MEASUREMENTS AND ERRORS

- Accuracy A measure of the closeness of agreement between an individual result and the accepted value. An accurate result is in close agreement with the accepted value.
- *Error* The difference between an individual measurement and the true value (or accepted reference value) of the quantity being measured.
- *Precision* The closeness of agreement between independent measurements obtained under the same conditions. It depends only on the distribution of random errors (i.e. the spread of measurements) and does not relate to the true value.
- Uncertainty An estimate attached to a measurement which characterises the range of values within which the true value is said to lie. It is written, for example, as 44.0 ± 0.4 .

Reliability The opposite of uncertainty; **high uncertainty = not very reliable** measurement

Accuracy of measurements

Uncertainty is often taken to be **half a division on either side of the smallest unit on the scale**. However, the accuracy of measurements also depends on the quality of the apparatus used (e.g. Grade A or Grade B glassware.)

example If a 100 cm³ measuring cylinder is graduated in 1 cm³ divisions.

- Class A maximum error of half a division (0.5 cm³)
- Class B maximum error of a whole division (1 cm³)

Glassware

When glassware is manufactured there will always be a maximum error. This is usually marked on the glassware.

or

Temperature Volumetric equipment must not get warm because expansion of the glass will alter the volume; the temperature is marked on the apparatus.

In or out? Apparatus either... holds an accurate measure (IN) volumetric flask measuring cylinder





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- *Non-digital* burette, measuring cylinder
 - record all the figures that are known for certain
 - read to half a division
 - for a burette, record values to two decimal places ending in a 5 or a 0



Maximum errors

Burette	• (• •	graduated in divisions every 0.1 cm ³ maximum error is half a division i.e. \pm 0.05 cm ³ purettes are read twice, so the overall maximum error is	2 x 0.05 =	± 0.1 cm ³
Pipette	• ; •	a 25 cm ³ pipette has a maximum error of 0.06 cm ³ ike all volumetric equipment it must be used properly		
	Q.1	 Calculate the maximum error of a 50 cm³ measuring cylinder 10 cm³ measuring cylinder 	cm ³ cm ³	

Balances a two-decimal place balance may have a maximum error of 0.005 g



a three-decimal place balance may have a maximum error of 0.0005 g



The significance of the maximum error in a measurement depends upon how large a quantity is being measured. It is useful to quote this error as a **percentage error**.

Measurements	F323
Percentage Error	 based on two factors - maximum error value of measurement
	• percentage error = $\frac{\text{maximum error x 100\%}}{\text{value of measurement}}$
	 the smaller the value measured, the greater the percentage error
Volumetric flask (250 cm ³)	maximum error = 0.2 cm^3
	percentage error = $\frac{0.2 \text{ cm}^3 \text{ x } 100}{250 \text{ cm}^3}$ = 0.08%
Pipette (25 cm³)	maximum error = 0.06 cm^3
(,	percentage error = $\frac{0.06 \text{ cm}^3 \text{ x } 100}{25 \text{ cm}^3}$ = 0.24%
Burette	maximum error = 0.05 cm ³ per reading 0.10 cm ³ per titration (you read it twice)
	percentage error depends on the volume delivered (the smaller the volume, the bigger the % error)
	for a 25.00 cm ³ delivery = $\frac{0.10 \text{ cm}^3 \text{ x } 100}{25.00 \text{ cm}^3}$ = 0.40%
	for a 15.00 cm ³ delivery = $0.10 \text{ cm}^3 \times 100 = 0.67\%$ 15.00 cm ³
2-decimal place top-pan balance	e mass of beaker + solid = 32.56 g maximum error = 0.005 g mass of empty beaker = 32.16 g maximum error = 0.005 g mass of solid = 0.40 g maximum error = 0.01g
	percentage error = $\frac{0.01 \text{ g} \times 100}{0.40 \text{ g}}$ = 2.5%
3-decimal place top-pan balance	e maximum error over two readings will be 0.001 g (2 x 0.0005) using the above values, percentage error will be = 0.25%

Thermometers

• maximum error depends on the scale and how many degrees per division

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• maximum error when measuring a temperature change is one division

Temperature • the greater the temperature change, the lower the percentage error *change*



Significant

figures When quoting a result, it should contain the same number of significant figures as the measurement that has the smallest number of significant figures.

