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2. At time t seconds ($t \geq 0$), a particle P has position vector \mathbf{p} metres, with respect to a fixed origin O , where

$$\mathbf{p} = (3t^2 - 6t + 4)\mathbf{i} + (3t^3 - 4t)\mathbf{j}.$$

Find

(a) the velocity of P at time t seconds, (2)

(b) the value of t when P is moving parallel to the vector \mathbf{i} . (3)

When $t = 1$, the particle P receives an impulse of $(2\mathbf{i} - 6\mathbf{j})$ N s. Given that the mass of P is 0.5 kg,

(c) find the velocity of P immediately after the impulse. (4)



3. A car of mass 1000 kg is moving at a constant speed of 16 m s^{-1} up a straight road inclined at an angle θ to the horizontal. The rate of working of the engine of the car is 20 kW and the resistance to motion from non-gravitational forces is modelled as a constant force of magnitude 550 N .

(a) Show that $\sin \theta = \frac{1}{14}$.

(5)

When the car is travelling up the road at 16 m s^{-1} , the engine is switched off. The car comes to rest, without braking, having moved a distance y metres from the point where the engine was switched off. The resistance to motion from non-gravitational forces is again modelled as a constant force of magnitude 550 N .

(b) Find the value of y .

(4)



4.

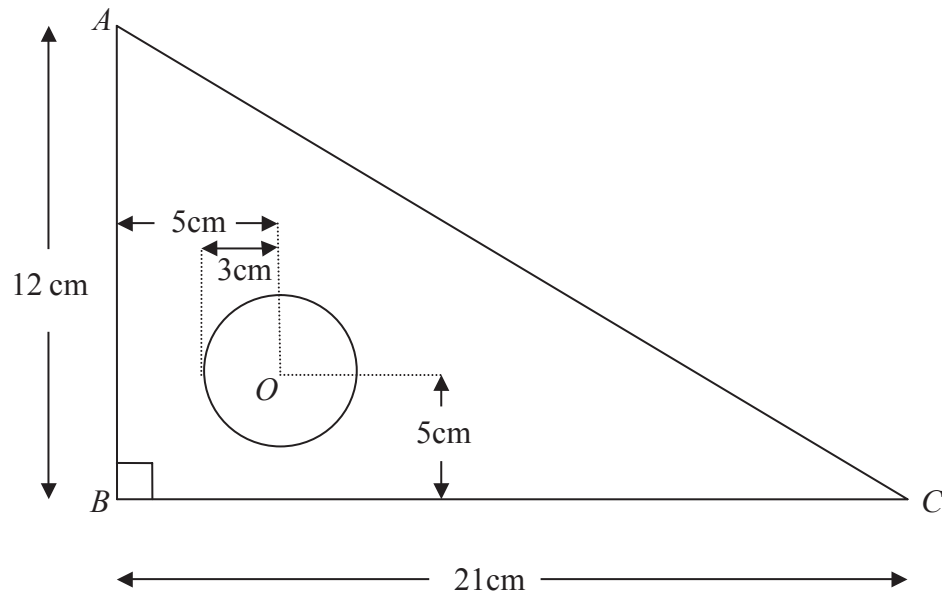


Figure 1

A set square S is made by removing a circle of centre O and radius 3 cm from a triangular piece of wood. The piece of wood is modelled as a uniform triangular lamina ABC , with $\angle ABC = 90^\circ$, $AB = 12$ cm and $BC = 21$ cm. The point O is 5 cm from AB and 5 cm from BC , as shown in Figure 1.

- (a) Find the distance of the centre of mass of S from
- AB ,
 - BC .
- (9)**

The set square is freely suspended from C and hangs in equilibrium.

- (b) Find, to the nearest degree, the angle between CB and the vertical.
- (3)**





Question 4 continued

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(Total 12 marks)

Q4

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5.

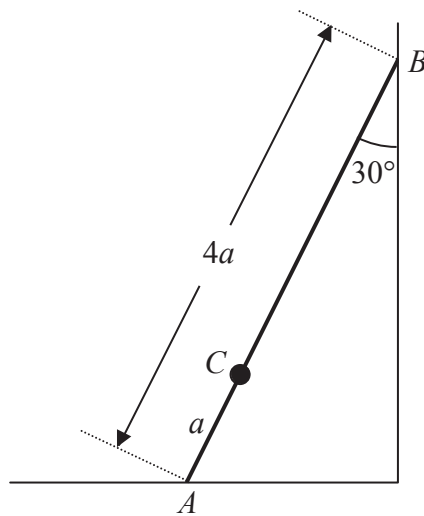


Figure 2

A ladder AB , of mass m and length $4a$, has one end A resting on rough horizontal ground. The other end B rests against a smooth vertical wall. A load of mass $3m$ is fixed on the ladder at the point C , where $AC = a$. The ladder is modelled as a uniform rod in a vertical plane perpendicular to the wall and the load is modelled as a particle. The ladder rests in limiting equilibrium making an angle of 30° with the wall, as shown in Figure 2.

Find the coefficient of friction between the ladder and the ground.

(10)





Question 5 continued

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6.

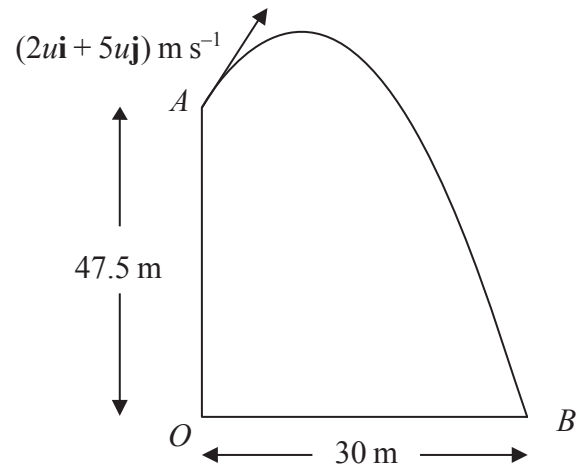


Figure 3

[In this question, the unit vectors \mathbf{i} and \mathbf{j} are in a vertical plane, \mathbf{i} being horizontal and \mathbf{j} being vertical.]

A particle P is projected from the point A which has position vector $47.5\mathbf{j}$ metres with respect to a fixed origin O . The velocity of projection of P is $(2u\mathbf{i} + 5u\mathbf{j})\text{ m s}^{-1}$. The particle moves freely under gravity passing through the point B with position vector $30\mathbf{i}$ metres, as shown in Figure 3.

- (a) Show that the time taken for P to move from A to B is 5 s . (6)
- (b) Find the value of u . (2)
- (c) Find the speed of P at B . (5)



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7. A particle P of mass $2m$ is moving with speed $2u$ in a straight line on a smooth horizontal plane. A particle Q of mass $3m$ is moving with speed u in the same direction as P . The particles collide directly. The coefficient of restitution between P and Q is $\frac{1}{2}$.

(a) Show that the speed of Q immediately after the collision is $\frac{2}{5}u$. (5)

(b) Find the total kinetic energy lost in the collision. (5)

After the collision between P and Q , the particle Q collides directly with a particle R of mass m which is at rest on the plane. The coefficient of restitution between Q and R is e .

(c) Calculate the range of values of e for which there will be a second collision between P and Q . (7)



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