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Surname

Other names

Pearson
Edexcel GCE

Centre Number

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Candidate Number

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Mechanics M4

Advanced/Advanced Subsidiary

Wednesday 15 June 2016 – Morning
Time: 1 hour 30 minutes

Paper Reference

6680/01

You must have:

Mathematical Formulae and Statistical Tables (Pink)

Total Marks

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Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Whenever a numerical value of g is required, take $g = 9.8 \text{ m s}^{-2}$, and give your answer to either two significant figures or three significant figures.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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1.

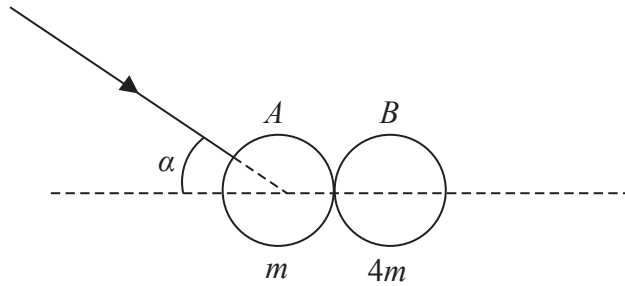


Figure 1

A smooth uniform sphere A of mass m is moving on a smooth horizontal plane when it collides with a second smooth uniform sphere B , which is at rest on the plane. The sphere B has mass $4m$ and the same radius as A . Immediately before the collision the direction of motion of A makes an angle α with the line of centres of the spheres, as shown in Figure 1. The direction of motion of A is turned through an angle of 90° by the collision and the coefficient of restitution between the spheres is $\frac{1}{2}$

Find the value of $\tan \alpha$.

(8)



Question 2 continued

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Q2

(Total 9 marks)



3. Two straight horizontal roads cross at right angles at the point X . A girl is running, with constant speed 5 m s^{-1} , due north towards X on one road. A car is travelling, with constant speed 20 m s^{-1} , due west towards X on the other road.

(a) Find the magnitude and direction of the velocity of the car relative to the girl, giving the direction as a bearing. (6)

At noon the girl is 150 m south of X and the car is 800 m east of X .

(b) Find the shortest distance between the car and the girl during the subsequent motion. (7)



4. A particle P of mass 9 kg moves along the horizontal positive x -axis under the action of a force directed towards the origin. At time t seconds, the displacement of P from O is x metres, P is moving with speed v m s $^{-1}$ and the force has magnitude $16x$ newtons. The particle P is also subject to a resistive force of magnitude $24v$ newtons.

- (a) Show that the equation of motion of P is

$$9 \frac{d^2x}{dt^2} + 24 \frac{dx}{dt} + 16x = 0 \quad (4)$$

It is given that the general solution of this differential equation is

$$x = e^{-\frac{4}{3}t} (At + B)$$

where A and B are arbitrary constants.

When $t = \frac{3}{4}$, P is travelling towards O with its maximum speed of $8e^{-1}$ m s $^{-1}$ and $x = d$.

- (b) Find the value of d . (3)

- (c) Find the value of x when $t = 0$ (5)



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Question 4 continued

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Q4

(Total 12 marks)



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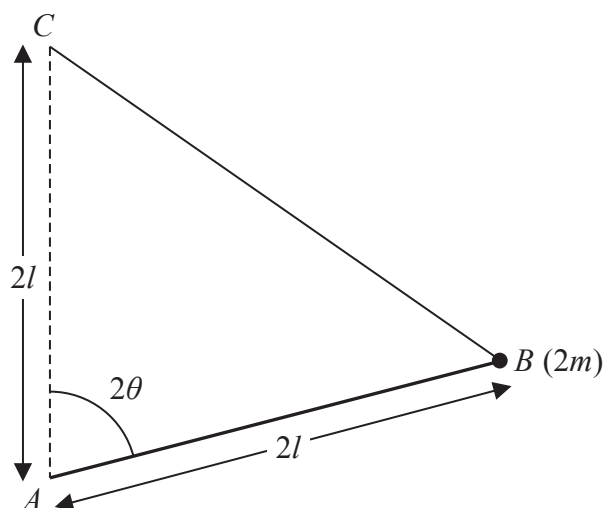


Figure 3

Figure 3 shows a uniform rod AB , of length $2l$ and mass $4m$. A particle of mass $2m$ is attached to the rod at B . The rod can turn freely in a vertical plane about a fixed smooth horizontal axis through A . One end of a light elastic spring, of natural length $2l$ and modulus of elasticity kmg , where $k > 4$, is attached to the rod at B . The other end of the spring is attached to a fixed point C which is vertically above A , where $AC = 2l$. The angle BAC is 2θ , where $\frac{\pi}{6} < \theta \leq \frac{\pi}{2}$

(a) Show that the potential energy of the system is

$$4mgl\{(k - 4)\sin^2 \theta - k \sin \theta\} + \text{constant} \quad (6)$$

Given that there is a position of equilibrium with $\theta \neq \frac{\pi}{2}$

(b) show that $k > 8$ (6)

Given that $k = 10$

(c) determine the stability of this position of equilibrium. (4)

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Question 6 continued

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Question 6 continued

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