

4. Show, using integration, that the moment of inertia of a uniform solid right circular cone of mass M , height h and base radius a , about an axis through the vertex, parallel to the base, is

$$\frac{3M}{20}(a^2 + 4h^2)$$

[You may assume without proof that the moment of inertia of a uniform circular disc, of radius r and mass m , about a diameter is $\frac{1}{4}mr^2$.]

(13)



5.

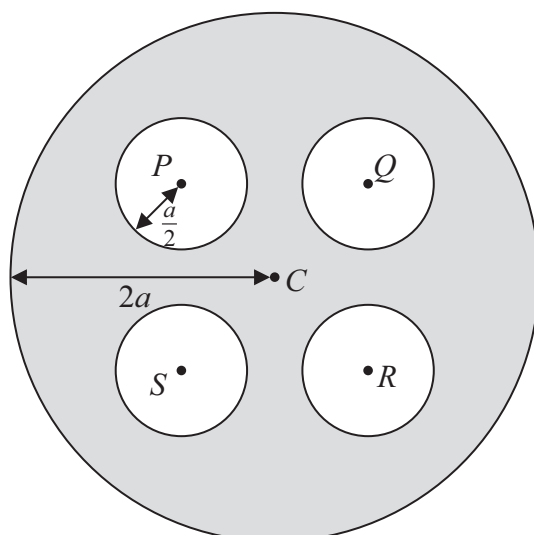


Figure 1

A uniform circular lamina has radius $2a$ and centre C . The points P , Q , R and S on the lamina are the vertices of a square with centre C and $CP = a$. Four circular discs, each of radius $\frac{a}{2}$, with centres P , Q , R and S , are removed from the lamina. The remaining lamina forms a template T , as shown in Figure 1.

The radius of gyration of T about an axis through C , perpendicular to T , is k .

(a) Show that $k^2 = \frac{55a^2}{24}$ (7)

The template T is free to rotate in a vertical plane about a fixed smooth horizontal axis which is perpendicular to T and passes through a point on its outer rim.

(b) Write down an equation of rotational motion for T and deduce that the period of small oscillations of T about its stable equilibrium position is

$$2\pi\sqrt{\left(\frac{151a}{48g}\right)}$$
(8)



Question 5 continued

Lined writing area for question 5.



6. A uniform circular disc, of radius r and mass m , is free to rotate in a vertical plane about a fixed smooth horizontal axis L which is perpendicular to the plane of the disc and passes through a point which is $\frac{1}{4}r$ from the centre of the disc. The disc is held at rest with its centre vertically above the axis. The disc is then slightly disturbed from its rest position.

You may assume without proof that the moment of inertia of the disc about L is $\frac{9mr^2}{16}$.

(a) Show that the angular speed of the disc when it has turned through $\frac{\pi}{2}$ is $\sqrt{\left(\frac{8g}{9r}\right)}$. (4)

(b) Find the magnitude of the force exerted on the disc by the axis when the disc has turned through $\frac{\pi}{2}$. (11)



Question 6 continued

A series of horizontal lines for writing the answer to Question 6.

Q6

(Total 15 marks)

TOTAL FOR PAPER: 75 MARKS

END

