

# Mark Scheme (Results)

June 2011

GCE Statistics S4 (6686) Paper 1

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## EDEXCEL GCE MATHEMATICS

### General Instructions for Marking

1. The total number of marks for the paper is 75.
2. The Edexcel Mathematics mark schemes use the following types of marks:
  - **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
  - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
  - **B** marks are unconditional accuracy marks (independent of M marks)
  - Marks should not be subdivided.

### 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod – benefit of doubt
- ft – follow through
- the symbol  $\checkmark$  will be used for correct ft
- cao – correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw – ignore subsequent working
- awrt – answers which round to
- SC: special case
- oe – or equivalent (and appropriate)
- dep – dependent
- indep – independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- $\square$  The second mark is dependent on gaining the first mark

**June 2011  
 Statistics S4 6686  
 Mark Scheme**

Question Number	Scheme	Marks
1.	$P(F_{8,10} > 3.07) = 0.05$ So need $P(F_{10,8} > x) = 0.01$ so $x = 5.81$ So $a = \frac{1}{5.81} = \underline{\mathbf{0.172}}$ awrt_0.172	B1 B1 <p style="text-align: right;"><b>2</b></p>
2.	$s_p^2 = \frac{6s_x^2 + 3s_y^2}{9}$ (= 192.03...) $1.735 < \frac{9s_p^2}{\sigma^2} < 23.589$ So 99% confidence interval is (73.26..., 996.14....)                      awrt ( <b><u>73.3,</u></b> <b><u>996)</u></b>	M1 B1M1B1 A1 <p style="text-align: right;"><b>5</b></p>
<b>Notes:</b>	1 <sup>st</sup> M1    for attempting $s_p^2$ 1 <sup>st</sup> B1    for 1.735 (or better) 2 <sup>nd</sup> M1    for use of $\frac{9s_p^2}{\sigma^2}$ , follow through their $s_p^2$ 2 <sup>nd</sup> B1    for 23.589 (or better) A1        for both values correct to awrt 3 sf	

Question Number	Scheme	Marks
3.	<p> <math>d = B - A : 1, 2, 3, -1, 3, -1, -2, 2</math>  <math>\bar{d} = 0.875</math>  <math>s_d^2 = \frac{33 - 8 \times 0.875^2}{7} = (3.8392\dots)</math>  <math>H_0 : \mu_d = 0 \quad H_1 : \mu_d &gt; 0</math>  <math>t_7 = \frac{0.875}{\frac{s_p}{\sqrt{8}}} = 1.263\dots</math> awrt <b>1.26</b>  <math>t_7(10\%)</math> one tail critical value is <b>1.415</b>             Not significant.            There is insufficient evidence to support the claim of manufacturer <i>B</i> or machine <i>B</i> does not produce more juice (than machine <i>A</i>)             1<sup>st</sup> M1 for attempting the <i>ds</i>            2<sup>nd</sup> M1 for attempting <math>\bar{d}</math>            3<sup>rd</sup> M1 for attempting <math>s_d</math> or <math>s_d^2</math>            4<sup>th</sup> M1 for attempting the correct test statistic            3<sup>rd</sup> A1 contextual statement only required.            Allow The juice provided by machine <i>A</i> is the same as by machine <i>B</i>   <b>NB</b> 2 sample test can score 3/8            M0 M0            M1 <math>\frac{7 \times 9.27 + 7 \times 16.79}{14}</math>            B1 for <math>H_0 : \mu_A = \mu_B \quad H_1 : \mu_A &lt; \mu_B</math>            M0 A0            B1 1.345            A0         </p>	<p>           M1            M1            M1             B1             M1A1             B1             A1   <b>8</b> </p>

