

## **General Certificate of Education**

# **Mathematics 6360**

MM1A Mechanics 1A

# **Mark Scheme**

2007 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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### Key to mark scheme and abbreviations used in marking

M	mark is for method				
m or dM	mark is dependent on one or more M marks and is for method				
A	mark is dependent on M or m marks and is for accuracy				
В	mark is independent of M or m marks and is for method and accuracy				
Е	mark is for explanation				
$\sqrt{\text{or ft or F}}$	follow through from previous				
	incorrect result	MC	mis-copy		
CAO	correct answer only	MR	mis-read		
CSO	correct solution only	RA	required accuracy		
AWFW	anything which falls within	FW	further work		
AWRT	anything which rounds to	ISW	ignore subsequent work		
ACF	any correct form	FIW	from incorrect work		
AG	answer given	BOD	given benefit of doubt		
SC	special case	WR	work replaced by candidate		
OE	or equivalent	FB	formulae book		
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme		
−x EE	deduct x marks for each error	G	graph		
NMS	no method shown	c	candidate		
PI	possibly implied	sf	significant figure(s)		
SCA	substantially correct approach	dp	decimal place(s)		

#### No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

June 07

### MM1A

Q	Solution	Marks	Total	Comments
1(a)	$320 = \frac{1}{2} \times a \times 80^2$	M1		Use of constant acceleration equation with $u = 0$
		A1		Correct equation
	$a = \frac{2 \times 320}{80^2} = 0.1 \text{ ms}^{-2}$	A1	3	AG Correct acceleration from correct working
(b)	$v = 0 + 0.1 \times 80$	M1		Use of constant acceleration equation with $u = 0$
	$= 8 \text{ ms}^{-1}$	A1	2	Correct velocity
(c)	$L - 450 \times 9.8 = 450 \times 0.1$	M1		Three term equation of motion
		A1		Correct equation
	L = 45 + 4410			
	= 4455			
	= 4500N  (to 3sf)	A1	3	AG Correct force
(d)	4410 N	В1	1	Correct force
	Total		9	
2(a)	$2\begin{bmatrix} 3 \\ 1 \end{bmatrix} + 2\begin{bmatrix} -4 \\ -5 \end{bmatrix}$	M1		Three term vector equation for
	$2\begin{bmatrix} 3 \\ -2 \end{bmatrix} + 3\begin{bmatrix} -4 \\ 1 \end{bmatrix} = 5\mathbf{v}$	A1		conservation of momentum Correct equation
	1[-6] [-12]	711		Correct equation
	$\mathbf{v} = \frac{1}{5} \begin{bmatrix} -6\\ -1 \end{bmatrix} = \begin{bmatrix} -1.2\\ -0.2 \end{bmatrix}$	A1	3	Correct velocity
(b)	$v = \sqrt{1.2^2 + 0.2^2} = 1.22 \text{ ms}^{-1}$	M1		Finding speed from their velocity in part (a)
		A1F	2	(must include addition of two terms) Correct speed from their velocity Accept 1.21
	Total		5	

MM1A (cont)

