

# Quadratic inequalities

The purpose of this part is to solve inequalities of the form

$$ax^2 + bx + c > 0 (\geq 0) \quad \text{or} \quad ax^2 + bx + c < 0 (\leq 0)$$

$$b^2 - 4ac > 0$$

$$f(x) = ax^2 + bx + c$$

$$f(x) = a(x - \alpha)(x - \beta)$$

$$b^2 - 4ac = 0$$

$$f(x) = ax^2 + bx + c$$

$$f(x) = a(x - \alpha)^2$$

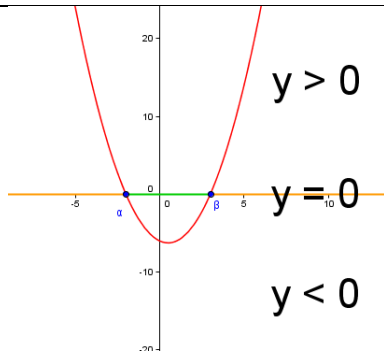
The parabola is TANGENT to the  $x$ -axis

$$b^2 - 4ac < 0$$

$$f(x) = ax^2 + bx + c$$

$f(x)$  can't be factorised

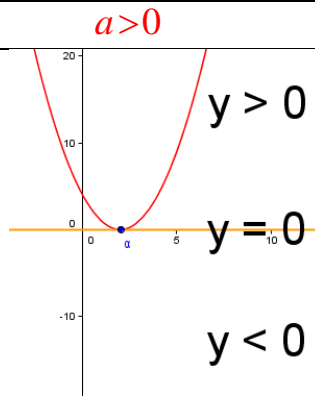
The parabola does not cross the  $x$ -axis.



$$ax^2 + bx + c > 0 \text{ for } x < \alpha \text{ or } x > \beta$$

$$ax^2 + bx + c < 0 \text{ for } \alpha < x < \beta$$

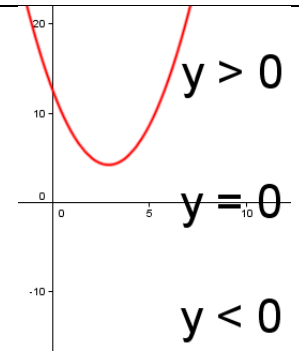
$$ax^2 + bx + c = 0 \text{ for } x = \alpha \text{ or } x = \beta$$



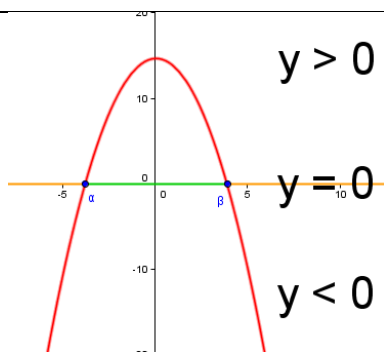
$$ax^2 + bx + c > 0 \text{ for } x < \alpha \text{ or } x > \alpha$$

$$ax^2 + bx + c < 0 \text{ has no solution}$$

$$ax^2 + bx + c = 0 \text{ for } x = \alpha$$



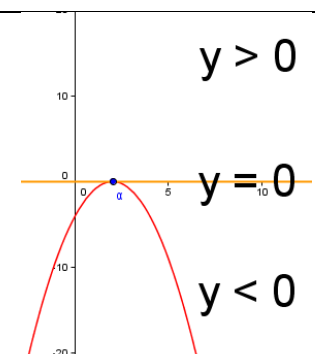
$$ax^2 + bx + c > 0 \text{ for all } x$$



$$ax^2 + bx + c > 0 \text{ for } \alpha < x < \beta$$

$$ax^2 + bx + c < 0 \text{ for } x < \alpha \text{ or } x > \beta$$

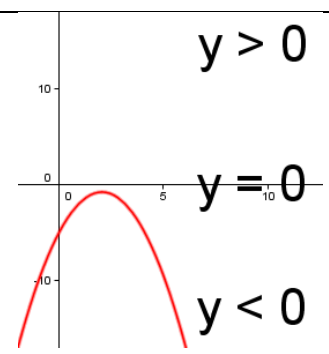
$$ax^2 + bx + c = 0 \text{ for } x = \alpha \text{ or } x = \beta$$



$$ax^2 + bx + c > 0 \text{ has no solution}$$

$$ax^2 + bx + c < 0 \text{ for } x < \alpha \text{ or } x > \alpha$$

$$ax^2 + bx + c = 0 \text{ for } x = \alpha$$



$$ax^2 + bx + c < 0 \text{ for all } x$$