

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										



General Certificate of Education  
Advanced Level Examination  
June 2014

# Mathematics

# MS04

## Unit Statistics 4

Tuesday 24 June 2014 9.00 am to 10.30 am

**For this paper you must have:**

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

**Time allowed**

- 1 hour 30 minutes

- Instructions**
- Use black ink or black ball-point pen. Pencil should only be used for drawing.
  - Fill in the boxes at the top of this page.
  - Answer **all** questions.
  - Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
  - You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
  - Do not write outside the box around each page.
  - Show all necessary working; otherwise marks for method may be lost.
  - Do all rough work in this book. Cross through any work that you do not want to be marked.
  - The **final** answer to questions requiring the use of tables or calculators should normally be given to three significant figures.

- Information**
- The marks for questions are shown in brackets.
  - The maximum mark for this paper is 75.

- Advice**
- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
  - You do not necessarily need to use all the space provided.

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
<b>TOTAL</b>	



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Answer **all** questions.

Answer each question in the space provided for that question.

**1** The continuous random variable  $T$  has probability density function  $f(t)$ , where

$$f(t) = \begin{cases} 5e^{-5t} & t \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

**(a)** Derive the cumulative distribution function of  $T$ . **[4 marks]**

**(b)** Find the probability that  $T > E(T)$ . **[1 mark]**

**(c)** Find the value of the constant  $c$  such that  $P(T > c) = 0.05$ . **[2 marks]**

QUESTION  
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QUESTION  
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QUESTION  
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QUESTION  
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QUESTION  
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QUESTION  
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**7 (a)** The random variable  $X$  has a geometric distribution with parameter  $p$ .

(i) Prove, from first principles, that  $E(X^2) = \frac{1}{p} + \frac{2(1-p)}{p^2}$ .

[4 marks]

(ii) Hence, given that  $E(X) = \frac{1}{p}$ , deduce that  $\text{Var}(X) = \frac{(1-p)}{p^2}$ .

[1 mark]

(iii) Given that  $p = \frac{1}{2}$ , calculate  $P(X > \text{Var}(X))$ .

[3 marks]

(b) As part of their archery practice, Robin and William are playing a game consisting of a number of rounds. For each round of the game, they each shoot one arrow at the gold inner circle of a target. The probability that Robin hits the gold with any one arrow is  $\frac{1}{5}$ , independently of all previous shots. The probability that William hits the gold with any one arrow is  $\frac{1}{6}$ , independently of all previous shots. In each round, Robin shoots first.

If, in a round, they both hit the gold, then the game is drawn.

If, in a round, Robin hits the gold and then William misses the gold, then Robin wins the game.

If, in a round, Robin misses the gold and then William hits the gold, then William wins the game.

If, in a round, they both miss the gold, then the game continues to the next round.

Find the probability that:

(i) the game is drawn after no more than three rounds have been completed;

[3 marks]

(ii) the game is drawn;

[2 marks]

(iii) Robin wins the game.

[3 marks]

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QUESTION  
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**END OF QUESTIONS**



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ANSWER IN THE SPACES PROVIDED**

