

Question Number	Scheme	Marks
1. (a)	$1 - 3x, + 9x^2, - 27x^3 + \dots$	B1, B1, B1 (3)
(b)	$(1+x)(1-3x+9x^2-27x^3\dots)$ $= 1 + (x-3x) + (9x^2-3x^2) + (19x^3-27x^3) \dots$ $= 1 - 2x + 6x^2 - 18x^3 *$	M1 A1 (2)
(c)	$x = .01$ $1 - 0.02 + 0.0006 - 0.000018, = 0.98058$	B1 M1, A1 cao (3) (8 marks)
2. (a)	Uses $\frac{A}{(2x-3)} + \frac{B}{(x+1)}$ Considers $-2x+13 = A(x+1) + B(2x-3)$ and substitutes $x = -1$ or $x = 1.5$, or compares coefficients and solves simultaneous equations To obtain $A = 4$ and $B = -3$.	M1 M1 A1, A1 (4)
(b)	Separates variables $\int \frac{1}{y} dy = \int \frac{4}{2x-3} - \frac{3}{x+1} dx$ $\ln y = 2 \ln(2x-3) - 3 \ln(x+1) + C$ Substitutes to give $\ln 4 = 2 \ln 1 - 3 \ln 3 + C$ and finds $C (\ln 108)$ $\ln y = \ln(2x-3)^2 - \ln(x+1)^3 (+\ln 108)$ $= \ln \frac{C(2x-3)^2}{(x+1)^3}$ $\therefore y = \frac{108(2x-3)^2}{(x+1)^3}$ Or $y = e^{2 \ln(2x-3) - 3 \ln(x+1) + \ln 108}$ special case M1 A2	M1 A1, B1 ft M1 M1 A1 A1 cso (7) (11 marks)

Question Number	Scheme	Marks												
3. (a)	<table border="1" style="display: inline-table; vertical-align: middle;"> <tr> <td>$x:$</td><td>0</td><td>0.5</td><td>1</td><td>1.5</td><td>2</td></tr> <tr> <td>$y:$</td><td>2</td><td>2.25</td><td>3</td><td>4.25</td><td>6</td></tr> </table> ≥ 2 correct ys	$x:$	0	0.5	1	1.5	2	$y:$	2	2.25	3	4.25	6	M1
$x:$	0	0.5	1	1.5	2									
$y:$	2	2.25	3	4.25	6									
	$R \approx \frac{1}{2} \times \frac{1}{2}, [2 + 2\{2.25 + 3 + 4.25\} + 6]$	B1, [M1 A1 ft]												
	$\frac{27}{4}$ or 6.75	A1 (5)												
(b)	Since curve bends under straight line \rightarrow overestimate	M1 (1)												
(c)	$V = \pi \int_0^2 y^2 dx = \pi \int_0^2 (x^4 + 4x^2 + 4) dx$ $= \pi \left[\frac{x^5}{5} + \frac{4}{3}x^3 + 4x \right]_0^2$ $= \pi \left[\left(\frac{32}{5} + \frac{32}{3} + 8 \right) - (0) \right]$ $= \frac{\pi}{15} [96 + 160 + 120] = \frac{376}{15} \pi \quad (\text{or } 25\frac{1}{15} \text{ or } 25.1\pi)$	$\pi \int y^2, y^2 = ()$ M1 M1 $x^n \rightarrow x^{n+1}$ M1 A1 Use of correct limits M1 A1 (6) (12 marks)												
4. (a)	$\frac{dV}{dt} = -kV$ $\int \frac{1}{V} dV = -k \int dt, \ln V = -kt$ $\ln V = -kt + C \quad V = Ae^{-kt} \quad *$	B1 M1 A1 (3)												
(b)	$t = 0, V = 20000: \quad 20000 = A$ $t = 3, V = 11000: \quad 11000 = Ae^{-3k}$ $e^{-3k} = 0.55$ $-3k = \ln 0.55$ $k \approx 0.199(3) \quad (\text{allow } 0.2)$	B1 M1, A1												
	$t = 10 \quad V = 20000e^{-10k}; \quad = £2700$	M1; A1 (5)												
(c)	$500 = 20000e^{-kt} \quad e^{-kt} = 0.025$ $-0.199t = \ln 0.025$ $t \approx 18.5 \quad (18.44) \text{ accept } 18 \text{ or } 19 \text{ yrs}$	M1 A1 A1 A1 (3) (11 marks)												

