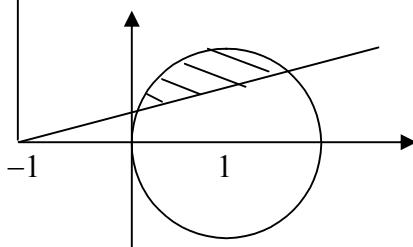
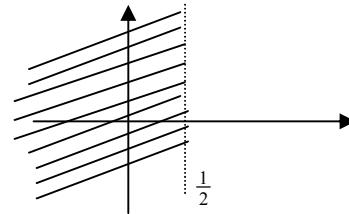


Question number	Scheme	Marks
1.	$\overrightarrow{AB} \times \overrightarrow{AC} = (\mathbf{b} - \mathbf{a}) \times (\mathbf{c} - \mathbf{a}) = (\mathbf{b} \times \mathbf{c}) - (\mathbf{a} \times \mathbf{c}) - (\mathbf{b} \times \mathbf{a}) + (\mathbf{a} \times \mathbf{a})$ <p>Using $\mathbf{a} \times \mathbf{c} = -\mathbf{c} \times \mathbf{a}$ or $\mathbf{b} \times \mathbf{a} = -\mathbf{a} \times \mathbf{b}$ or $\mathbf{a} \times \mathbf{a} = \mathbf{0}$</p> $ \overrightarrow{AB} \times \overrightarrow{AC} = AB \cdot AC \sin \theta = 2 \times \text{area of triangle}, \text{ or equivalent}$ <p>Final result : $\frac{1}{2} \mathbf{a} \times \mathbf{b} + \mathbf{b} \times \mathbf{c} + \mathbf{c} \times \mathbf{a} \quad (*)$</p>	M1 A1 B1 M1 A1 cso [5]
2.	$f(1) = 3 \times 7 - 1 = 20; \text{ divisible by 4}$ $f(k+1) = (2k+3)7^{k+1} - 1$ <p>Showing that $f(k+1) = f(k) + 4m$ or equivalent</p> $\begin{aligned} \text{e.g. } f(k+1) - f(k) &= (2k+3)7^{k+1} - 1 - \{(2k+1)7^k - 1\} \\ &= (12k+20)7^k = 4(3k+5)7^k \end{aligned}$ <p>If true for $n = k$, then true for $n = k + 1$</p> <p>Conclusion , with no wrong working seen.</p>	B1 B1 M1 A1 M1 A1 [6]

(cso = correct solution only)

Question number	Scheme	Marks
3.	(a) Deriving characteristic equation $(4 - \lambda)(-9 - \lambda) + 30 = 0$ $\Rightarrow \lambda^2 + 5\lambda - 6 = 0 \Rightarrow (\lambda + 6)(\lambda - 1) = 0 \Rightarrow \lambda = -6, \lambda = 1$ (b) Stating, implying or showing $\lambda = 1$ associated with point invariant line. $\Rightarrow \begin{pmatrix} 4 & -5 \\ 6 & -9 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} x \\ y \end{pmatrix}$ Equation is $4x - 5y = x \Rightarrow 3x - 5y = 0$ any equivalent form	M1 A1 M1 A1 (4) B1 M1 A1 (3) [7]
4.	(i) (a)  Circle One half line correct Second half line [s.c. Allow B1 for two “full” lines in correct position]	M1 A1 B1 B1 (4)
	(b) Shading correct region	A1 ft (1)
	(ii) (a) Rearrange $w = \frac{z-1}{z}$ to give $z = f(w)$ or $z - 1 = f(w)$ $\left(z = \frac{1}{1-w}, \Rightarrow \right) z - 1 = \frac{w}{1-w}$, or $ z - 1 = z w \Rightarrow z w = 1$ Completion: ($ z - 1 = 1 \rightarrow$) $ w = 1 - w = w - 1 *$	M1 A1 A1 (3)
	(b)  Correct line shown Correct shading	M1 A1 (2) [10]

