

General Certificate of Education

Mathematics 6360

MPC1 Pure Core 1

Mark Scheme

2008 examination - January series

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Key to mark scheme and abbreviations used in marking

| M | mark is for method | | | |
|-------------|--|-----|----------------------------|--|
| m or dM | mark is dependent on one or more M marks and is for method | | | |
| A | mark is dependent on M or m marks and is for accuracy | | | |
| В | mark is independent of M or m marks and is for method and accuracy | | | |
| E | mark is for explanation | | | |
| √or ft or F | follow through from previous | | | |
| | incorrect result | MC | mis-copy | |
| CAO | correct answer only | MR | mis-read | |
| CSO | correct solution only | RA | required accuracy | |
| AWFW | anything which falls within | FW | further work | |
| AWRT | anything which rounds to | ISW | ignore subsequent work | |
| ACF | any correct form | FIW | from incorrect work | |
| AG | answer given | BOD | given benefit of doubt | |
| SC | special case | WR | work replaced by candidate | |
| OE | or equivalent | FB | formulae book | |
| A2,1 | 2 or 1 (or 0) accuracy marks | NOS | not on scheme | |
| –x EE | deduct x marks for each error | G | graph | |
| NMS | no method shown | c | candidate | |
| PI | possibly implied | sf | significant figure(s) | |
| SCA | substantially correct approach | dp | decimal place(s) | |

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

MPC1

| MPCI | Calad' | M - 1 | Tr. 4 1 | C |
|------------|--|------------|----------|---|
| Q | Solution | Marks | Total | Comments |
| 1(a) | Mid-point of $BC = (3, -2)$ | B1 | | Either coordinate correct |
| | | B1 | 2 | Both cords correct. Accept $x = 3$, $y = -2$ |
| | | | | |
| (b)(i) | $\Delta y = 3-1$ | M1 | | $\pm \frac{2}{6}$ OE implies M1 |
| (b)(i) | $\frac{\Delta y}{\Delta x} = \frac{3-1}{-2-4}$ | IVI I | | 6 Thipnes WI |
| | $=-\frac{1}{2}$ | | | |
| | $=-\frac{1}{2}$ | A1 | 2 | |
| | 3 | | | |
| (ii) | y-3 = "their grad" $(x+2)$ or | | | Or $y = mx + c$ and correct attempt to |
| (11) | y - 3 = their grad (x + 2) or y - 1 = "their grad" (x - 4) | M1 | | find c |
| | Hence $x + 3y = 7$ | A1 | 2 | iniq c |
| | Thence $x + 3y = 7$ | AI | 2 | |
| (iii) | y + 5 = "their grad AB " $(x - 2)$ | M1 | | Or "their $x + qy = c$ " and attempt to find c |
| (111) | | 1411 | | or then x + qy = c and attempt to find c |
| | $y+5=-\frac{1}{3}(x-2)$ or $x+3y+13=0$ | A1 | 2 | OE |
| | 3. | | | |
| | | | | |
| (c) | Grad $BC = 3$ (from $\frac{\Delta y}{\Delta x} = \frac{1+5}{4-2}$ OE) | B1 | | Or 2 lengths correct: |
| | $\Delta x = 4-2$ | D 1 | | $AB = \sqrt{40}; BC = \sqrt{40}; AC = \sqrt{80}$ |
| | $m_1 m_2 = -1$ stated or | | | |
| | 1 | | | |
| | grad $BC = 3$ and grad $AB = -\frac{1}{3}$ or | M1 | | Or attempt at Pythagoras or Cosine Rule |
| | , | 1711 | | Of attempt at 1 yanagoras of Cosme Rule |
| | grad $BC \times \text{grad } AB \ (=3 \times -\frac{1}{3})$ | | | |
| | 3 | | | |
| | Product of gradients $= -1$ | A1 | _ | $AC^2 = AB^2 + BC^2 \Rightarrow \angle ABC = 90^\circ$ |
| | Hence AB and BC are perpendicular | CSO | 3 | Completing proof and statement |
| | Total | | 11 | Completing proof and statement |
| | 1 Otal | M1 | 11 | Reduce one power by 1 |
| 2(a) | $\frac{\mathrm{d}y}{\mathrm{d}x} = 4x^3 - 32$ | A1 | | One term correct |
| 2(a) | dx = 1x - 32 | A1 | 3 | All correct (no $+ c$ etc) |
| | | 711 | 3 | Thi correct (no + c etc) |
| | dy | | | |
| (b) | Stationary point $\Rightarrow \frac{dy}{dx} = 0$ | M1 | | |
| | | | | 1 |
| | $\Rightarrow x^3 = 8$ | A1√ | | $x^n = k$ following from their $\frac{dy}{dx}$ |
| | _ | | | u.x |
| | $\Rightarrow x = 2$ | A 1 | 3 | CSO |
| | $\Rightarrow x^3 = 8$ $\Rightarrow x = 2$ $\frac{d^2 y}{dx^2} = 12x^2$ | | | |
| (c)(i) | $\frac{\mathrm{d}^2 y}{12x^2} = 12x^2$ | B1√ | 1 | FT their $\frac{dy}{dx}$ |
| (0)(1) | $\frac{dx^2}{dx^2}$ = 12x | DI√ | 1 | $\frac{1}{dx}$ |
| | | | | |
| | d^2v | , | | dv |
| (ii) | When $x = 2$, $\frac{d^2y}{dx^2}$ considered | M1 | | Or complete test with $2 \pm \varepsilon$ using $\frac{dy}{dx}$ |
| | \Rightarrow minimum point | E1√ | 2 | dx |
| | — minimum point | L1V | <i>_</i> | |
| | .a | | | |
| (d) | Putting $x = 0$ into their $\frac{dy}{dx}$ (= -32) | M1 | | |
| | dx | | | |
| | $\frac{dy}{dx} < 0 \Rightarrow$ decreasing | A1√ | 2 | Allow "increasing" if their $\frac{dy}{dx} > 0$ |
| | dx | 111V | | $\frac{1}{dx}$ |
| | Total | | 11 | |