Rounding off	 if the last figure is 	between 5 and 9 inclusive	round up
	 if the last figure is 	between 0 and 4 inclusive	round down
•	should only be done at th	e end of a calculation	
•	should not be done after e	each step of a calculation (it c	auses rounding errors)

example	50.67 rounded to	3 sig figs	is	50.7
		2 sig figs	is	51
		1 sig figs	is	100

• for larger numbers, use standard form

example	371 rounded to	2 sig figs	is	3.7 x 10 ²
		3 sig figs	is	3.71 x 10 ²

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Scale

Recording volumes during titrations

Burette measurements should be recorded to 2 decimal places with the last figure either 0 or 5.

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During a titration, initial and final burette readings should be taken; the titre (actual volume delivered) is calculated by difference. Record titration results in a table as shown below.

	Approx	1	2	3
final volume / cm ³	26.00	26.75	30.85	24.60
initial volume / cm ³	1.00	2.30	6.00	0.25
titre / cm ³	25.00	24.45	24.85	24.35
tick if used to calculate mean		1		1

Mean titres • repeat the titrations until there are two concordant titres (within 0.10 cm³)

- take an average of the concordant titres
- if this is not possible, use the two titres that have the closest agreement

example the two concordant titres are the 1st and 3rd (within 0.1 cm³ of each other)
mean (average) titre value =
$$\frac{24.45 \text{ cm}^3 + 24.35 \text{ cm}^3}{2}$$
 = 25.40 cm³
overall maximum error = 2×0.05 = 0.10 cm³
overall percentage error = $\frac{0.10 \text{ cm}^3 \times 100}{25.40 \text{ cm}^3}$ = 0.39%

There is a case for arguing that the accumulated errors indicate that one decimal place is more appropriate but this should not be used. The maximum error is the worst-case scenario and it is likely that the actual titre will in reality be more accurate than one decimal place.

If concordant titres within 0.05 cm³ of one another are found there is a problem when calculating the mean titre. For example, a student may obtain three recorded titres of 24.45 cm³, 24.85 cm³ and 24.40 cm³.

mean titre value =
$$\frac{24.45 \text{ cm}^3 + 24.40 \text{ cm}^3}{2}$$
 = 24.425 cm³

This mean titre has a value that is more accurate than the burette can measure. The value of 24.425 cm³ should more correctly be 'rounded' to 24.43 cm³. It would seem very unfair not to credit a mean titre of 24.425 cm³ in this case, especially as the results showed a better concordancy.

In assessed A level practical tasks, the mean of two titres of **25.25 cm³** and **25.20 cm³** will be allowed as **25.2**, **25.20**, **25.25** or **25.225** cm³.

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Errors in

procedure The accuracy of a final result also depends on the procedure used.

For example, in an enthalpy experiment, the measurement of a temperature change may be precise but there may be large heat losses to the surroundings which affect the accuracy of overall result.

Anomalous

readings Where an experiment uses repeated measurements of the same quantity, (e.g. titrations) anomalous readings should be identified. If a titre is clearly outside the range of all other readings, it can be judged as being anomalous and should be ignored when the mean titre is calculated.

If a plotted graph reveals that a value is anomalous, then it too should be ignored.

Introducing rounding errors in multi-step calculations

Example When 6.074 g of a carbonate is reacted with 50.0 cm³ of 2.0 mol dm⁻³ HCl(aq) (which is an excess), a temperature rise of 5.5 °C is obtained. [The specific heat capacity of the solution is 4.18 J g⁻¹ K⁻¹]

Heat produced = $50.0 \times 4.18 \times 5.5 = 1149.5 \text{ J} = 1.1495 \text{ kJ}$ (by calculator)

Since the least certain measurement (the temperature rise) is only to 2 significant figures the answer should also be quoted to 2 significant figures.

Therefore, the heat produced should be quoted as 1.1 kJ

If this figure is to be used subsequently to calculate the enthalpy change per mole then a 'rounding' error will be produced. **The 1.1495 kJ value must be used.**

For example, if the carbonate has a molar mass of 84.3 g mol⁻¹, the enthalpy change per mole of carbonate can be calculated from the value above.

Using the calculator value of 1.1495 kJ for the heat produced enthalpy per mole = 15.95371255 kJ mol⁻¹ = 16 kJ mol⁻¹ (to 2 sig figs) Using the rounded value of 1.1 kJ for the heat produced, enthalpy per mole = 15.26671057 kJ mol⁻¹ = 15 kJ mol⁻¹ (to 2 sig figs)

Rounding to 2 sig figs too early produces a 'rounding error'.

References The Royal Society of Chemistry has produced several very helpful documents on measurements and errors; www.rsc.org/education/teachers/learnnet/pdf/learnnet/RSCmeasurements_teacher.pdf www.rsc.org/pdf/amc/brief13.pdf

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