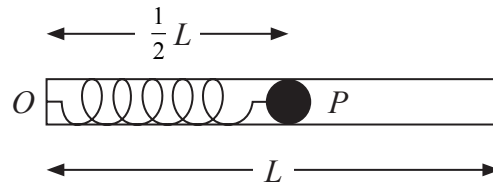




1.



**Figure 1**

A light elastic spring, of natural length  $L$  and modulus of elasticity  $\lambda$ , has a particle  $P$  of mass  $m$  attached to one end. The other end of the spring is fixed to a point  $O$  on the closed end of a fixed smooth hollow tube of length  $L$ .

The tube is placed horizontally and  $P$  is held inside the tube with  $OP = \frac{1}{2}L$ , as shown in Figure 1. The particle  $P$  is released and passes through the open end of the tube with speed  $\sqrt{2gL}$ .

(a) Show that  $\lambda = 8mg$ . (4)

The tube is now fixed vertically and  $P$  is held inside the tube with  $OP = \frac{1}{2}L$  and  $P$  above  $O$ . The particle  $P$  is released and passes through the open top of the tube with speed  $u$ .

(b) Find  $u$ . (5)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---









Leave  
blank

**Question 2 continued**

Blank writing area for Question 2 continued, consisting of 30 horizontal lines.

**(Total 11 marks)**

Q2

Grading box with two empty cells.



3.

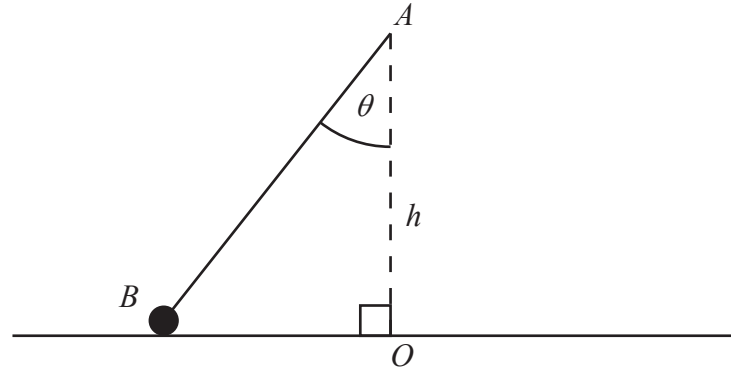


Figure 2

Figure 2 shows a particle  $B$ , of mass  $m$ , attached to one end of a light elastic string. The other end of the string is attached to a fixed point  $A$ , at a distance  $h$  vertically above a smooth horizontal table. The particle moves on the table in a horizontal circle with centre  $O$ , where  $O$  is vertically below  $A$ . The string makes a constant angle  $\theta$  with the downward vertical and  $B$  moves with constant angular speed  $\omega$  about  $OA$ .

(a) Show that  $\omega^2 \leq \frac{g}{h}$ . (8)

The elastic string has natural length  $h$  and modulus of elasticity  $2mg$ .

Given that  $\tan\theta = \frac{3}{4}$ ,

(b) find  $\omega$  in terms of  $g$  and  $h$ . (5)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---





**Question 3 continued**

Lined area for writing the answer to Question 3. The area contains 35 horizontal lines for writing.

Leave blank





**Question 3 continued**

Ruled area for handwritten answers, consisting of approximately 30 horizontal lines.

Leave blank





**Question 3 continued**

Leave  
blank

Lined area for writing the answer to Question 3.

**(Total 13 marks)**

**Q3**

--	--

11

**Turn over**



4.

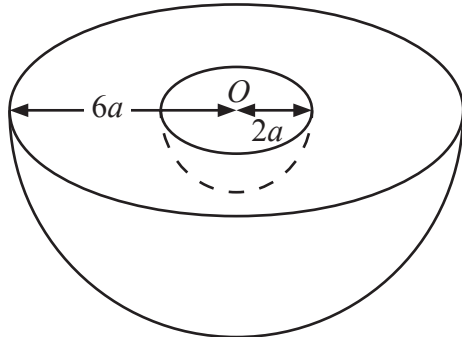


Figure 3

A uniform solid hemisphere, of radius  $6a$  and centre  $O$ , has a solid hemisphere of radius  $2a$ , and centre  $O$ , removed to form a bowl  $B$  as shown in Figure 3.

- (a) Show that the centre of mass of  $B$  is  $\frac{30}{13}a$  from  $O$ . (5)

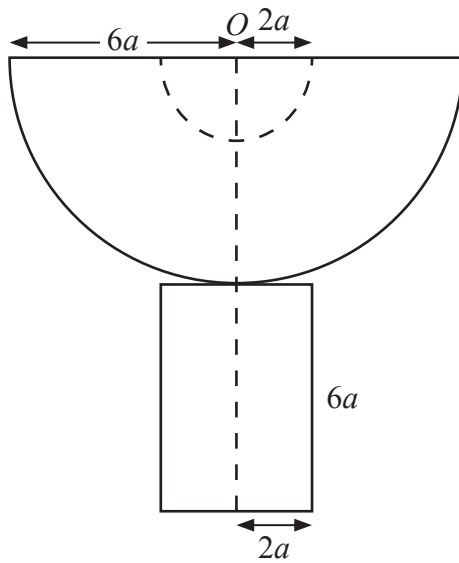


Figure 4

The bowl  $B$  is fixed to a plane face of a uniform solid cylinder made from the same material as  $B$ . The cylinder has radius  $2a$  and height  $6a$  and the combined solid  $S$  has an axis of symmetry which passes through  $O$ , as shown in Figure 4.

- (b) Show that the centre of mass of  $S$  is  $\frac{201}{61}a$  from  $O$ . (4)

The plane surface of the cylindrical base of  $S$  is placed on a rough plane inclined at  $12^\circ$  to the horizontal. The plane is sufficiently rough to prevent slipping.

- (c) Determine whether or not  $S$  will topple. (4)









5. A particle  $P$  of mass  $m$  is attached to one end of a light inextensible string of length  $a$ . The other end of the string is attached to a fixed point  $O$ . The particle is released from rest with the string taut and  $OP$  horizontal.

- (a) Find the tension in the string when  $OP$  makes an angle of  $60^\circ$  with the downward vertical. (6)

A particle  $Q$  of mass  $3m$  is at rest at a distance  $a$  vertically below  $O$ . When  $P$  strikes  $Q$  the particles join together and the combined particle of mass  $4m$  starts to move in a vertical circle with initial speed  $u$ .

- (b) Show that  $u = \sqrt{\left(\frac{ga}{8}\right)}$ . (3)

The combined particle comes to instantaneous rest at  $A$ .

- (c) Find
- (i) the angle that the string makes with the downward vertical when the combined particle is at  $A$ ,
- (ii) the tension in the string when the combined particle is at  $A$ . (6)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---



