MPC1 (cont)

| 3(a) | $5\sqrt{8} = 10\sqrt{2}$ | | | - L |
|---------|---|------------|----|--|
| | 370 - 1072 | B1 | | Or $\frac{5\sqrt{16}+6}{\sqrt{2}}$ gets B1 |
| | $\frac{6}{\sqrt{2}} = \frac{6\sqrt{2}}{2} \qquad (=3\sqrt{2})$ | M1 | | then M1 for rationalising; and A1 answer |
| | Answer = $13\sqrt{2}$ | A1 | 3 | n=13 |
| (b) | $\frac{\sqrt{2}+2}{3\sqrt{2}-4} \times \frac{3\sqrt{2}+4}{3\sqrt{2}+4}$ | M1 | | Multiplying top & bottom by $\pm (3\sqrt{2} + 4)$ |
| | $Numerator = 6 + 6\sqrt{2} + 4\sqrt{2} + 8$ | m1 | | Multiplying out (condone one slip) |
| | Denominator = $18 - 16 $ (= 2) | B1 | | |
| | Final answer = $5\sqrt{2} + 7$ | A1 | 4 | |
| 4(a) | $\frac{\text{Total}}{x^2 + (y - 5)^2}$ | B1 | 7 | <i>b</i> = 5 |
| , , | RHS = 5 | В1 В1 | 2 | $\begin{vmatrix} b-5\\k=5 \end{vmatrix}$ |
| | | D1 | 2 | |
| (b)(i) | Centre (0, 5) | B1√ | 1 | FT their b from part (a) |
| (ii) | Radius = $\sqrt{5}$ | B1√ | 1 | FT their k from part (a); RHS must be > 0 |
| (/ (/ | $x^2 + 4x^2 - 20x + 20 = 0$ | M1 | | May substitute into original or "their (a)" |
| | $\Rightarrow x^2 - 4x + 4 = 0$ | A1 | 2 | CSO; AG |
| (ii) | $(x-2)^2 = 0$ or $x = 2$ | M1 | | |
| | Repeated root implies tangent | E1 | | Or $b^2 - 4ac$ shown = 0 plus statement |
| | Point of contact is $P(2, 4)$ | A1 | 3 | |
| (d) | $\left(CQ^2 = \right)1^2 + 1^2$ | M1 | | FT their C |
| | $\sqrt{2} < \sqrt{5} \implies Q$ lies inside circle | A1 | 2 | CQ or CQ^2 OE must appear for A1 |
| | Total | CSO | 11 | og o |
| 5(a) | (9+x)(1-x) | M1 | | $\pm (9 \pm x)(1 \pm x)$ |
| | | A1 | 2 | Correct factors |
| (b) | $25 - (x^2 + 8x + 16) = 9 - 8x - x^2$ | B1 | 1 | AG |
| (c)(i) | x = -4 is line of symmetry | B1 | 1 | |
| (ii) | Vertex is (-4, 25) | B1,B1 | 2 | |
| (iii) | _ <i>y</i> _ | M1 | | General ∩ shape |
| | 9 | B1 | | −9 and 1 marked on <i>x</i> -axis or stated |
| | x | A 1 | 3 | 9 marked on y-axis and maximum to the |
| | -9/ 1 | | | left of <i>y</i> -axis Must continue below <i>x</i> -axis at both ends |
| | Total | | 9 | Wast continue below x-axis at both ends |

