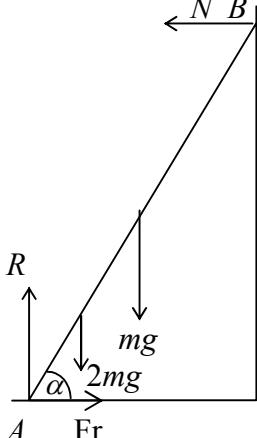


| Question number | Scheme   | Marks  |
|-----------------|--|--|
| 1. (a)          | Use of $(8 + \lambda)m$<br><b>i:</b> $3m \times 4 + \lambda m \times 4 = (8 + \lambda)m \times 2$<br>Solving to $\lambda = 2$ (*)<br><b>j:</b> $5m \times (-3) + 2m \times 2 = 10m \times k$<br>$k = -1.1$ | B1<br>M1<br>M1 A1 (4)<br>M1 A1<br>A1 (3)<br><b>(7 marks)</b> |
| 2. (a)          | $T_r = \frac{24000}{12} (= 2000)$<br>N2L: $T_r - 1200 = 1000 \times f$<br>$f = 0.08$   | M1<br>M1 A1ft<br>A1 (4)                                      |
| (b)             | Work Energy $\frac{1}{2} \times 1000 \times 14^2 = 1200d$<br>$d = 81\frac{2}{3}$ awrt 81.7   | M1 A1<br>A1 (3)  |
| (c)             | Resistances may vary with speed  | B1 (1)<br><b>(8 marks)</b>                                   |

| Question number          | Scheme  | Marks                        |                                     |                          |    |         |         |         |    |      |                             |           |                                   |
|--------------------------|---|------------------------------|-------------------------------------|--------------------------|----|---------|---------|---------|----|------|-----------------------------|-----------|-----------------------------------|
| 3.                       |  <p>(↑) <math>R = 3mg</math><br/> <math>M(B)</math><br/> <math>mg a \cos \alpha + 2mg \times \frac{3}{2} a \cos \alpha + Fr \times 2a \sin \alpha = R \times 2a \cos \alpha</math><br/> Solving to <math>Fr = \frac{3}{4} mg</math></p>  | B1<br>M1 A2 1,0<br>M1 A1     |                                     |                          |    |         |         |         |    |      |                             |           |                                   |
|                          | $Fr \leq \mu R \Rightarrow \frac{3}{4} mg \leq \mu 3mg$<br>$\mu \geq \frac{1}{4}$ (least value is $\frac{1}{4}$ )   | M1<br>M1 A1 (9)<br>(9 marks) |                                     |                          |    |         |         |         |    |      |                             |           |                                   |
| 4. (a)                   | <table style="width: 100%; text-align: center;"> <tr> <td><input type="checkbox"/></td> <td><input checked="" type="checkbox"/></td> <td><input type="checkbox"/></td> </tr> <tr> <td>MR</td> <td><math>48a^2</math></td> <td><math>12a^2</math></td> <td><math>60a^2</math></td> </tr> <tr> <td>CM</td> <td><math>4a</math></td> <td><math>(-) \frac{1}{3} \times 4a</math></td> <td><math>\bar{x}</math></td> </tr> </table> $48a^2 \times 4a - 12a^2 \times \frac{4}{3}a = 60\bar{x}$<br>Solving to $\bar{x} = \frac{44}{15}a$ (*) | <input type="checkbox"/>     | <input checked="" type="checkbox"/> | <input type="checkbox"/> | MR | $48a^2$ | $12a^2$ | $60a^2$ | CM | $4a$ | $(-) \frac{1}{3} \times 4a$ | $\bar{x}$ | B1, B1ft<br>B1<br>M1 A1<br>A1 (6) |
| <input type="checkbox"/> | <input checked="" type="checkbox"/>   | <input type="checkbox"/>     |                                     |                          |    |         |         |         |    |      |                             |           |                                   |
| MR                       | $48a^2$   | $12a^2$                      | $60a^2$                             |                          |    |         |         |         |    |      |                             |           |                                   |
| CM                       | $4a$  | $(-) \frac{1}{3} \times 4a$  | $\bar{x}$                           |                          |    |         |         |         |    |      |                             |           |                                   |
| (b)                      | $\lambda M \times 4a = M \times \frac{44}{15}a$<br>$\lambda = \frac{11}{15}$  | M1 A1<br>A1 (3)<br>(9 marks) |                                     |                          |    |         |         |         |    |      |                             |           |                                   |

