



# General Certificate of Education

## Mathematics 6360

### *MS2A Statistics 2A*

# Mark Scheme

## *2006 examination - January series*

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

## Key To Mark Scheme And Abbreviations Used In Marking

M	mark is for method		
m or dM	mark is dependent on one or more M marks and is for method		
A	mark is dependent on M or m marks and is for accuracy		
B	mark is independent of M or m marks and is for method and accuracy		
E	mark is for explanation		
✓ or ft or F	follow through from previous incorrect result	MC	mis-copy
CAO	correct answer only	MR	mis-read
CSO	correct solution only	RA	required accuracy
AWFW	anything which falls within	FW	further work
AWRT	anything which rounds to	ISW	ignore subsequent work
ACF	any correct form	FIW	from incorrect work
AG	answer given	BOD	given benefit of doubt
SC	special case	WR	work replaced by candidate
OE	or equivalent	FB	formulae book
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme
-x EE	deduct x marks for each error	G	graph
NMS	no method shown	c	candidate
PI	possibly implied	sf	significant figure(s)
SCA	substantially correct approach	dp	decimal place(s)

### No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

**Otherwise we require evidence of a correct method for any marks to be awarded.**

## MS2A

Question	Solution	Marks	Total	Comments
1(a)(i)	$P(X \leq 1) = 0.9098$	M1 A1	2	AWRT 0.91
(ii)	$P(Y = 2) = \frac{e^{-2.5} (2.5)^2}{2!}$ $= 0.257$	M1 A1	2	AWFW 0.256 and 0.257
(b)(i)	$T = X + Y \sim P_o(3.0)$ $P(T = 2) = \frac{e^{-3.0} \times (3.0)^2}{2!}$ $= 0.224$ <b>OR</b> using tables: $= 0.4232 - 0.1991$ $= 0.224$	B1 M1 A1	3	P(Total of 2 breakdowns) = $P([x, y] = 2)$ $= P([2, 0] \text{ or } [0, 2] \text{ or } [1, 1])$ $= [0.0758 \times 0.0821] +$ $[0.6065 \times 0.25652] +$ $[0.20521 \times 0.3033]$ $= 0.006223 + 0.155585$ $+ 0.062233$ $= 0.224$
(ii)	$p = (0.224)^4 = 0.0025$	M1A1	2	
(c)(i)	$4X \sim P_o(2.0)$ $4Y \sim P_o(10.0) \Rightarrow \mu = 12.0$	B1	1	
(ii)	$P(T \geq 18) = 1 - P(T \leq 17)$ $= 1 - 0.9370$ $= 0.0630$	M1 A1	2	
<b>Total</b>			<b>12</b>	

## MS2A (cont)

Question	Solution	Marks	Total	Comments																		
<b>2(a)</b>	$H_0$ : Choice independent of gender	B1		gender not associated with choice																		
	<table border="0"> <tr> <td></td> <td>Squash</td> <td>Badminton</td> <td>Archery</td> <td>Hockey</td> <td></td> </tr> <tr> <td>Male</td> <td>5/3.5</td> <td>16/14</td> <td>30/24.5</td> <td>19/28</td> <td>M1</td> </tr> <tr> <td>Female</td> <td>4/5.5</td> <td>20/22</td> <td>33/38.5</td> <td>53/44</td> <td></td> </tr> </table>		Squash	Badminton	Archery	Hockey		Male	5/3.5	16/14	30/24.5	19/28	M1	Female	4/5.5	20/22	33/38.5	53/44				
		Squash	Badminton	Archery	Hockey																	
	Male	5/3.5	16/14	30/24.5	19/28	M1																
	Female	4/5.5	20/22	33/38.5	53/44																	
	Combine Squash and Badminton	M1		$E_i < 5$ (Similar categories)																		
	<table border="0"> <tr> <td></td> <td>S &amp; B</td> <td>Archery</td> <td>Hockey</td> <td></td> </tr> <tr> <td>Male</td> <td>21/17.5</td> <td>30/24.5</td> <td>19/28</td> <td>M1</td> </tr> <tr> <td>Female</td> <td>24/27.5</td> <td>33/38.5</td> <td>53/44</td> <td>M1</td> </tr> </table>		S & B	Archery	Hockey		Male	21/17.5	30/24.5	19/28	M1	Female	24/27.5	33/38.5	53/44	M1						
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	Male	21/17.5	30/24.5	19/28	M1																	
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$\chi^2$ values																						
<table border="0"> <tr> <td></td> <td>S &amp; B</td> <td>Archery</td> <td>Hockey</td> <td></td> </tr> <tr> <td>Male</td> <td>0.7000</td> <td>1.2347</td> <td>2.8928</td> <td>M1</td> </tr> <tr> <td>Female</td> <td>0.4455</td> <td>0.7857</td> <td>1.8409</td> <td></td> </tr> </table>		S & B	Archery	Hockey		Male	0.7000	1.2347	2.8928	M1	Female	0.4455	0.7857	1.8409								
	S & B	Archery	Hockey																			
Male	0.7000	1.2347	2.8928	M1																		
Female	0.4455	0.7857	1.8409																			
$\chi^2_{\text{calc}} = 7.90$		A1		(7.8 to 7.9)																		
$\nu = 2$		B1																				
$\chi^2_{5\%}(2) = 5.991$		B1ft		(on their $\nu$ )																		
Reject $H_0$ Sufficient evidence, at the 5% level of significance, to support an association between the choice of sport and gender		A1ft	10	reject $H_0$ and $H_0$ stated <b>or</b> statement in context																		
<b>(b) More females and fewer males chose to participate in hockey than expected</b>		B1 B1	2																			
<b>Total</b>			<b>12</b>																			
<b>3(a)</b>	$\bar{x} = 301.0$	B1																				
<b>(b)</b>	$S^2 = (4.945)^2 = 24.5$	B1	2	AWFW 24.4 to 24.5																		
	$\nu = 9$																					
	$t = 3.250$	B1B1																				
	99% confidence interval for $\mu$ $= 301.0 \pm 3.250 \times \left( \frac{4.945}{\sqrt{10}} \right)$ $= 301.0 \pm 5.08$ $= (295.9, 306.1)$	M1 A1 A1	5	$(\text{their } \bar{x}) \pm t \times \left( \frac{\text{their } \sigma}{\sqrt{10}} \right)$																		
<b>(c)</b>	Since 290 is less than the lower limit of the confidence interval, it is probably safe to assume that the mean weight of packets of rice exceeds 290 grams	E2	2																			
<b>Total</b>			<b>9</b>																			

