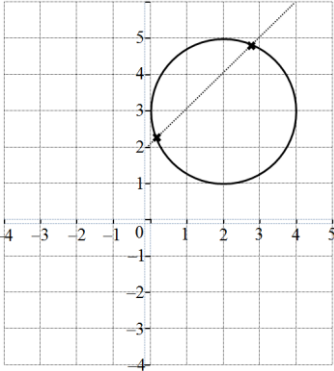
Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep\*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be ‘follow through’. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for *g*. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate’s data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some papers. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. ‘Fresh starts’ will not affect an earlier decision about a misread. Note that a miscopy of the candidate’s own working is not a misread but an accuracy error.
- i If a graphical calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.
- k Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned on this occasion, but shows what a complete solution might look like



Question		Answer	Marks	AOs	Guidance	
1	(i)	$z_2 = 4 \left( \cos \frac{\pi}{3} + i \sin \frac{\pi}{3} \right)$ $= 2 + 2\sqrt{3}i$	<b>M1</b>  <b>A1</b> <b>[2]</b>	<b>1.1</b>  <b>1.1</b>	May be implied  or exact equivalent	$a = 2, b = 2\sqrt{3}$
1	(ii)	$\frac{z_2}{z_1} = \frac{(2+2\sqrt{3}i)(1-i)}{(1+i)(1-i)}$ $= \frac{(2+2\sqrt{3})+(2\sqrt{3}-2)i}{2}$ $= (\sqrt{3}+1) + (\sqrt{3}-1)i$	<b>M1</b>  <b>A1 FT</b> <b>[2]</b>	<b>1.1a</b>  <b>1.1</b>	FT their $z_2$  Must be simplified	
2	(i)	Shear $x$ -axis fixed, (0,1) to (2,1)	<b>B1</b> <b>B1</b> <b>[2]</b>	<b>1.2</b> <b>1.1</b>	allow $x$ -axis invariant, [shear] factor 2.	
2	(ii)	Shear preserves area $\Rightarrow$ New area[ = 5 $\times$ 1] = 5 (square units)	<b>B1</b>  <b>B1</b> <b>[2]</b>	<b>2.2a</b>  <b>1.1</b>	Or $\det \mathbf{M} = 1$	

Question		Answer	Marks	AOs	Guidance
3	(i)	$ z - (2 + 3i)  = 2$	M1 A1 [2]	1.1 1.1	Form $ z - \alpha  = k$ All correct Cartesian form of equation scores <b>M0A0</b> .
3	(ii)	<p>Attempt at locus <math>\arg(z - 2i) = \frac{\pi}{4}</math> drawn soi.</p> 	M1 A1  [2]	3.1a 1.1	Line at acute angle to real axis Half-line from 2i  A0 if any other wrong point marked.

Question	Answer	Marks	AOs	Guidance
4 (i)	$\begin{bmatrix} 1 & -2 & -1 \\ 3 & 1 & 5 \\ -4 & 2 & -3 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 6 \\ -4 \\ a \end{bmatrix}$ $\Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 13 & 8 & 9 \\ 11 & 7 & 8 \\ -10 & -6 & -7 \end{bmatrix} \begin{bmatrix} 6 \\ -4 \\ a \end{bmatrix}$ $= \begin{bmatrix} 46+9a \\ 38+8a \\ -36-7a \end{bmatrix}$ <p>So coordinates <math>(46+9a, 38+8a, -36-7a)</math></p>	<p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>A1</b></p> <p><b>[4]</b></p>	<p><b>1.1a</b></p> <p><b>1.1</b></p> <p><b>1.1</b></p> <p><b>2.5</b></p>	<p>Implied used of matrices</p> <p>Attempt to use inverse matrix BC</p> <p>All three elements correct.</p> <p>Answer written as coordinates, with at least one element correct.</p>
4 (ii)	$46+9a=0 \text{ so } a=-\frac{46}{9}$ $38+8 \times \left(-\frac{46}{9}\right) \neq 0 \text{ so there is no intersection on the } z\text{-axis as both } x \text{ and } y \text{ coordinates would need to be zero}$	<p><b>M1</b></p> <p><b>A1</b></p> <p><b>[2]</b></p>	<p><b>3.1a</b></p> <p><b>2.1</b></p>	<p>Find value of <math>a</math> for <math>x</math> or <math>y</math>-coordinate to be zero</p> <p>Complete clear argument with correct conclusion (allow FT from their (i))</p>
<p><b>Alternate Method</b></p> <p><b>M1</b> attempt at elimination of one variable</p> <p><b>M1</b> attempt at elimination of second variable</p>				
<p><b>Alternate method</b></p> <p><b>M1</b> <math>x=y=0</math> so <math>z=-6</math> on first plane</p> <p><b>A1</b> <math>z=-0.8</math> on second plane so no intersection on <math>z</math>-axis.</p>				

