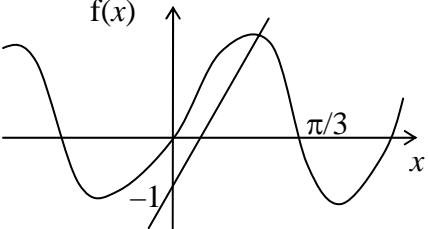
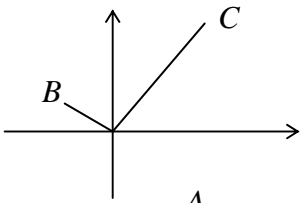
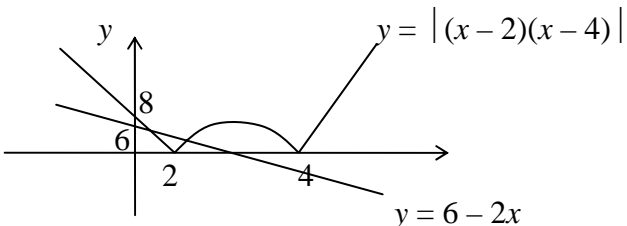
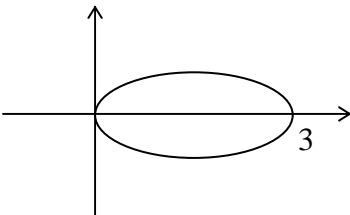


Question Number	Scheme	Marks
<p>1. (a)</p> <p>(b)</p>	$(r + 1)^3 - (r - 1)^3 = (r^3 + 3r^2 + 3r + 1) - (r^3 - 3r^2 + 3r - 1)$ $= 6r^2 + 2$ <p>attempt to use an identity</p> $\sum_{r=1}^n (6r^2 + 2) = \cancel{2^3} - 0^3$ $= \cancel{3^3} - 1^3$ $\cancel{4^3} - \cancel{2^3}$ $\vdots \quad \vdots$ $(\cancel{n-1})^3 - (\cancel{n-3})^3$ $n^3 - (\cancel{n-2})^3$ $(n + 1)^3 - (\cancel{n-1})^3$ $= (n + 1)^3 + n^3 - 1^3$ <p>differences (must see)</p> $6 \sum_{r=1}^n r^2 = (n + 1)^3 + n^3 - 1 - 2n$ <p>2n or equiv.</p> $= 2n^3 + 3n^2 + n$ $\sum_{r=1}^n r^2 = \frac{1}{6}n(2n + 1)(n + 1) \quad (*)$ <p>Sub. $\Sigma 2$ and $\div 6$ or equiv. c.s.o.</p>	<p>M1</p> <p>A1 (2)</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>M1, A1</p> <p>(6 marks)</p>
<p>2. (a)</p> <p>or</p> <p>(b)</p>	 <p>$y = \sin 3x$</p> <p>$y = 2x - 1$</p> <p>1 point where they meet</p> <p>Shape</p> <p>Asymptotic behaviour to $y = -2x + 1$</p> <p>Cross x-axis once + comment</p> <p>Attempt to diff. $\cos 3x$ + two terms for M1</p> $f'(x) = 3\cos 3x - 2$ $u_1 = 0.8 - \frac{0.075}{-4.212}$ $= 0.8179$ $u_2 = 0.8177$	<p>B1</p> <p>B1</p> <p>B1 (3)</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>M1, A1</p> <p>M1</p> <p>A1</p> <p>A1 (5)</p> <p>(8 marks)</p>

Question Number	Scheme	Marks
<p>3. (a)</p> <p>ALT</p> <p>(b)</p>	$ z = 2\sqrt{2} \quad w = 2$ $\therefore wz^2 = (2\sqrt{2})^2 \times 2 = 16$ $\arg z = -\frac{\pi}{4} \quad \arg w = \frac{5\pi}{6}; \therefore \arg wz^2 = -\frac{\pi}{4} - \frac{\pi}{4} + \frac{5\pi}{6} = \frac{\pi}{3}, 60^\circ$ $z^2 = -8i; \therefore z^2w = 8 + 8\sqrt{3}i$ $ z^2w = \sqrt{8^2 + 8^2 \times 3}$ $= 16$ $\arg z^2w = \tan^{-1}\sqrt{3}$ $= \frac{\pi}{3}$  <p>Points A and B Point C</p> $\text{angle } BOC = \frac{5\pi}{6} - \frac{\pi}{3}$ $= \frac{\pi}{2}, 90^\circ$	<p>M1, A1</p> <p>M1, A1</p> <p>M1, A1 (6)</p> <p>M1, A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>B1ft</p> <p>M1</p> <p>A1 (4)</p> <p>(10 marks)</p>
<p>4. (a)</p> <p>(b)</p> <p>(c)</p>	$IF = e^{\int 1+\frac{3}{x} dx}$ $= e^{x+3\ln x}$ $= e^x e^{\ln x^3}$ $= x^3 e^x$ <p>must see</p> $x^3 e^x y = \int x^3 e^x \frac{1}{x^2} dx$ $= \int x e^x dx$ $= x e^x - e^x + c$ <p>∫ by parts</p> $y = \frac{1}{x^2} - \frac{1}{x^3} + \frac{c}{x^3} e^{-x}$ <p>o.e.</p> $I = c e^{-1} \therefore c = e^1$ $y = \frac{1}{4} - \frac{1}{8} + \frac{e \cdot e^{-2}}{8}$ $= \frac{1}{8}(1 + e^{-1})$ <p>or = 0.171</p> <p>0.171 or better</p>	<p>M1</p> <p>A1</p> <p>A1 (3)</p> <p>M1</p> <p>M1 A1</p> <p>A1 (4)</p> <p>M1</p> <p>M1</p> <p>A1 (3)</p> <p>(10 marks)</p>

