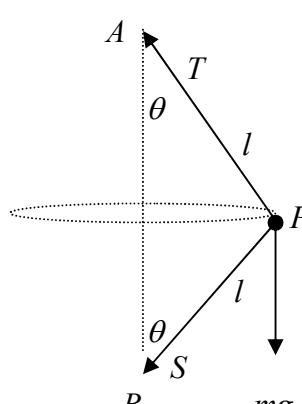
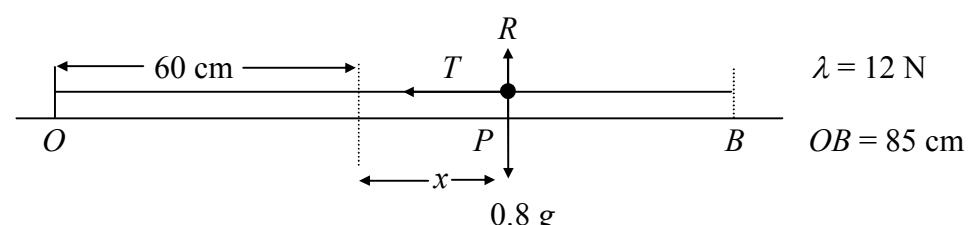


Question Number	Scheme	Marks
1.	$R = mg$ $F = \mu R = \mu mg$ <p>Attempt to relate <math>Fd</math> to EPE</p> $\frac{2}{3} mg d = \frac{4 mg (\frac{a}{2})^2}{2a}$ <p>Final answer: <math>d = \frac{3}{4} a</math></p>	B1 B1 M1 M1 A1 ft A1 (6) (6 marks)
2.	$( \Downarrow ) \quad R \cos 10^\circ = mg$ $( \leftrightarrow ) \quad R \sin 10^\circ = \frac{mv^2}{r}$ <p>Solving for <math>r</math>: <math>r = \left[ \frac{18^2}{g \tan 10^\circ} \right]</math></p> <p><math>r = 190</math> (m) [Accept 187, 188]</p>	M1 A1 M1 A1 ft M1 A1 (6) (6 marks)
3. (a)	$\frac{1}{10}x(4 - 3x) = 0.2 a$ $\frac{1}{10}x(4 - 3x) = 0.2v \frac{dv}{dx} \text{ or } \frac{1}{10}x(4 - 3x) = 0.2 \frac{d(\frac{1}{2}v^2)}{dx}$ <p>Integrating: <math>v^2 = 2x^2 - x^3</math> (+ C)</p> <p>Substituting <math>x = 6</math>, <math>v = 0</math> to find candidate's C</p> $v^2 = 2x^2 - x^3 + 144$	M1 A1 M1 M1 A1 M1 A1 (7)
(b)	Substituting $x = 0$ and finding $v$ ; $v = 12$ ( $\text{m s}^{-1}$ )	M1; A1 ft (2)  (9 marks)

(ft = follow through mark)

Question Number	Scheme	Marks
4. (a)	 <p> <math>(\downarrow) (T - S) \cos \theta = mg</math>  <math>(\leftrightarrow) (T + S) \sin \theta = mr\omega^2</math>  <math>= m(l \sin \theta) \omega^2</math>          Finding <math>T</math> in terms of <math>l</math>, <math>m</math>, <math>\omega^2</math> and <math>g</math>  <math>T = \frac{1}{6}m(3l\omega^2 + 4g)</math> (*)       </p>	M1 A1 M1 A1 ft A1 M1 A1 (7)
(b)	$S = \frac{1}{6}m(3l\omega^2 - 4g)$	M1 A1 (2)
(c)	Setting $S \geq 0$ ; $\omega^2 \geq \frac{4g}{3l}$ (*)	M1 A1 (2)
		<b>(11 marks)</b>
5. (a)	 <p>         Hooke's Law: <math>T = \frac{12x}{0.6}</math> [= <math>20x</math>]          Equation of motion: <math>(-)T = 0.8\ddot{x}</math>  <math>-\frac{12x}{0.6} = 0.8\ddot{x}</math>      <math>\ddot{x} = -25x</math>          Finding <math>\omega</math> from derived equation of form <math>\ddot{x} = -\omega^2x</math>          Period <math>= \frac{2\pi}{\omega} = \frac{2\pi}{5}</math> (*)       </p>	M1 M1 A1 M1 A1 (5)
(b)	Substituting (candidate's) $\omega$ and $a$ in $\omega^2a$ ; $= 25 \times 0.25 = 6.25 \text{ (m s}^{-2}\text{)}$ (or finding $T_{\max} = 0.8a \Rightarrow a = 5/0.8 = 6.25$ )	M1; A1 (2)
(c)	Complete method for $x$ ; $x = 0.25 \cos 10^\circ$ (-0.2098) Using $v^2 = \omega^2(a^2 - x^2) \Rightarrow v = (\pm)5\sqrt{[(0.25)^2 - (0.25 \cos 10^\circ)]}$ $v = (\pm) 0.68 \text{ (m s}^{-1}\text{)}$	M1 A1 M1 A1 ft A1 (5)
(d)	Direction $\overrightarrow{OB}$ or equivalent	B1 (1)
		<b>(13 marks)</b>