Question Number	Scheme	Marks
<b>4.</b> (a)	$[X = \text{no. of incorrectly addressed letters. } X \sim B(40, 0.05)]$ $P(X > 3) = 1 - P(X \leq 3), = 1 - 0.8619 = 0.1381$ <b>awrt <u>0.138</u></b>	M1, A1  (2)
(b)	$P(\text{Type II Error}) = P(X \leq 3   p = 0.10)$ $= 0.4231$ <b>awrt</b>  <b><u>0.423</u></b>	M1 A1  (2)
(c)	Power = 1 - P(Type II error) so $s = \mathbf{0.58}$ (0.5769)	B1  (1)
(d)	$Y = \text{no. of incorrectly addressed letters in a sample of 15. } Y \sim B(15, 0.05)$ Size = $P(Y \geq 2) + P(Y = 1) \times P(Y \geq 2)$ $= [1 - 0.8290] \times [1 + 0.8290 - 0.4633]$ $= 0.23353\dots$ <b>awrt</b>  <b><u>0.23</u></b>	M1 A1 A1  (3)
(e)	(use overlay)	B1B1  (2)
(f)	2 <sup>nd</sup> / consultants test is quicker (since it uses fewer letters) 2 <sup>nd</sup> / consult test is more powerful for $p < 0.125$ (and values greater than this should be unlikely)	B1 B1  (2) <b>12</b>
<b>Notes:</b>		
(a)	M1 for $1 - P(X \leq 3)$ and $X \sim B(40, 0.05)$	
(b)	M1 for a correct interpretation of P(Type II error)	
(c)	B1 must be 2dp	
(d)	M1 for a correct strategy 1 <sup>st</sup> A1 for a correct numerical expression	
(e)	1 <sup>st</sup> B1 for correct points (accept $\pm$ one 2mm square) 2 <sup>nd</sup> B1 for curve	
(f)	1 <sup>st</sup> B1 for selecting 2 <sup>nd</sup> test 2 <sup>nd</sup> B1 for a suitable supporting reason eg more powerful for small values of $p/p$ around 0.05	

Question Number	Scheme	Marks
<p><b>5.</b></p> <p><b>(a)</b></p>	$s_x^2 = \frac{1559691 - 6 \times \left(\frac{3059}{6}\right)^2}{5} = 22.1666\dots$ $H_0: \sigma_x^2 = \sigma_y^2 \quad H: \sigma_x^2 \neq \sigma_y^2$ $\frac{s_x^2}{s_y^2} = 1.895\dots$ $F_{5,4} = 6.26$ $\frac{s_x^2}{s_y^2} = 1.895\dots$ <p><b>awrt 1.90</b> and comment</p> <p>: not significant - variances of <b>weights</b> of the two <b>boxes</b> can be assumed equal.</p>	<p>M1</p> <p>B1</p> <p>M1</p> <p>B1</p> <p>A1</p> <p>(5)</p>
<p><b>(b)</b></p>	$\bar{x} = 509.833\dots \Rightarrow \bar{x} - \bar{y} = 5.03333$ $s_p^2 = \frac{5s_x^2 + 4s_y^2}{9} = 17.513\dots$ <p><b>17.5</b></p> <p>5% two tail <math>t</math> value is <math>t_9 = 1.833</math></p> <p>90% confidence interval is <math>5.03\dots \pm 1.833 \times \sqrt{17.513\dots} \times \sqrt{\frac{1}{6} + \frac{1}{5}}</math></p> <p>(0.388....., 9.6782...)</p> <p><b>awrt (0.388, 9.68)</b></p>	<p>M1</p> <p>M1A1</p> <p>B1</p> <p>M1</p> <p>A1, A1</p> <p>(7)</p>
<p><b>(c)</b></p>	<p>Zero is not in CI, there <u>is</u> evidence to <u>reject</u> the manufacturer's claim</p> <p>Or the weight of the contents of the boxes has changed.</p>	<p>B1ft, B1ft</p> <p>(2)</p> <p><b>14</b></p>
<p><b>Notes:</b></p> <p><b>(a)</b></p> <p><b>(b)</b></p>	<p>1<sup>st</sup> M1 for use of the correct formula for <math>s_x^2</math> with reasonable attempt at <math>\sum x^2</math> and <math>\sum x</math></p> <p>2<sup>nd</sup> M1 for use of the correct test statistic. Allow use of 3.42 instead of <math>3.42^2</math>. Top must be their variance.</p> <p>1<sup>st</sup> M1 for attempting <math>\bar{x} - \bar{y}</math> can follow through their <math>\bar{x}</math></p> <p>2<sup>nd</sup> M1 for attempt to find pooled estimate of variance</p> <p>3<sup>rd</sup> M1 for use of correct formula for CI allow any <math>t</math> value and ft their <math>\bar{x}</math> and <math>s_p</math></p>	