Question		Answer	Marks	AOs	Guidance	
5		$\alpha + \frac{2}{\alpha} + \alpha + \frac{2}{\alpha} = 4$ $\alpha^2 - 2\alpha + 2 = 0$ $\alpha = 1 \pm i$ Roots are $1+i, 1-i, 2$ $p = (1+i)(1-i) + 2(1+i) + 2(1-i)$ $= 2 + 2 + 2i + 2 - 2i$ $= 6$	<b>M1</b> <b>M1</b> <b>A1</b> <b>A1</b>  <b>M1</b> <b>A1</b> <b>A1</b> <b>[7]</b>	<b>1.1a</b>  <b>3.1a</b>  <b>1.1</b> <b>3.2a</b>  <b>3.1a</b>  <b>1.1</b> <b>1.1</b>	Attempt to use sum of roots  Interpret solution of quadratic to get all three roots of cubic  Some correct simplification	
6	(i)	$6^2 + 7^2 + 8^2 + 9^2 + 10^2$ $= 330 \text{ AG}$	<b>B1</b>  <b>[1]</b>	<b>1.1</b>	Must show method	Or 385-55
6	(ii)	$\sum_{r=1}^{2n} r^2 - \sum_{r=1}^n r^2$ $= \frac{1}{6}(2n)(2n+1)(4n+1) - \frac{1}{6}(n)(n+1)(2n+1)$ $= \frac{1}{6}n(2n+1)((8n+2) - (n+1))$ $= \frac{1}{6}n(2n+1)(7n+1)$	<b>M1</b>  <b>A1</b>  <b>M1</b>  <b>A1</b>  <b>[4]</b>	<b>3.1a</b>   <b>1.1</b>  <b>1.1</b>  <b>1.1</b>	For attempt at difference  For successful substitution of $2n$ into formula Factors $n$ and $2n+1$  oe, must be correct and factorised	

Question	Answer	Marks	AOs	Guidance
7 (i)	Substituting $x = 4, y = 1, z = 2$ into LHS of equation of plane, $3 \times 4 - 5 \times 1 + 2$ $= 12 - 5 + 2$ $= 9$ $= \text{RHS}$ $\begin{pmatrix} 3 \\ -5 \\ 1 \end{pmatrix} \cdot \begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix}$ $= 3 \times 1 - 5 \times 1 + 2$ $= 0$ Normal vector for plane is perpendicular to $\begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix}$ , so $\begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix}$ is in the plane.	E1    M1   A1   E1   [4]	1.1    3.1a   1.1   2.4	

Question		Answer	Marks	AOs	Guidance
7	(ii)	$\begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix}$ is a suitable normal vector for second plane, [because it is perpendicular to normal vector of $\Pi$ ]. $x + y + 2z = \dots$ $\phantom{x + y + 2z} = 9$	<b>E1</b>   <b>M1</b> <b>A1</b>   <b>[3]</b>	<b>3.1a</b>   <b>1.1</b> <b>1.1</b>	Many other solutions are possible e.g. Show $\begin{pmatrix} 5 \\ 3 \\ 0 \end{pmatrix}$ is perpendicular to $\begin{pmatrix} 3 \\ -5 \\ 1 \end{pmatrix}$ using scalar product <b>E1</b> $5x + 3y = \dots$ <b>M1</b> $\phantom{5x + 3y} = 23$ <b>A1</b>

