

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

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## Pearson Edexcel International Advanced Level

Time 1 hour 30 minutes

Paper  
reference

**WMA14/01**

### Mathematics

International Advanced Level

Pure Mathematics P4

**You must have:**

Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 11 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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2. (a) Express  $\frac{3x}{(2x-1)(x-2)}$  in partial fraction form.

(3)

(b) Hence show that

$$\int_5^{25} \frac{3x}{(2x-1)(x-2)} dx = \ln k$$

where  $k$  is a fully simplified fraction to be found.

*(Solutions relying entirely on calculator technology are not acceptable.)*

(4)

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5. In this question you must show all stages of your working.  
Solutions relying entirely on calculator technology are not acceptable.

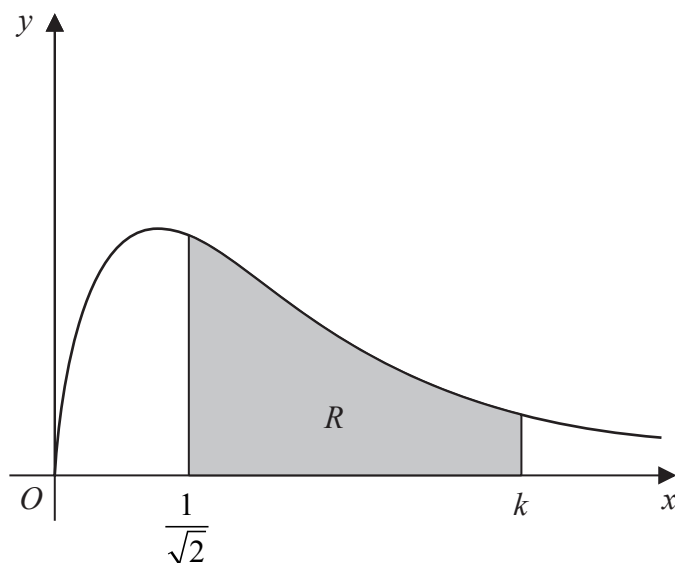


Figure 2

Figure 2 shows a sketch of part of the curve with equation

$$y = \frac{12\sqrt{x}}{(2x^2 + 3)^{1.5}}$$

The region  $R$ , shown shaded in Figure 2, is bounded by the curve, the line with equation  $x = \frac{1}{\sqrt{2}}$ , the  $x$ -axis and the line with equation  $x = k$ .

This region is rotated through  $360^\circ$  about the  $x$ -axis to form a solid of revolution.

Given that the volume of this solid is  $\frac{713}{648}\pi$ , use algebraic integration to find the exact value of the constant  $k$ .

(6)

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6.

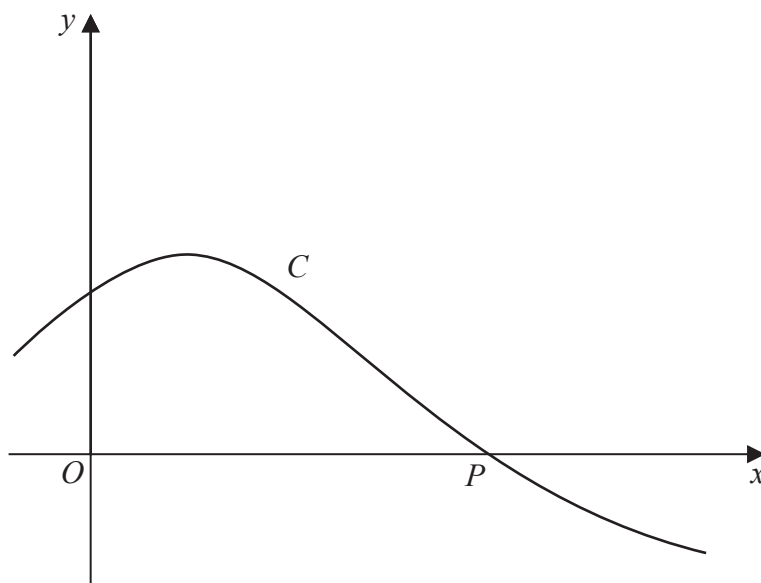


Figure 3

Figure 3 shows a sketch of the curve  $C$  with parametric equations

$$x = 1 + 3 \tan t \quad y = 2 \cos 2t \quad -\frac{\pi}{6} \leq t \leq \frac{\pi}{3}$$

The curve crosses the  $x$ -axis at point  $P$ , as shown in Figure 3.

- (a) Find the equation of the tangent to  $C$  at  $P$ , writing your answer in the form  $y = mx + c$ , where  $m$  and  $c$  are constants to be found.

(5)

The curve  $C$  has equation  $y = f(x)$ , where  $f$  is a function with domain  $[k, 1 + 3\sqrt{3}]$

- (b) Find the exact value of the constant  $k$ .

(1)

- (c) Find the range of  $f$ .

(2)

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8. A student was asked to prove by contradiction that

“there are no positive integers  $x$  and  $y$  such that  $3x^2 + 2xy - y^2 = 25$ ”

The start of the student’s proof is shown in the box below.

Assume that integers  $x$  and  $y$  exist such that  $3x^2 + 2xy - y^2 = 25$

$$\Rightarrow (3x - y)(x + y) = 25$$

If  $(3x - y) = 1$  and  $(x + y) = 25$

$$\left. \begin{array}{l} 3x - y = 1 \\ x + y = 25 \end{array} \right\} \Rightarrow 4x = 26 \Rightarrow x = 6.5, y = 18.5 \quad \text{Not integers}$$

Show the calculations and statements that are needed to complete the proof.

(4)





9. With respect to a fixed origin  $O$ , the equations of lines  $l_1$  and  $l_2$  are given by

$$l_1: \mathbf{r} = \begin{pmatrix} 2 \\ 8 \\ 10 \end{pmatrix} + \lambda \begin{pmatrix} -1 \\ 2 \\ 3 \end{pmatrix}$$

$$l_2: \mathbf{r} = \begin{pmatrix} -4 \\ -1 \\ 2 \end{pmatrix} + \mu \begin{pmatrix} 5 \\ 4 \\ 8 \end{pmatrix}$$

where  $\lambda$  and  $\mu$  are scalar parameters.

Prove that lines  $l_1$  and  $l_2$  are skew.

(5)









Question 10 continued

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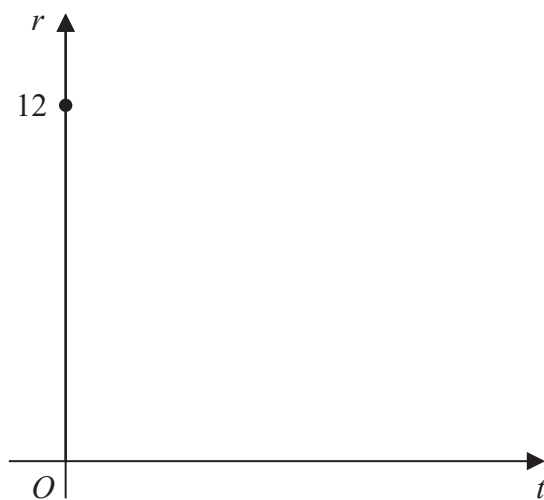


Diagram 1











