

GCE Examinations
Advanced Subsidiary / Advanced Level
Decision Mathematics
Module D1

Paper D

MARKING GUIDE

This guide is intended to be as helpful as possible to teachers by providing concise solutions and indicating how marks should be awarded. There are obviously alternative methods that would also gain full marks.

Method marks (M) are awarded for knowing and using a method.

Accuracy marks (A) can only be awarded when a correct method has been used.

(B) marks are independent of method marks.



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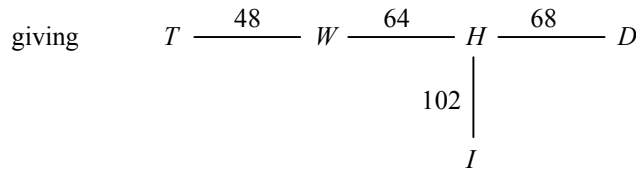
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D1 Paper D – Marking Guide

1. (a)

<i>order:</i>	4	3	5	1	2
	Durness	Helmsdale	Inverness	Thurso	Wick
Durness	–	(68)	123	81	92
Helmsdale	68	–	102	72	(64)
Inverness	123	(102)	–	148	127
Thurso	81	72	148	–	48
Wick	92	64	127	(48)	–



M3 A2

(b) 282 km

A1 (6)

2. (a) e.g. choose middle name, latter if middle pair
interrogate, giving answer or list of about half the previous list
repeat until celebrity found

B4

(b) with list of 1 name, need 1 interrogation
with list of 2 names, need a maximum of 2 interrogations
with list of 4 names, need a maximum of 3 interrogations etc.
with list of 2^n names, need a maximum of $(n + 1)$ interrogations
 $2^{20} = 1\,048\,576$ so with 1 million need a maximum of 21 interrogations.
(accept 20)

M2 A1 (7)

3. (a) if $y = 0$, lowest weight = 22 (SADT)
if y large, lowest weight = 27 (SBDT)
 \therefore lowest weight between 22 and 27 inclusive

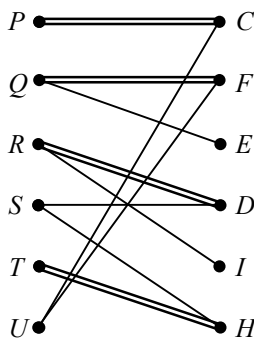
M2 A1

(b) if $y = 0$, minimum cut = 14, $\{S, A, B, C, E\} \mid \{D, T\}$
if y large, minimum cut = 22, $\{S, A, B, C, D, E\} \mid \{T\}$
maximum flow = minimum cut \therefore between 14 and 22 inclusive

M2 A1

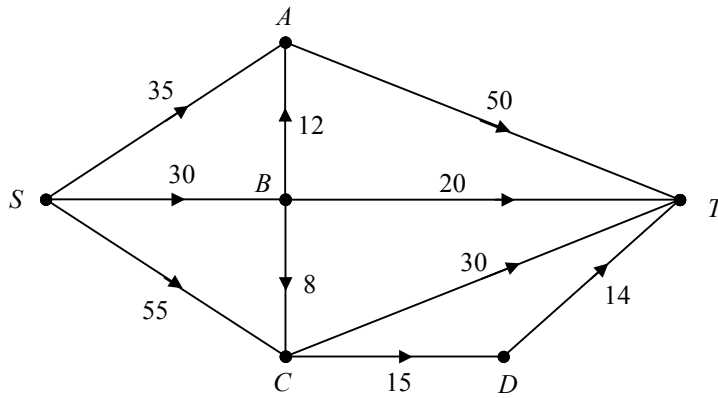
(c) (i) e.g. shortest route by road between 2 towns
(ii) e.g. maximum traffic flow between 2 towns

B1
B1 (8)

4. (a) 
- (b) initial matching shown by \equiv A1
- (c) search for alternating path giving e.g. $S - D = R - I$ (breakthrough) M1 A1
 change status giving $S = D - R = I$ M1
 search for alternating path giving e.g. $U - F = Q - E$ (breakthrough) M1 A1
 change status giving $U = F - Q = E$ M1
 complete matching e.g. $P - C, Q - E, R - I, S - D, T - H, U - F$ A1
- (d) P and U both now only interested in C which only one can have B2 (11)
-

