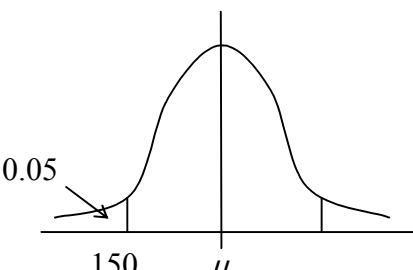
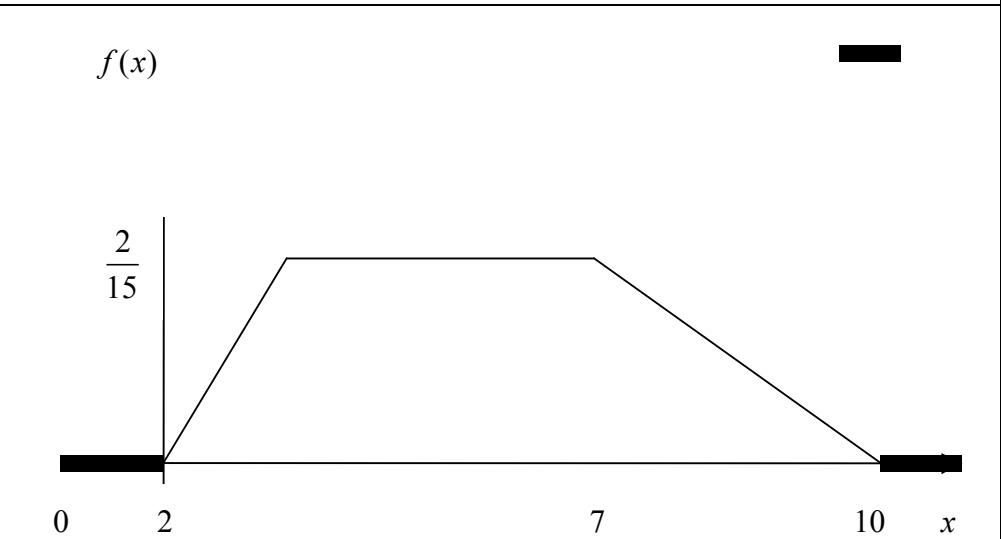


Question Number	Scheme	Marks
1. (a)	Survey is less time consuming.	B1
(b)	It is easier/quicker to analyse the results	B1 (2)
(c)	List of members	B1 (1)
(d)	The members	B1 (1) (4 marks)
2. (a)	Y is the random variable consisting of any function of the X_i that involves no other quantities.	B1 B1 (2)
(b)	$Y = \bar{X} = \frac{\sum X}{n}$	B1 (1)
(c)	When all possible samples are taken and the values of Y found then the values form a probability distribution (known as the sampling distribution of Y)	B1 B1 (2) (5 marks)
3. (a)	$E(R) = \frac{\alpha + \beta}{2} = 3 \Rightarrow \alpha + \beta = 6$	M1 A1
(b)	$\text{Var}(R) = \frac{(\beta - \alpha)^2}{12} = \frac{25}{3} \Rightarrow (\beta - \alpha)^2 = 100$ $\alpha = -2, \beta = 8$	M1 A1 M1 A1 A1 (7)
	$P(R < 6.6) = \frac{1}{10} \times 8.6 = 0.86$	M1 A1 (2) (9 marks)
4. (a)	$H_0 : \rho = 0.20, H_1 : \rho < 0.20$	B1 B1
	$X = \text{number buying single packets}, X \sim B(25, 0.20)$	
	$P(X \leq 2) = 0.0982$	M1 A1
	$0.0982 > 5\%$, so not significant	(comparison) M1
	No reason to suspect the percentage who bought crisps in single packets that day was lower than usual	(context) A1 ft (2)
	$H_0 : \rho = 0.03, H_1 : \rho \neq 0.03$	B1 B1
	$Y = \text{number buying bumper packs}, Y \sim B(300, 0.03) \Rightarrow Y \sim Po(9)$	M1
	$P(Y \leq 3) = 0.0212 \text{ and } P(Y \leq 15) = 0.9780 \Rightarrow P(Y \geq 16) = 0.0220$	M1 A1
	Critical region $Y \leq 3$ and $Y \geq 16$	A1 (6)
	Significance level = $0.0212 + 0.0220 = 0.0432$	B1 ft (1) (13 marks)