Q Q	Solution	Marks	Total	Comments
3(a)	$T_1 \sin 35^\circ = T_2 \sin 35^\circ$	M1		Resolving two forces and forming an
	$T_1 = T_2$			equation, with different tensions for each
	OR	A1	2	string Correct result from correct working
	$T_1 \cos 55^\circ = T_2 \cos 55^\circ$	711	2	Correct result from correct working
	$T_1 = T_2$			
	$I_1 - I_2$			
(b)	$T_1 \cos 35^\circ + T_2 \cos 35^\circ = 2 \times 9.8$	M1		Resolving forces to form a three term
, ,	1 2			vertical equation
		A1		Correct equation
	$T_1 \cos 35^\circ + T_1 \cos 35^\circ = 2 \times 9.8$	A1		$T_1$ or $T_2$ eliminated correctly
	2×9.8	dM1		Solving for $T_1$ or $T_2$
	$T_1 = \frac{2 \times 9.8}{2 \cos 35^{\circ}} = 12.0 \text{ N (to 3sf)}$	A1	5	Correct tension
	200833			Accept 12 N or 11.9 N
	2 40 250 0.0			
(c)	$2\times40\cos35^\circ=9.8m$	M1 A1		Forming an equation to find <i>m</i>
	80 cos 35°	Al		Correct equation
	$m = \frac{80\cos 35^{\circ}}{9.8} = 6.69 \text{ kg}$	A1	3	Correct mass
	OR			
	$m = \frac{40}{11.96} \times 2$			
	=6.69  kg			
	Tot	al	10	
4(a)	3.45g - T = 3.45a	M1		Three term equation of motion for one
		A1		particle Correct equation
	T - 1.45g = 1.45a	M1		Three term equation of motion for other
				particle
		A1		particle Correct equation
	2g = 4.9a	A1		
	9		E	Correct equation
	2g = 4.9a $a = \frac{2 \times 9.8}{4.9} = 4 \text{ ms}^{-2}$	A1	5	Correct equation  AG Correct acceleration from correct
	9		5	Correct equation
(b)	9		5	Correct equation  AG Correct acceleration from correct
(b)	$a = \frac{2 \times 9.8}{4.9} = 4 \text{ ms}^{-2}$	A1	5	Correct equation  AG Correct acceleration from correct working
(b)	$a = \frac{2 \times 9.8}{4.9} = 4 \text{ ms}^{-2}$ $T = 1.45 \times 4 + 1.45 \times 9.8$ $= 20.01$	A1 M1		Correct equation  AG Correct acceleration from correct working  Use of one equation from (a) to find T
	$a = \frac{2 \times 9.8}{4.9} = 4 \text{ ms}^{-2}$ $T = 1.45 \times 4 + 1.45 \times 9.8$ $= 20.01$ $= 20.0 \text{ N (to 3 sf)}$	A1	5	Correct equation  AG Correct acceleration from correct working
	$a = \frac{2 \times 9.8}{4.9} = 4 \text{ ms}^{-2}$ $T = 1.45 \times 4 + 1.45 \times 9.8$ $= 20.01$ $= 20.0 \text{ N (to 3 sf)}$	A1 M1 A1		Correct equation  AG Correct acceleration from correct working  Use of one equation from (a) to find T  Correct T
	$a = \frac{2 \times 9.8}{4.9} = 4 \text{ ms}^{-2}$ $T = 1.45 \times 4 + 1.45 \times 9.8$ $= 20.01$ $= 20.0 \text{ N (to 3 sf)}$	A1 M1		Correct equation  AG Correct acceleration from correct working  Use of one equation from (a) to find T
	$a = \frac{2 \times 9.8}{4.9} = 4 \text{ ms}^{-2}$ $T = 1.45 \times 4 + 1.45 \times 9.8$ $= 20.01$ $= 20.0 \text{ N (to 3 sf)}$	A1 M1 A1		Correct equation  AG Correct acceleration from correct working  Use of one equation from (a) to find T  Correct T
	$a = \frac{2 \times 9.8}{4.9} = 4 \text{ ms}^{-2}$ $T = 1.45 \times 4 + 1.45 \times 9.8$ $= 20.01$ $= 20.0 \text{ N (to 3 sf)}$	A1 M1 A1 M1		Correct equation  AG Correct acceleration from correct working  Use of one equation from (a) to find $T$ Correct $T$ Use of $s = \frac{1}{2}$
	$a = \frac{2 \times 9.8}{4.9} = 4 \text{ ms}^{-2}$ $T = 1.45 \times 4 + 1.45 \times 9.8$ $= 20.01$ $= 20.0 \text{ N (to 3 sf)}$	A1 M1 A1 M1		Correct equation  AG Correct acceleration from correct working  Use of one equation from (a) to find $T$ Correct $T$ Use of $s = \frac{1}{2}$ Use of constant acceleration equation with
	$a = \frac{2 \times 9.8}{4.9} = 4 \text{ ms}^{-2}$ $T = 1.45 \times 4 + 1.45 \times 9.8$ $= 20.01$	A1 M1 A1 M1 M1	2	Correct equation  AG Correct acceleration from correct working  Use of one equation from (a) to find $T$ Correct $T$ Use of $s = \frac{1}{2}$ Use of constant acceleration equation with $u = 0$