(ft = follow-through mark)

Question number	Scheme	Marks
5.	<p>(a) $(\cos \theta + i \sin \theta)^5 = \cos 5\theta + i \sin 5\theta$</p> $(\cos \theta + i \sin \theta)^5 = \cos^5 \theta + 5 \cos^4 \theta (i \sin \theta) + 10 \cos^3 \theta (i \sin \theta)^2$ $+ 10 \cos^2 \theta (i \sin \theta)^3 + 5 \cos \theta (i \sin \theta)^4 + (i \sin \theta)^5$ $\cos 5\theta = \cos^5 \theta - 10 \cos^3 \theta \sin^2 \theta + 5 \cos \theta \sin^4 \theta$ $= \cos^5 \theta - 10 \cos^3 \theta (1 - \cos^2 \theta) + 5 \cos \theta (1 - 2\cos^2 \theta + \cos^4 \theta)$ $= 16 \cos^5 \theta - 20 \cos^3 \theta + 5 \cos \theta \quad (*)$ <p>(b) $\cos 5\theta = -1$ (or 1, or 0)</p> $5\theta = (2n \pm 1)180^\circ \Rightarrow \theta = (2n \pm 1)36^\circ$ $x = \cos \theta = -1, -0.309, 0.809$	M1 M1 A1 M1 M1 A1 cso (6) M1 A1 M1 A1 (4) [10]

((*)) indicates final line is given on the paper; cso = correct solution only)

Question number	Scheme	Marks
6.	<p>(a) $\text{Det } \mathbf{A} = 3(u - 3) - (u - 5) - (3 - 5) = 2u - 2$ [= $2(u - 1)$] (*)</p> <p>(b) Cofactors $\begin{pmatrix} u-3 & 5-u & -2 \\ -(u+3) & 3u+5 & -4 \\ 2 & -4 & 2 \end{pmatrix}$ (- 1 A mark for each term wrong)</p> $\mathbf{A}^{-1} = \frac{1}{2(u-1)} \begin{pmatrix} u-3 & -(u+3) & 2 \\ 5-u & 3u+5 & -4 \\ -2 & -4 & 2 \end{pmatrix}$ <p>(c) $\begin{pmatrix} a \\ b \\ c \end{pmatrix} = \mathbf{A}^{-1} \begin{pmatrix} 3 \\ 1 \\ 6 \end{pmatrix}$, Using $u = 6$: $\frac{1}{10} \begin{pmatrix} 3 & -9 & 2 \\ -1 & 23 & -4 \\ -2 & -4 & 2 \end{pmatrix} \begin{pmatrix} 3 \\ 1 \\ 6 \end{pmatrix} = \frac{1}{10} \begin{pmatrix} 12 \\ -4 \\ 2 \end{pmatrix}$</p> $a = \frac{6}{5}, \quad b = -\frac{2}{5}, \quad c = \frac{1}{5}$ (One correct A1, other 2 correct A1) <p>[Algebraic approach: Finding one value M1 A1, other two A1]</p>	M1 A1 (2) M1 A3 M1 A1 ft (6) M1 A1, A1 (3) [11]

((*)) indicates final line is given on the paper; awrt = anything which rounds to; ft = follow-through mark)