Question		Answer	Marks	AOs	Guidance		
8	(i)	DR					
		<b>Either</b> If it has a complex root, the complex conjugate is also a root. Hence complex roots occur in pairs and, as the equation has three roots, at least one must be real.	E1	2.1			
			E1	2.4			
		<b>Or</b> Based on graph of $y = f(x)$ . If coefficient of $x^3$ is positive then $y$ is negative for large negative $x$ and positive for large positive $x$ , so graph (which is continuous) cuts $x$ -axis at least once – giving a real root of $f(x) = 0$ . If coefficient of $x^3$ is negative then $y$ is positive for large negative $x$ and negative for large positive $x$ , so graph (which is continuous) again cuts $x$ -axis at least once – giving a real root of $f(x) = 0$ .	E1				
			E1				
			[2]				

Question		Answer	Marks	AOs	Guidance
8	(ii)	DR $f(-5) = 0$ $\Rightarrow z + 5$ is a factor $z^3 + 9z^2 + 27z + 35 = (z + 5)(z^2 + 4z + 7)$ $z^2 + 4z + 7 = 0 \Rightarrow (z + 2)^2 + 3 = 0$ $\Rightarrow$ roots are $-5, -2 \pm \sqrt{3}i$ Roots form triangle, area $\frac{1}{2} \times 2\sqrt{3} \times 3$ $= 3\sqrt{3}$ (square units)	<b>M1</b>  <b>A1</b> <b>B1</b>  <b>M1</b>  <b>A1</b> <b>M1</b>  <b>A1</b>  <b>[7]</b>	<b>3.1a</b>  <b>1.1</b> <b>1.1</b>  <b>1.1</b>  <b>2.1</b>  <b>3.2a</b>  <b>1.1</b>	$f(\pm 1)$ or $f(\pm 5)$ or $f(\pm 7)$ correctly must be seen Finding $z + 5$ is a factor Correct factorising  Attempt at solving quadratic must be seen  Any valid method attempted on any 3 distinct non-collinear roots, however obtained, must be seen FT their roots as above <b>A0</b> for decimal answer



Question	Answer	Marks	AOs	Guidance
9 (i)	<p>When <math>n = 1</math>, <math>\mathbf{M}^1 = \begin{pmatrix} 1-4 &amp; 8 \\ -2 &amp; 1+4 \end{pmatrix} = \begin{pmatrix} -3 &amp; 8 \\ -2 &amp; 5 \end{pmatrix}</math></p> <p>Assume true for <math>n = k</math>: <math>\mathbf{M}^k = \begin{pmatrix} 1-4k &amp; 8k \\ -2k &amp; 1+4k \end{pmatrix}</math></p> <p><math>\mathbf{M}^{k+1} = \mathbf{M}^k \times \mathbf{M} = \begin{pmatrix} 1-4k &amp; 8k \\ -2k &amp; 1+4k \end{pmatrix} \begin{pmatrix} -3 &amp; 8 \\ -2 &amp; 5 \end{pmatrix}</math></p> <p><math>= \begin{pmatrix} -3-4k &amp; 8+8k \\ -2-2k &amp; 5+4k \end{pmatrix}</math></p> <p><math>= \begin{pmatrix} 1-4(k+1) &amp; 8(k+1) \\ -2(k+1) &amp; 1+4(k+1) \end{pmatrix}</math></p> <p>which is the formula with <math>n = k + 1</math>. Therefore if true for <math>n</math>, true for <math>n + 1</math>.</p> <p>True for 1 <math>\Rightarrow</math> true for 2, 3,... and all positive integers</p>	<p><b>B1</b></p> <p><b>E1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>A1</b></p> <p><b>E1</b></p> <p>[6]</p>	<p><b>1.1</b></p> <p><b>2.1</b></p> <p><b>1.1</b></p> <p><b>2.1</b></p> <p><b>2.4</b></p> <p><b>2.2a</b></p>	<p>OR <math>\mathbf{M}^{k+1} = \mathbf{M} \times \mathbf{M}^k = \begin{pmatrix} -3 &amp; 8 \\ -2 &amp; 5 \end{pmatrix} \begin{pmatrix} 1-4k &amp; 8k \\ -2k &amp; 1+4k \end{pmatrix}</math></p> <p>Not required to check both ways round.</p> <p>Convincingly expressed in terms of <math>k + 1</math></p> <p>Completion of proof by induction. Dependent on <b>B1</b> and previous <b>E1</b></p>
9 (ii)	<p><math>\begin{pmatrix} -3 &amp; 8 \\ -2 &amp; 5 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} x \\ y \end{pmatrix}</math></p> <p><math>\Rightarrow -3x + 8y = x, -2x + 5y = y</math></p> <p><math>\Rightarrow y = \frac{1}{2}x</math></p>	<p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p>[3]</p>	<p><b>1.1a</b></p> <p><b>1.1</b></p> <p><b>2.2a</b></p>	<p>Using <math>\mathbf{Mx} = \mathbf{x}</math></p> <p>Obtaining an equation</p> <p>Any correct form; must state both equations lead to this answer.</p>