MPC1 (cont)

| Q Q | Solution | Marks | Total | Comments |
|---------|--|----------|-------|---|
| 6(a)(i) | p(-1) = -1 + 7 - 6 | M1 | | Finding p(-1) |
| | = 0 therefore $x + 1$ is a factor | A1 | 2 | Shown to $= 0$ plus statement |
| (ii) | $p(x) = (x+1)(x^2 - x - 6)$ | M1 | | Long division/inspection (2 terms correct) |
| | | A1 | | Quadratic factor correct |
| | p(x) = (x+1)(x+2)(x-3) | A1 | 3 | May earn M1,A1 for correct second factor then A1 for $(x+1)(x+2)(x-3)$ |
| (b)(i) | A(-2,0) | B1 | 1 | Condone $x = -2$ |
| (**) | $x^4 - 7x^2$ | 3.41 | | |
| (11) | $\frac{x^4}{4} - \frac{7x^2}{2} - 6x (+c)$ | M1 A1 | | One term correct |
| | $\frac{1}{2}$ (may have + c or not) | A1 A1 | | Another term correct All correct unsimplified |
| | (may have te of hot) | Aı | | All correct unshipfilled |
| | $\left[\frac{81}{4} - \frac{63}{2} - 18\right] - \left[\frac{1}{4} - \frac{7}{2} + 6\right]$ | m1 | | F(3) - F(-1) attempted in correct order |
| | = - 32 | A1 | 5 | CSO; OE |
| (iii) | Area of shaded region = 32 | B1√ | 1 | FT their (b)(ii) but positive value needed |
| | dy | M1 | | One term correct |
| (iv) | $\frac{dy}{dx} = 3x^2 - 7$ | A1 | | All correct (no $+ c$ etc) |
| | uл | | 3 | CSO |
| | When $x = -1$, gradient = -4 | A1 | 3 | CSO |
| (v) | Gradient of normal = $\frac{1}{4}$ | B1√ | | |
| | $y =$ "their gradient" $(x \pm 1)$ | M1 | | Must be finding normal , not tangent |
| | $y = \frac{1}{4}(x+1)$ | A1 | 3 | CSO; any correct form eg $4y - x = 1$ |
| | Total | | 18 | |
| 7(a) | $x^{2} + 7 = k(3x+1) \Rightarrow x^{2} - 3kx + 7 - k = 0$ | B1 | 1 | AG |
| (b) | $b^2 - 4ac = (-3k)^2 - 4(7-k)$ | M1 | | Clear attempt at $b^2 - 4ac$ |
| | | | | Condone slip in one term of expression |
| | (2 distinct roots when) $b^2 - 4ac > 0$ | B1 | | Must involve <i>k</i> |
| | $9k^2 + 4k - 28 > 0$ | A1 | 3 | CSO; AG |
| (c) | (9k-14)(k+2) | M1 | | Factors or formula correct unsimplified |
| | Critical points -2 and $\frac{14}{9}$ | A1 | | |
| | $\frac{2}{9}$ | AI | | |
| | Sketch ∪ or sign diagram correct | M1 | | +ve -ve +ve -2 <u>14</u> |
| | $k < -2, k > \frac{14}{9}$ | A1 | 4 | 9 |
| | Total | | 8 | |
| | TOTAL | | 75 | |
| | TOTAL | <u> </u> | 13 | 1 |