Question Number	Scheme	Marks
5. (a)	$L \sim N(\mu, 0.3^2), P(L < 150) = 0.05 \Rightarrow P\left(Z < \frac{150 - \mu}{0.3}\right) = 0.05$ $\Rightarrow \frac{150 - \mu}{0.3} = -1.6449$ $\mu = 150 + 0.49347 = 150.5$ 	M1 A1, B1 A1 (4)
(b)	X represents number less than 150cm. $X \sim B(10, 0.05)$ $P(X \leq 2) = 0.9885$	B1 M1 A1 (3)
(c)	Normal approximation $\mu = 500 \times 0.05 = 25, \sigma^2 = 23.75$ or 25 $P(X < 35) \approx P\left(Z < \frac{34.5 - 25}{\sqrt{23.75 \text{ or } 25}}\right) \pm 0.5, \text{ standardise}$ $\approx P(Z < 1.95 \text{ or } 1.9)$ $\approx 0.9744 \text{ or } 0.9713$	B1, B1 M1, M1 A1 A1 (6) (13 marks)
6. (a)	X represents number of faults per 25 m $\Rightarrow X \sim Po(1.5)$ $P(X = 4) = 0.0471$	B1 B1 (2)
(b)	Y represents number of faults per 100 m $\Rightarrow Y \sim Po(6.0)$ $P(Y < 6) = P(Y \leq 5) = 0.4457$	B1 B1
	R represents number of 100 m balls containing fewer than 6 faults $R \sim B(3, 0.4457)$	M1 A1
	$P(R = 1) = C_1^3 \times 0.4457 \times (1 - 0.4457)^2 = 0.41082$ accept 0.4111	M1 A1 (6)
(c)	S represents number of faults in a 500 m ball $\Rightarrow S \sim Po(30)$ $P(23 \leq S \leq 33) \approx P\left(\frac{22.5 - 30}{\sqrt{30}} \leq Z \leq \frac{33.5 - 30}{\sqrt{30}}\right) \pm 0.5, \text{ standardise}$ $\approx P(-1.37 \leq Z \leq 0.64)$ ≈ 0.6536	B1 M1, M1 A1 A1 A1 (6) (14 marks)

Question Number	Scheme	Marks
7. (a)	$f(x)$ 	B1 (labels) B1 (graph) B1 (axes)
(b) (i)	$F(x) = \int_0^x \frac{x}{15} dx = \frac{x^2}{30}$ for $0 \leq x \leq 2$ $F(x) = \frac{12}{15} + \int_2^x \left(\frac{4}{9} - \frac{2x}{45}\right) dx = \frac{4x}{9} - \frac{x^2}{45} - \frac{11}{9}$ for $7 \leq x \leq 10$	B1 B1 M1 A1
(ii)	$F(x) = \frac{2}{15} + \int_2^x \frac{2}{15} dx = \frac{2x}{15} - \frac{2}{15}$ for $2 \leq x \leq 7$	B1 M1 A1
	(iii)	$F(x) = 0, x < 0, F(x) = 1, x > 10$
(c)	$P(X \leq 8.2) = F(8.2) = 0.928$	M1 A1 (2)
(d)	$E(X) = \int_0^2 \frac{x^2}{15} dx + \int_2^7 \frac{2x}{15} dx + \int_7^{10} \left(\frac{4x}{9} - \frac{2x^2}{45}\right) dx$ $= \left[\frac{x^3}{45}\right]_0^2 + \left[\frac{x^2}{15}\right]_2^7 + \left[\frac{2x^2}{9} - \frac{2x^3}{125}\right]_7^{10} = 4.78$	M1 A1 A1 A1 (4)
		(17 marks)