Question		Answer	Marks	AOs	Guidance
9	(iii)	<p><math>M^n</math> represents the transformation repeated <math>n</math> times.</p> <p>Each repeat leaves points on <math>y = \frac{1}{2}x</math> unchanged.</p>	<p>E1</p> <p>E1</p> <p>[2]</p>	<p>2.4</p> <p>2.1</p>	
9	(iv)	$\begin{pmatrix} 1-4n & 8n \\ -2n & 1+4n \end{pmatrix} \begin{pmatrix} x \\ \frac{1}{2}x \end{pmatrix}$ $= \begin{pmatrix} x-4nx+8n(\frac{1}{2}x) \\ -2nx+\frac{1}{2}x+4n(\frac{1}{2}x) \end{pmatrix}$ $= \begin{pmatrix} x \\ \frac{1}{2}x \end{pmatrix}$ <p>so same invariant line for all <math>n</math>.</p>	<p>M1</p> <p>A1</p> <p>E1</p> <p>[3]</p>	<p>1.1</p> <p>1.1</p> <p>2.3</p>	<p>Multiplication with some progress</p> <p>cao</p>

Question	AO1	AO2	AO3(PS)	AO3(M)	Total
1i	2	0	0	0	2
1ii	2	0	0	0	2
2i	2	0	0	0	2
2ii	1	1	0	0	2
3i	2	0	0	0	2
3ii	1	0	1	0	2
4i	3	1	0	0	4
4ii	0	1	1	0	2
5	4	0	3	0	7
6i	1	0	0	0	1
6ii	3	0	1	0	4
7i	2	1	1	0	4
7ii	2	0	1	0	3
8i	0	2	0	0	2
8ii	4	1	2	0	7
9i	2	4	0	0	6
9ii	2	1	0	0	3
9iii	1	1	0	0	2
9iv	2	1	0	0	3
<b>Totals</b>	36	14	10	0	60

## Summary of Updates

Date	Version	Change
October 2019	2	Amendments to the front cover rubric instructions to candidates
November 2022	2.1	Correction of minor typographical error in the markscheme

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## AS Level Further Mathematics B (MEI)

### Y410 Core Pure

Printed Answer Booklet

Version 2

## Date – Morning/Afternoon

Time allowed: 1 hour 15 minutes

**You must have:**

- Question Paper Y410 (inserted)
- Formulae Further Mathematics B (MEI)

**You may use:**

- a scientific or graphical calculator



First name

Last name

Centre number

Candidate number

### INSTRUCTIONS

- The Question Paper will be found inside the Printed Answer Booklet.
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer **all** the questions.
- **Write your answer to each question in the space provided in the Printed Answer Booklet.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