MM1A (cont)

Q Q	Solution	Marks	Total	Comments
5(a)	$V = 150 \tan 30^{\circ}$	M1		Using trigonometry (usually tan or sine
				rule) to find $V$
	$= 86.6 \text{ ms}^{-1}$	A1	2	AG Correct answer from correct working
		111	_	(Division by 2 only acceptable if sin 30°
	OR			or cos 60° seen)
	V 150			,
	$\frac{V}{\sin 30^{\circ}} = \frac{150}{\sin 60^{\circ}}$			
	$V = 86.6 \text{ ms}^{-1}$			
	, 0010 1110			
<b>(b)</b>	150	M1		Using trigonometry or Pythagoras to find <i>v</i>
	$\frac{150}{v} = \cos 30^{\circ}$	<b>A</b> 1		Correct expression
	150	A 1	2	Comment on second
	$v = \frac{150}{\cos 30^{\circ}} = 173 \text{ ms}^{-1} \text{ (to 3sf)}$	A1	3	Correct answer
	Total		5	
6(a)	$2.45 = \frac{1}{2} \times 9.8t^2$	M1		Equation for time to ground
	2.43 = 2 \times 3.61	A1		Correct equation
	$t = \sqrt{\frac{2.45}{4.9}} = 0.707$ seconds (to 3 sf)		2	1.00
	$1 - \sqrt{\frac{4.9}{4.9}} = 0.707$ Seconds (10.3.81)	A1	3	AG Correct time from correct working
(b)	$s = 20 \times 0.707 = 14.1 \text{ m (to 3sf)}$	M1	•	Using 20 × time from part (a)
(-)	0.707 .0.0 (.000	A1	2	Correct distance
(c)	$v_y = 0.707 \times 9.8 = 6.929$	M1 A1		Finding vertical component of velocity Correct vertical component
	. (6929)	dM1		Using tan to find the angle
	$\theta = \tan^{-1} \left( \frac{6.929}{20} \right) = 19.1^{\circ}$	A1	4	Correct angle
	Total	111	9	
7(a)	$\mathbf{u} = 5\mathbf{i}$	B1	1	Correct velocity
()				
(b)	$\mathbf{v} = 5\mathbf{i} + (-0.2\mathbf{i} + 0.25\mathbf{j})t$	M1		Use of constant acceleration equation with
				<b>u</b> and <b>a</b> not zero
		A1	2	Correct velocity
				Give M1A0 for using 5j
(c)	5 - 0.2t = 0	M1		Easterly component zero
		A1		Correct equation
	$t = \frac{5}{0.2} = 25 \text{ seconds}$	A1	3	•
	$t = \frac{1}{0.2} = 25$ seconds	AI	3	Correct t
(d)	$\mathbf{r} = 5\mathbf{i} \times 25 + \frac{1}{2}(-0.2\mathbf{i} + 0.25\mathbf{j}) \times 25^2$	M1		Use of constant acceleration equation
	2 0.21 + 0.23 j) × 23	A 1 E		with t from part (c)
		A1F		Correct expression based on <i>t</i> from part (c)
	= 62.5i + 78.125j	A1		Correct simplification CAO
	· ·	dM1		Using tan to find the angle
	$\theta = \tan^{-1} \left( \frac{62.5}{78.125} \right)$	A1F		Correct expression based on $t$ from part (c),
				with correct two values (either way)
	= 38.7°	A1	6	Correct angle CAO
	Total		12	
	TOTAL		60	