5. (a) e.g. locate all odd vertices and identify all ways of pairing these
 for each way find total of minimum times between pairs
 choose lowest total
 minimum time is total of all arcs + lowest total found above B3
- (b) odd vertices are A, B, C and D B1
 minimum AB and $CD = 20 + 80 = 100$
 AC and $BD = 40 + 60 = 100$
 AD and $BC = 40 + 20 = 60$; lowest is 60 M1 A1
 total = sum of all arcs + 60 = 1460 + 60 = 1520 seconds A1
 route: e.g. $FGHIJKLDEAGIBCDEABCJLF$ A1
- (c) odd vertices now C and D , minimum $CD = 200$ M1 A1
 new total = 1440 + 200 = 1640 seconds B1 (11)
 removal of arc has increased total time as it provided a useful link
-

6. (a)



M2 A1

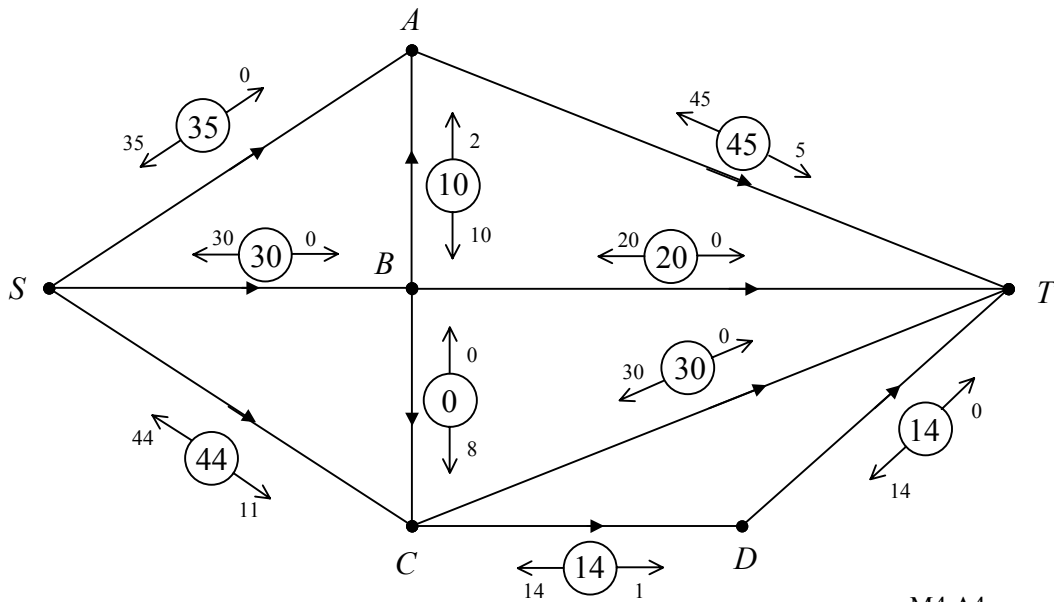
(b) $50 + 20 + 30 + 15 = 115$

A1

(c) minimum cut = $\{S, C, D\} \mid \{A, B, T\} = 109$

M1 A1

(d) e.g. start with $SAT = 35, SBT = 20, SCT = 30$
augment $SBAT$ by 10 and $SCDT$ by 14 giving maximum flow below



M4 A4

(e) this is maximum flow as it is equal to the minimum cut

B1

(f) e.g. maximum traffic flow between 2 points on a one-way system

B1

(16)

7. (a) maximise $R = 4x + 10y + 2z$ given
 $x - y \leq 5$
 $-y + 2z \leq 0$
 $2x + 4y + z \leq 40$
 $x \geq 0, y \geq 0, z \geq 0$

M2 A2

- (b) to change inequalities into equations

B1

- (c) only one positive value so pivot row is 3rd row

2nd tableau is:

Basic Var.	x	y	z	r	s	t	Value
r	$\frac{3}{2}$	0	$\frac{1}{4}$	1	0	$\frac{1}{4}$	15
s	$\frac{1}{2}$	0	$\frac{9}{4}$	0	1	$\frac{1}{4}$	10
y	$\frac{1}{2}$	1	$\frac{1}{4}$	0	0	$\frac{1}{4}$	10
R	1	0	$\frac{1}{2}$	0	0	$\frac{5}{2}$	100

M3 A3

- (d) final tableau as all values on the objective row are ≥ 0

B1

- (e) centre provides 10 courses for adults (not pensioners)
and gets £100 revenue per day

B2

- (f) no. e.g. the slack variable s associated with this constraint is not zero
so optimal solution without this constraint would be the same

B2

(16)

Total

(75)