Question Number	Scheme	Marks
<p>5. (a)</p>  <p>(b) $6 - 2x = (x - 2)(x - 4)$ and $-6 + 2x = (x - 2)(x - 4)$ $x^2 - 4x + 2 = 0$ $x^2 - 8x + 14 = 0$ either $x = \frac{4 \pm \sqrt{16 - 8}}{2}$ $x = \frac{8 \pm \sqrt{64 - 56}}{2}$ $= 2 - \sqrt{2}$ $= 4 - \sqrt{2}$</p> <p>(c) $2 - \sqrt{2} < x < 4 - \sqrt{2}$</p>	<p>Line crosses axes Curve shape Axes contacts 6, 8, 3 Cusps at 2 and 4</p> <p>PI & attempt diff.</p> <p>subst. in eqn. & equate</p> <p>solving sim. eqn.</p> <p>ft on their λ and μ</p>	<p>B1 B1 B1 B1 (4) M1, M1 M1 A1, A1 (5) M1, A1 (2) (11 marks)</p>
<p>6. (a)</p> $m^2 + 4m + 5 = 0$ $m = \frac{-4 \pm \sqrt{-4}}{2}$ $= -2 \pm i$ $y = e^{-2x}(A \cos x \pm B \sin x)$ $PI = \lambda \sin 2x + \mu \cos 2x$ $y' = 2\lambda \cos 2x - 2\mu \sin 2x$ $y'' = -4\lambda \sin 2x - 4\mu \cos 2x$ $\therefore -4\lambda - 8\mu + 5\lambda = 65$ $-4\mu + 8\lambda + 5\mu = 0$ $\lambda - 8\mu = 65$ $8\lambda + \mu = 0$ $64\lambda + 8\mu = 0$ $65\lambda = 65$ $\lambda = 1, \mu = -8$ $y = e^{-2x}(A \cos x + B \sin x) + \sin 2x - 8 \cos 2x$ <p>(b) As $x \rightarrow \infty, e^{-2x} \rightarrow 0 \therefore y \rightarrow \sin 2x - 8 \cos 2x$ $y \rightarrow R \sin(2x + \alpha)$ $R = \sqrt{65}$ $\alpha = \tan^{-1} -8 = -1.446 \text{ or } -82.9^\circ$</p>	<p>PI & attempt diff.</p> <p>subst. in eqn. & equate</p> <p>solving sim. eqn.</p> <p>ft on their λ and μ</p>	<p>M1 A1 M1 M1 A1 M1 M1 A1 A1ft (9) B1ft M1 A1 (3) (12marks)</p>

Question Number	Scheme	Marks
7. (a)	 <p>Shape + horiz. axis 3</p>	B1 B1 (2)
(b)	$\text{Area} = \frac{1}{2} \int r^2 d\theta$ $= \frac{1}{2} \int 9 \cos^2 2\theta d\theta$ <p style="text-align: right;">use of $\frac{1}{2} \int r^2$</p> $= \frac{9}{2} \int \frac{\cos 4\theta + 1}{2} d\theta$ <p style="text-align: right;">use of $\cos 4\theta = 2\cos^2 2\theta - 1$</p> $= \frac{9}{2} \left[\frac{\sin 4\theta}{8} + \frac{\theta}{2} \right]_{\frac{\pi}{6}}^{\frac{\pi}{4}}$ $= \frac{9}{2} \left[\frac{\pi}{8} - \frac{\sqrt{3}}{16} - \frac{\pi}{12} \right]$ <p style="text-align: right;">subst. $\frac{\pi}{4}$ and $\frac{\pi}{6}$</p> $= \frac{9}{2} \left[\frac{\pi}{24} - \frac{\sqrt{3}}{16} \right] \text{ or } 0.103$	M1 M1 ∫ dM1, A1 M1 A1 (6)
(c)	$r \sin \theta = 3 \sin \theta \cos 2\theta$ $\frac{dy}{d\theta} = 3 \cos \theta \cos 2\theta - 6 \sin \theta \sin 2\theta$ <p style="text-align: right;">diff. $r \sin \theta$</p> $\frac{dy}{d\theta} = 0 \Rightarrow 6 \cos^2 \theta - 3 \cos \theta - 12 \sin^2 \theta \cos \theta = 0$ <p style="text-align: right;">use of $\frac{dy}{d\theta} = 0$</p> $6 \cos^2 \theta - 3 \cos \theta - 12(1 - \cos^2 \theta) \cos \theta = 0$ <p style="text-align: right;">use double angle formula</p> $18 \cos^3 \theta - 15 \cos \theta = 0$ <p style="text-align: right;">solving</p> $\cos \theta = 0 \quad \text{or} \quad \cos^2 \theta = \frac{5}{6} \quad \text{or} \quad \tan^2 \theta = \frac{1}{5} \quad \text{or} \quad \sin^2 \theta = \frac{1}{6}$ $\therefore r = 3(2 \times \frac{5}{6}) - 1$ $= 2$ $\therefore r \sin \theta = 2 \sqrt{\frac{1}{6}}$ <p style="text-align: right;">use of $d = 2r \sin \theta$</p> $d = \frac{2\sqrt{6}}{3}$	M1, A1 M1 M1 M1 A1 M1 A1 (8)
		(16 marks)