Question number	Scheme	Marks
7.	<p>(a) Normal to plane is $(-\mathbf{i} + 5\mathbf{j} + 3\mathbf{k})$</p> <p>Equation of plane: $\mathbf{r} \cdot (-\mathbf{i} + 5\mathbf{j} + 3\mathbf{k}) = (\mathbf{i} + 2\mathbf{j} - \mathbf{k}) \cdot (-\mathbf{i} + 5\mathbf{j} + 3\mathbf{k})$</p> $\Rightarrow -x + 5y + 3z = -1 + 10 - 3 = 6 \text{ or equivalent } (*)$ <p>[If vector equation of plane is by-passed, then B1 M2 A1]</p> <p>(b) $\frac{1}{\sqrt{35}}$</p> $ 6 - (\mathbf{i} + 2\mathbf{j} + 2\mathbf{k}) \cdot (-\mathbf{i} + 5\mathbf{j} + 3\mathbf{k}) $ <p>or $\overrightarrow{PQ} \cdot (-\mathbf{i} + 5\mathbf{j} + 3\mathbf{k}) = 3\mathbf{k} \cdot (-\mathbf{i} + 5\mathbf{j} + 3\mathbf{k})$</p> $\text{Distance} = \frac{9}{\sqrt{35}} \text{ or a.w.r.t } 1.52$ <p>(c) Direction of one line in plane = $(-\mathbf{i} + 5\mathbf{j} + 3\mathbf{k})$</p> <p>Direction of another line in plane = $(3\mathbf{i} - 2\mathbf{k}) - (\mathbf{i} + 2\mathbf{j} + 2\mathbf{k})$</p> $\Rightarrow \mathbf{r} = (\mathbf{i} + 2\mathbf{j} + 2\mathbf{k}) + s(-\mathbf{i} + 5\mathbf{j} + 3\mathbf{k}) + t(2\mathbf{i} - 2\mathbf{j} - 4\mathbf{k})$ <p>or $(3\mathbf{i} - 2\mathbf{k}) + s(-\mathbf{i} + 5\mathbf{j} + 3\mathbf{k}) + t(2\mathbf{i} - 2\mathbf{j} - 4\mathbf{k})$</p>	B1 M1 M1 A1 (4) B1 M1 A1 A1 (4) M1 M1 M1 A1 (4) [12]

((*)) indicates final line is given on the paper)

Question number	Scheme	Marks
8.	(a) $x_0 = 0, y_0 = 1, \left(\frac{dy}{dx}\right)_0 = 0 - 1 = -1$	B1
	$y_1 - y_0 = 0.05(-1) \Rightarrow y_1 = 1 - 0.05 = 0.95$	M1 A1ft
	$x_1 = 0.05, y_1 = 0.95, \left(\frac{dy}{dx}\right)_1 = 0.05^2 - 0.95^2 \quad (= -0.9)$	A1 ft
	$y_2 - y_1 = 0.05(-0.9) \Rightarrow y_2 = 0.95 - 0.045 = 0.905$ (A1 is c.s.o.)	M1 A1 (6)
(b)	$\frac{dy}{dx} = x^2 - y^2 \Rightarrow \frac{d^2y}{dx^2} = 2x - 2y \frac{dy}{dx}$	M1 A1
	$\Rightarrow \frac{d^3y}{dx^3} = 2 - 2y \frac{d^2y}{dx^2} - 2\left(\frac{dy}{dx}\right)^2 \quad \text{allow at this stage}$	M1 A1 (4)
(c)	$[y_{x=0} = 1, \left(\frac{dy}{dx}\right)_{x=0} = -1,] \quad \left(\frac{d^2y}{dx^2}\right)_{x=0} = 0 - 2(1)(-1) = 2$	B1
	$\left(\frac{d^3y}{dx^3}\right)_{x=0} = 2 - 2(-1)^2 - 2(1)(2) = -4$	B1
	Maclaurin: $y = 1 - x + x^2 - \frac{2}{3}x^3$	M1 A1 (4)
	[Alternative (c) $y = 1 + a_1x + a_2x^2 + a_3x^3$	
	$\Rightarrow x^2 - (1 + a_1x + a_2x^2 + a_3x^3)^2 = a_1 + 2a_2x + 3a_3x^2 \quad \text{B1}$	[14]
	Compare coeffs $\Rightarrow a_1 = -1; a_2 = 1, a_3 = -\frac{2}{3}$. B1; M1 A1]	

((*) indicates final line is given on the paper; cso = correct solution only; ft = follow-through mark)