

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
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5	
6	
7	
TOTAL	



General Certificate of Education
Advanced Level Examination
June 2014

Mathematics

MM03

Unit Mechanics 3

Friday 6 June 2014 1.30 pm to 3.00 pm

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The **final** answer to questions requiring the use of calculators should be given to three significant figures, unless stated otherwise.
- Take $g = 9.8 \text{ m s}^{-2}$, unless stated otherwise.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



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Answer **all** questions.

Answer each question in the space provided for that question.

- 1** A tennis ball is projected from a point O with a velocity of $(4\sqrt{3}\mathbf{i} + 4\mathbf{j}) \text{ m s}^{-1}$, where \mathbf{i} and \mathbf{j} are horizontal and vertical unit vectors respectively. The ball travels in a vertical plane through O which is 30 cm above the horizontal surface of a tennis court. During its flight, the horizontal and upward vertical distances of the ball from O are x metres and y metres respectively.

Model the ball as a particle.

- (a)** Show that, during the flight, the equation of the trajectory of the ball is given by

$$y = \frac{x}{\sqrt{3}} - \frac{49x^2}{480}$$

[4 marks]

- (b)** The ball hits a vertical net at a point A . The net is at a horizontal distance of 4 m from O .

Determine the height of the point A , above the surface of the tennis court. Give your answer to the nearest centimetre.

[2 marks]

- (c)** State a modelling assumption, other than the ball being a particle, that you need to make to answer this question.

[1 mark]

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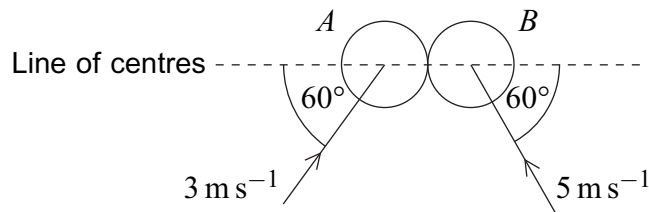
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- 6** Two smooth spheres, A and B , have equal radii and masses 2 kg and 4 kg respectively.

The spheres are moving on a smooth horizontal surface and collide. As they collide, A has velocity 3 m s^{-1} at an angle of 60° to the line of centres of the spheres, and B has velocity 5 m s^{-1} at an angle of 60° to the line of centres, as shown in the diagram.



Just after the collision, B moves in a direction perpendicular to the line of centres.

- (a) Find the speed of A immediately after the collision. **[6 marks]**
- (b) Find the acute angle, correct to the nearest degree, between the velocity of A and the line of centres immediately after the collision. **[2 marks]**
- (c) Find the coefficient of restitution between the spheres. **[2 marks]**
- (d) Find the magnitude of the impulse exerted on B during the collision. **[2 marks]**

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- 7 Two small smooth spheres, A and B , are the same size and have masses $2m$ and m respectively. Initially, the spheres are at rest on a smooth horizontal surface. The sphere A receives an impulse of magnitude J and moves with speed $2u$ directly towards B .

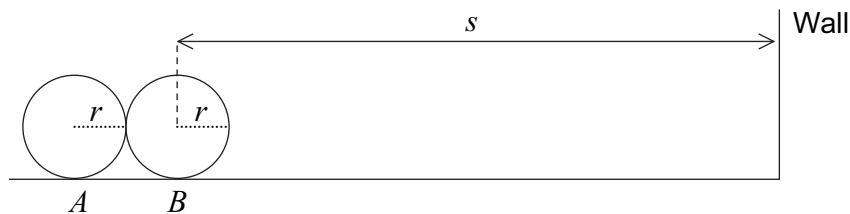
(a) Find J in terms of m and u .

[2 marks]

(b) The sphere A collides directly with B . The coefficient of restitution between A and B is $\frac{2}{3}$. Find, in terms of u , the speeds of A and B immediately after the collision.

[5 marks]

(c) At the instant of collision, the centre of B is at a distance s from a fixed smooth vertical wall which is at right angles to the direction of motion of A and B , as shown in the diagram.

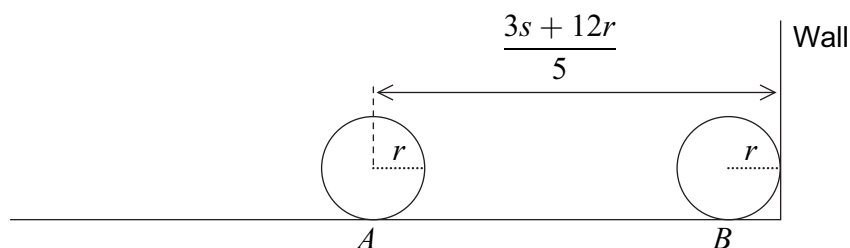


Subsequently, B collides with the wall. The radius of each sphere is r .

Show that the distance of the centre of A from the wall at the instant that B hits the wall is $\frac{3s + 12r}{5}$.

[4 marks]

(d) The diagram below shows the positions of A and B when B hits the wall.



The sphere B collides with A again after rebounding from the wall. The coefficient of restitution between B and the wall is $\frac{2}{5}$.

Find the distance of the **centre of B** from the wall at the instant when A and B collide again.

[4 marks]



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END OF QUESTIONS



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