

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

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## Pearson Edexcel International Advanced Level

Time 1 hour 30 minutes

Paper  
reference

**WMA13/01**

### Mathematics

International Advanced Level

Pure Mathematics P3

**You must have:**

Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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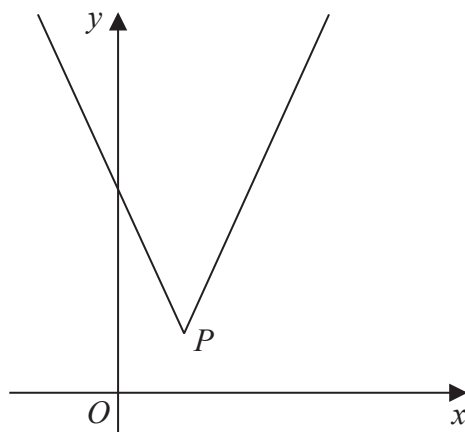


Figure 1

Figure 1 shows a sketch of part of the graph with equation  $y = f(x)$ , where

$$f(x) = |3x - 13| + 5 \quad x \in \mathbb{R}$$

The vertex of the graph is at point  $P$ , as shown in Figure 1.

(a) State the coordinates of  $P$ . (2)

(b) (i) State the range of  $f$ .  
 (ii) Find the value of  $ff(4)$  (2)

(c) Solve, using algebra and showing your working,  

$$16 - 2x > |3x - 13| + 5$$
 (4)

The graph with equation  $y = f(x)$  is transformed onto the graph with equation  $y = af(x + b)$

The vertex of the graph with equation  $y = af(x + b)$  is  $(4, 20)$

Given that  $a$  and  $b$  are constants,

(d) find the value of  $a$  and the value of  $b$ . (2)

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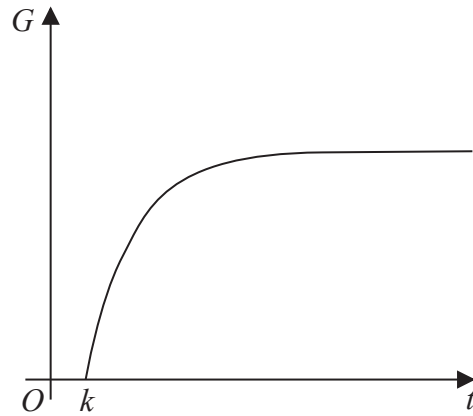


Figure 2

The total mass of gold,  $G$  tonnes, extracted from a mine is modelled by the equation

$$G = 40 - 30e^{1-0.05t} \quad t \geq k \quad G \geq 0$$

where  $t$  is the number of years after 1st January 1800.

Figure 2 shows a sketch of  $G$  against  $t$ .

**Use the equation of the model to answer parts (a), (b) and (c).**

- (a) (i) Find the value of  $k$ .  
 (ii) Hence find the year and month in which gold started being extracted from the mine. (3)

- (b) Find the total mass of gold extracted from the mine up to 1st January 1870. (2)

There is a limit to the mass of gold that can be extracted from the mine.

- (c) State the value of this limit. (1)

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Question 3 continued

Lined writing area for the answer to Question 3.

(Total 6 marks)

Q3

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### Question 4 continued

Lined writing area for the answer to Question 4 continued.

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**Question 4 continued**

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Lined area for writing the answer to Question 4.

**(Total 7 marks)**

Q4



P 6 9 2 0 4 A 0 1 5 3 2

5. (i) Find, by algebraic integration, the exact value of

$$\int_2^4 \frac{8}{(2x - 3)^3} dx \quad (4)$$

(ii) Find, in simplest form,

$$\int x(x^2 + 3)^7 dx \quad (2)$$

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Question 5 continued

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Q5

(Total 6 marks)



P 6 9 2 0 4 A 0 1 7 3 2

6. (i) The curve  $C_1$  has equation

$$y = 3 \ln(x^2 - 5) - 4x^2 + 15 \quad x > \sqrt{5}$$

Show that  $C_1$  has a stationary point at  $x = \frac{\sqrt{p}}{2}$  where  $p$  is a constant to be found. (4)

(ii) A different curve  $C_2$  has equation

$$y = 4x - 12 \sin^2 x$$

(a) Show that, for this curve,

$$\frac{dy}{dx} = A + B \sin 2x$$

where  $A$  and  $B$  are constants to be found.

(b) Hence, state the maximum gradient of this curve. (4)

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8. A curve  $C$  has equation  $y = f(x)$ , where

$$f(x) = \arcsin\left(\frac{1}{2}x\right) \quad -2 \leq x \leq 2 \quad -\frac{\pi}{2} \leq y \leq \frac{\pi}{2}$$

(a) Sketch  $C$ .

(1)

(b) Given  $x = 2 \sin y$ , show that

$$\frac{dy}{dx} = \frac{1}{\sqrt{A - x^2}}$$

where  $A$  is a constant to be found.

(3)

The point  $P$  lies on  $C$  and has  $y$  coordinate  $\frac{\pi}{4}$

(c) Find the equation of the tangent to  $C$  at  $P$ . Write your answer in the form  $y = mx + c$ , where  $m$  and  $c$  are constants to be found.

(3)

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**Question 8 continued**

Lined area for writing the answer to Question 8.

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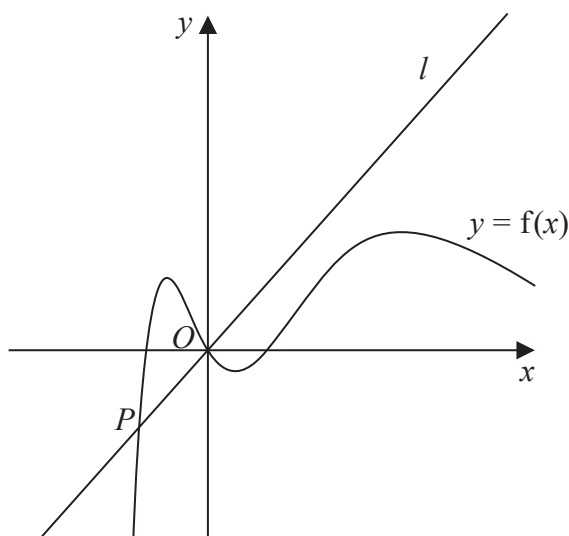


Figure 3

Figure 3 shows a sketch of part of the curve with equation  $y = f(x)$ , where

$$f(x) = x(x^2 - 4)e^{-\frac{1}{2}x}$$

(a) Find  $f'(x)$ .

(2)

The line  $l$  is the normal to the curve at  $O$  and meets the curve again at the point  $P$ .

The point  $P$  lies in the 3rd quadrant, as shown in Figure 3.

(b) Show that the  $x$  coordinate of  $P$  is a solution of the equation

$$x = -\frac{1}{2}\sqrt{16 + e^{\frac{1}{2}x}}$$

(4)

(c) Using the iterative formula

$$x_{n+1} = -\frac{1}{2}\sqrt{16 + e^{\frac{1}{2}x_n}} \quad \text{with } x_1 = -2$$

find, to 4 decimal places,

(i) the value of  $x_2$

(ii) the  $x$  coordinate of  $P$ .

(3)

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