Question Number	Scheme	Marks
5. (a)	$\frac{8}{x} - x^2 = 0 \Rightarrow x^3 = 8 \Rightarrow x = 2$	M1 A1 (2)
(b)	$\left(\frac{8}{x} - x^2 \right) = x^4 - 16x + \frac{64}{x^2}$ M1 3(or 4) terms $\int (x^4 - 16x + 64x^{-2}) dx = \frac{x^5}{5} - 8x^2 - \frac{64}{x}$ $\left[\frac{x^5}{5} - 8x^2 - \frac{64}{x} \right]_1^2 = \left(\frac{32}{5} - 32 - 32 \right) - \left(\frac{1}{5} - 8 \right) - 64$	M1 A1 M1 A1 ft
	Volume is $\frac{71}{5}\pi$ (units ³)	A1 (7) (9 marks)
6. (a)	$\mathbf{r} = \mathbf{i} + 2\mathbf{j} - 3\mathbf{k} \pm \lambda(4\mathbf{i} - 5\mathbf{j} + 3\mathbf{k})$ or $\mathbf{r} = 5\mathbf{i} - 3\mathbf{j} \pm \lambda(4\mathbf{i} - 5\mathbf{j} + 3\mathbf{k})$ (or any equivalent vector equation)	M1A1 (2)
(b)	Show that $\mu = -3$	B1 (1)
(c)	Using $\cos \theta = \frac{(4\mathbf{i} - 5\mathbf{j} + 3\mathbf{k}) \cdot (\mathbf{i} - 2\mathbf{j} + 2\mathbf{k})}{\sqrt{(4^2 + 5^2 + 3^2)} \sqrt{(1^2 + 2^2 + 2^2)}}$ $= \frac{20}{15\sqrt{2}} = \frac{4}{3\sqrt{2}}$ (ft on $4\mathbf{i} - 5\mathbf{j} + 3\mathbf{k}$) num, denom.	M1 A1 ft A1 ft
	$\theta = 19.5^\circ$ (allow 19 or 20 if no wrong working is seen)	A1 (4)
(d)	Shortest distance = $AC \sin \theta$	M1
	$AC = \sqrt{((a-1)^2 + 2^2 + (b+3)^2)}$ (= 3)	M1A1
	Shortest distance = 1 unit	A1 (4) (11 marks)

Question Number	Scheme	Marks
7. (a)	$\begin{aligned}y^2 &= 81 \sin^2 2t \\&= 81 \times 4 \sin^2 t \cos^2 t \\&= 4 \times 9(1 - \cos^2 t) \times 9 \cos^2 t \\&= 4(9 - x^2) x^2\end{aligned}$	M1 M1 M1 A1 (4)
(b)	$\begin{aligned}\int y \, dx &= - \int_{\frac{\pi}{2}}^0 9 \sin 2t \, 3 \sin t \, dt \\&= \int_0^{\frac{\pi}{2}} 27 \sin 2t \sin t \, dt\end{aligned}$	M1, A1 B1 (3)
(c)	$\begin{aligned}27 \int_0^{\frac{\pi}{2}} \sin 2t \sin t \, dt &= 27 \int 2 \sin^2 t \cos t \, dt \\&= 27 \left[\frac{2}{3} \sin^3 t \right]_0^{\frac{\pi}{2}}, = 18\end{aligned}$	M1 M1 A1, A1 (4)
(d)	$\begin{aligned}\text{Rectangular area} &= 18 \times 6 = 108 \\ \text{Red area} &= \text{Rectangular} - 4 \times \text{Blue} = 108 - 72 = 36\end{aligned}$	M1 A1 M1 A1 (4) (15 marks)