| Question number | Scheme  | Marks   |
|-----------------|---|---|
| 5. (a)          | $v = \int a \, dt = 2t^2 - 8t \text{ } (+c)$<br>Using $v = 6, t = 0; v = 2t^2 - 8t + 6$<br>$v = 0 \Rightarrow 2t^2 - 8t + 6 = 0, \Rightarrow t = 1, 3$<br>$S = \int (2t^2 - 8t + 6) \, dt = \left[ \frac{2}{3}t^3 - 4t^2 + 6t \right]$<br>$= 0 - 2\frac{2}{3}$<br>Distance is $(\pm)2\frac{2}{3} \text{ m}$ | M1 A1<br>M1 A1 (4)<br>M1 A1<br>M1 A2, 1, 0<br>M1<br>A1 (7)<br><b>(11 marks)</b> |
| 6. (a)          | L.M. $2u = 2x + y$<br>NEL $y - x = \frac{1}{3}u$<br>Solving to $x = \frac{5}{9}u \text{ (*)}$<br>$y = \frac{8}{9}u \text{ (*)}$   | M1 A1<br>M1 A1<br>M1 A1<br>A1 (7)   |
| (b)             | $(\pm) \frac{8}{9}eu$<br>L.M. $\frac{10}{9}u - \frac{8}{9}eu = w$<br>NEL $w = \frac{1}{3} \left( \frac{5}{9}u + \frac{8}{9}eu \right)$  | B1<br>M1 A1<br>M1 A1  |
|                 | Solving to $e = \frac{25}{32}$<br>accept 0.7812s  | M1 A1 (7)   |
| (c)             | Q still has velocity and will <i>bounce back</i> from wall colliding with stationary P.   | B1 (1)<br><b>(15 marks)</b>   |

| Question number | Scheme   | Marks  |
|-----------------|--|--|
| 7. (a)          | $\mathbf{I} = 0.4(15\mathbf{i} + 16\mathbf{j} + 20\mathbf{i} - 4\mathbf{j})$ ( $= 0.4(35\mathbf{i} + 12\mathbf{j}) = 14\mathbf{i} + 4.8\mathbf{j}$ )<br>$ \mathbf{I}  = \sqrt{(14^2 + 4.8^2)}$ or $0.4\sqrt{(35^2 + 12^2)}$<br>= 14.8 (Ns) | M1<br>M1 for any magnitude<br>A1 (4)                                   |
| (b)             | Initial K.E. = $\frac{1}{2}m(15^2 + 16^2)$ ( $= 240.5m = 96.2$ J)<br>$\frac{1}{2}mv^2 = \frac{1}{2}m(15^2 + 16^2) = m \times 9.8 \times 1.2$<br>$v^2 = 504.52$<br>$v = 22$ (m s <sup>-1</sup> )  | M1<br>-1 each incorrect term<br>M1 A2, 1,0<br>M1<br>accept 22.5 A1 (6) |
| (c)             | $\arccos \frac{15}{22.5} = 48^\circ$   | accept 48.1° M1 A1 A1 A1 (4)   |
| (d)             | Air resistance<br>Wind (problem not 2 dimensional)<br>Rotation of ball (ball is not a particle)  | any 2 B1, B1 (2)<br><b>(16 marks)</b>                                  |
| Alt (b)         | Resolve $\uparrow$ with 16 and 9.8<br>( $\uparrow$ ) $v_y^2 = 16^2 + 2 \times (-9.8) \times (-1.2)$<br>( $v_y^2 = 279.52$ , $v_y \approx 16.7$ ....)<br>$v^2 = 15^2 + 279.52$<br>$v = 22$ (m s <sup>-1</sup> )                             | M1<br>M1 A1<br>M1 A1<br>accept 22.5 A1 (6)                             |
| Alt (c)         | $\arctan \frac{16.7}{15} = 48^\circ$   | M1 A1 A1 A1 (4)  |