Question Number	Scheme	Marks
<b>6.</b>  <b>(a)</b>	$E(Y^m) = \frac{n}{\beta^n} \int y^m \times y^{n-1} dy =, \left[ \frac{n}{\beta^n} \times \frac{1}{m+n} \times y^{m+n} \right]_0^\beta$ $= \frac{n}{\beta^n} \times \frac{1}{m+n} \times \beta^{m+n} = \frac{n}{m+n} \beta^m \quad (*)$	M1, A1  A1cso  (3)
<b>(b)</b>	$E(Y) = \frac{n}{n+1} \beta$	B1  (1)
<b>(c)</b>	$E(Y^2) = \frac{n}{n+2} \beta^2, \quad \text{Var}(Y) = E(Y^2) - [E(Y)]^2$ $\text{Var}(Y) = \frac{n}{n+2} \beta^2 - \frac{n^2}{(n+1)^2} \beta^2 = \frac{n}{(n+1)^2 (n+2)} \beta^2 \quad (*)$	B1, M1  A1cso  (3)
<b>(d)</b>	As $n \rightarrow \infty$ $E(Y) \rightarrow \beta$ , $\text{Var}(Y) \rightarrow 0$ So $Y$ is a consistent estimator for $\beta$ .	M1, A1 A1  (3)
<b>(e)</b>	$k = \frac{n+1}{n}$	B1  (1)
<b>(f)</b>	$\text{Var}(M) = 4\text{Var}(\bar{X}) = 4 \frac{\sigma^2}{n} = \frac{4}{n} \times \frac{\beta^2}{12} = \frac{\beta^2}{3n}$ $\frac{(n+1)^2}{n^2} \times \frac{n}{(n+1)^2 (n+2)} \beta^2 = \frac{\beta^2}{n(n+2)} < \frac{\beta^2}{3n} \text{ so } S \text{ is better } (n > 1)$	B1  M1A1  (3)
<b>(g)</b>	Max = 9.1, $s = \frac{6}{5} \times 9.1 = \underline{\underline{10.9(2)}}$	M1A1  (2) <b>16</b>



Question Number	Scheme	Marks
<p><b>Notes:</b></p> <p>(a)</p> <p>(c)</p> <p>(d)</p> <p>(f)</p> <p>(g)</p>	<p>M1 for attempt to integrate <math>y^m f(m)</math>            1<sup>st</sup> A1 for correct integration (limits not needed yet)            2<sup>nd</sup> A1 for use of correct limits and proceeding to printed answer. No incorrect working seen.</p> <p>M1 for use of their <math>E(Y)</math> and <math>E(Y^2)</math> in a correct formula for <math>\text{Var}(Y)</math></p> <p>M1 for examining both <math>E(Y)</math> and <math>\text{Var}(Y)</math> for <math>n \rightarrow \infty</math>            1<sup>st</sup> A1 for correct limits for both the above            2<sup>nd</sup> A1 for a correct statement following correct working</p> <p>M1 for attempting <math>\text{Var}(S)</math></p> <p>M1 for correct use of <math>S</math> to find estimate</p>	
<p>7.</p> <p>(a)</p>	$s_x^2 = \frac{214856 - 20 \times \left(\frac{2072}{20}\right)^2}{19} = 10.357\dots$ <p><b>awrt</b></p> <p><b>10.4</b></p> <p><math>H_0 : \sigma = 2.8</math> (or <math>\sigma^2 = \dots</math>)    <math>H_1 : \sigma \neq 2.8</math> (or <math>\sigma^2 \neq \dots</math>)</p> $\frac{(n-1)s^2}{\sigma^2} \sim \chi^2_{19} \quad \text{test statistic} = 25.102\dots$ <p><b>awrt</b></p> <p><b>25.1</b></p> <p><math>\chi^2_{19}(0.025) = 32.852, \quad \chi^2_{19}(0.975) = 8.907</math></p> <p>Not significant so no evidence of a change in standard deviation</p>	<p>B1</p> <p>B1</p> <p>M1A1</p> <p>B1B1</p> <p>A1</p> <p>(7)</p>





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