## MS2A (cont)

Question	Solution	Marks	Total	Comments
4(a)(i)	$\text{Area} = k(b-a) = 1$ $\Rightarrow k = \frac{1}{b-a}$	E1	1	AG
(ii)	$E(X) = \int_a^b kx \, dx$ $= \left( \frac{kx^2}{2} \right)_a^b$ $= \frac{1}{2}k(b^2 - a^2)$ $= \frac{1}{2} \times \frac{1}{(b-a)} \times (b-a)(a+b)$ $= \frac{1}{2}(a+b)$	M1 A1 M1 A1	4	(factors shown) AG
(b)(i)	$\mu = 1$	B1	1	
(ii)	$\sigma^2 = \text{Var}(X) = \frac{1}{12}(b-a)^2$ $= \frac{1}{12} \times 6^2$ $= 3$ $\therefore \sigma = \sqrt{3}$	M1 A1	2	AWRT 1.73
(iii)	$P\left(X < \frac{2-\mu}{\sigma}\right) = P\left(X < \frac{1}{\sqrt{3}}\right)$ $= \frac{1}{6} \times 2.577$ $= 0.430$	M1ft M1ft A1	3	(on their $\mu$ and $\sigma$ )
	<b>Total</b>		<b>11</b>	

Question	Solution	Marks	Total	Comments
5(a)	$E(X) = \sum_{\text{all } x} x P(X = x)$ $= 50$ $E(X^2) = \sum_{\text{all } x} x^2 P(X = x)$ $= 2602.6(0)$ $\text{Var}(X) = E(X^2) - [E(X)]^2$ $= 2602.6 - 50^2$ $= 102.6(0)$ $\Rightarrow \text{standard deviation}(X) = 10.13$	B1 M1 M1 A1	4	CAO    (to nearest 1p)
(b)	$E(Y) = \mu = E(10X + 250)$ $= 10 \times E(X) + 250$ $= 750$ $\text{s.d}(Y) = 10 \times 10.1$ $= 101$	B1ft B1ft	2	On their $E(X)$  On their $\text{sd}(X)$
<b>Total</b>			<b>6</b>	
6	$H_0 : \mu = 1000$ $H_1 : \mu \neq 1000$ $\bar{x} = \frac{12036}{12} = 1003$ $S = 5.444$ $\nu = 12 - 1 = 11$ $t = \frac{\bar{x} - \mu}{\frac{S}{\sqrt{n}}} = \frac{1003 - 1000}{\frac{5.444}{\sqrt{12}}} = 1.91$ $t_{\text{crit}} = \pm 2.201$ <p>Accept <math>H_0</math> Insufficient evidence to indicate a change in the mean content of sherry in a bottle</p>	B1 B1 B1 B1 M1 A1ft A1 B1ft A1ft E1ft	10	2-tailed test  $S^2 = 29.6$  (on their $\nu$ ) (on their $t$ - values)
<b>Total</b>			<b>10</b>	
<b>TOTAL</b>			<b>60</b>	