(ft = follow through mark; (\*) indicates final line is given on the paper)

Question Number	Scheme	Marks
6. (a)	<p>Energy: <math>\frac{1}{2}mv^2 - \frac{1}{2}mu^2 = mga(1 - \cos \theta)</math></p> <p>Radial: <math>(\pm R) + mg \cos \theta = \frac{mv^2}{a}</math></p> <p>Eliminating <math>v</math> and finding <math>\cos \theta = , \frac{u^2 + 2ga}{3ga}</math></p>	M1 A1 A1 M1 A1 M1, A1 (7)
(b)	<p>Energy (C and ground): <math>\frac{1}{2}m\left(\frac{9ag}{2}\right) - \frac{1}{2}mv^2 = mga(1 - \cos \theta)</math></p> <p>Eliminating <math>v</math>: <math>\frac{1}{2}m\left(\frac{9ag}{2}\right) - \frac{1}{2}mag \cos \theta = mga(1 + \cos \theta)</math></p> <p><math>\cos \theta = \frac{5}{6}</math></p> <p><math>\theta = 34^\circ</math></p>	M1 A1 M1 A1 M1 A1 ft A1 (7) <b>(14 marks)</b>
Alt (b)	<p>Or energy (A and ground): <math>\frac{1}{2}m\left(\frac{9ag}{2}\right) - \frac{1}{2}mu^2 = 2mga</math></p> <p><math>u^2 = \frac{1}{2}ga</math></p> <p>Using with (a) to find <math>\cos \theta = \frac{5}{6}; \theta = 34^\circ</math></p>	M1 A1 M1 A1 M1 A1; A1 (7)
Alt	Projectile approach: $V_x = v \cos \theta; V_y^2 = (v \sin \theta)^2 + 2ga(1 + \cos \theta)$ $\left(\frac{9ag}{2}\right) = V_x^2 + V_y^2 \Rightarrow \left(\frac{9ag}{2}\right) - v^2 = 2ga(1 + \cos \theta)$ – M1 A1, then scheme	

(ft = follow through mark)

Question Number	Scheme	Marks
7. (a)	$V = \pi \int y^2 \, dx = \frac{1}{4} \pi \int (x-2)^4 \, dx$ $\int (x-2)^4 \, dx = \frac{1}{5} (x-2)^5$ $V = \frac{8\pi}{5}$	M1 M1 A1 A1 (4)
(b)	Using $\pi \int xy^2 \, dx = \frac{1}{4} \pi \int x(x-2)^4 \, dx$ Correct strategy to integrate [e.g. substitution, expand, by parts] [e.g. $\frac{1}{4} \pi \int (u-2)^4 \, du$ ; $\frac{1}{4} \pi \int (x^5 - 8x^4 + 24x^3 - 32x^2 + 16x) \, dx$ ] $= \frac{1}{4} \pi \left[ \frac{2u^5}{5} + \frac{u^6}{6} \right]$ or $\frac{1}{4} \pi \left[ \frac{x^6}{6} - \frac{8x^5}{5} + 6x^4 - \frac{32x^3}{3} + 8x^2 \right]$ $= \frac{8\pi}{15}$ limits need to be used correctly $V_c(\rho) \bar{x} = \pi(\rho) \int xy^2 \, dx$ seen anywhere $\bar{x} = \frac{1}{3} \text{ cm } (*)$ no incorrect working seen	M1 M1 M1 A1 A1 (7) M1 A1 M1
(c)	Moments about B: $8A = 10W - 2W(\frac{1}{3})$ $A = \frac{59W}{12}$ (4.9W)	M1 A1 A1 M1 A1 (5) <b>(16 marks)</b>

(ft = follow through mark; (\*) indicates final line is given on the paper)