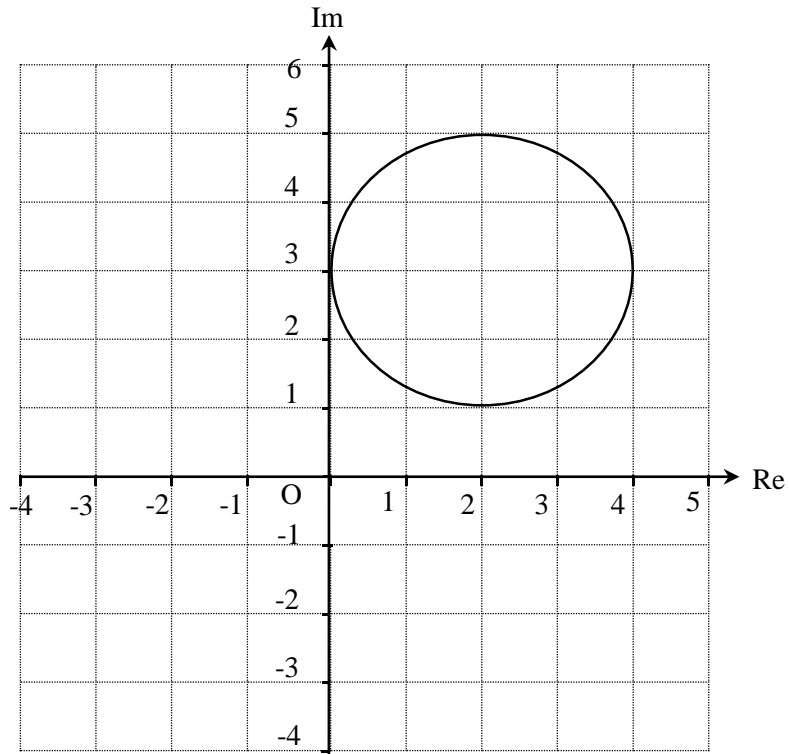
### INFORMATION

- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is used. You should communicate your method with correct reasoning.
- The Printed Answer Booklet consists of **12** pages. The Question Paper consists of **4** pages.

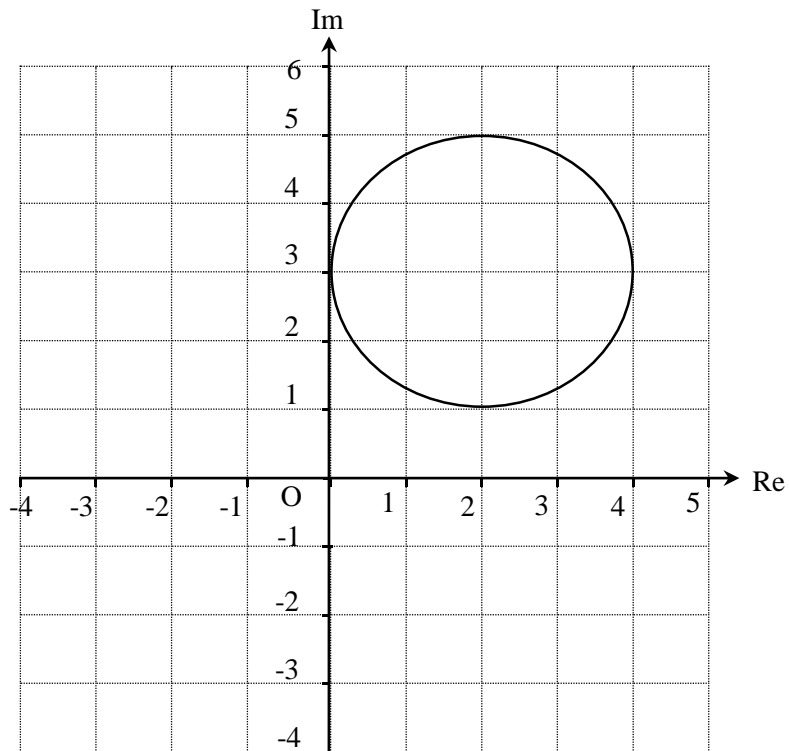
<b>1 (i)</b>	
<b>1 (ii)</b>	
<b>2 (i)</b>	
<b>2 (ii)</b>	

3 (i)

3 (ii)



Spare copy of graph for question 3 (ii)



<b>4 (i)</b>	
<b>4 (ii)</b>	





<b>6 (i)</b>	
<b>6 (ii)</b>	









<b>9 (ii)</b>	
<b>9 (iii)</b>	
<b>9 (iv)</b>	

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