

Question Number	Scheme	Marks
1.	<p style="text-align: center;"> 6 1 18 12 9 0 5 13 14 18 12 13 14 9 6 1 0 5 18 14 13 12 9 6 1 5 0 18 14 13 12 9 6 5 1 0 18 14 13 12 9 6 5 1 0 18 14 13 12 9 6 5 1 0 </p> <p>Datchet (18), Wraysbury (14), Staines (13), Feltham (12), Halliford (9), Ashford (6), Poyle (5), Colnbrook (1), Laleham (0).</p>	M1 A1 A1 A1 A1 A1 (5) (5 marks)
2. (a)	No negative elements in the profit row.	B1 (1)
(b)	$P = 11, x = 1, y = \frac{1}{3}, z = 0; r = \frac{2}{3} s = 0, t = 0$	M1 A1; A1 (3)
(c)	$P + z + s + t = 11$	B1
	$\Rightarrow P = 11 - z - s - t$ so increasing z, s or t would decrease P .	B1 (2)
3. (a)	$1 - C \quad 1 - C$ $2 - B \quad 2 - A$ $3 - B \quad \text{and} \quad 3 - D$ $4 - E \quad 4 - B$ $5 - D \quad 5 - A$ (b) $2 - B = 4 - C = 1 - E$ $2 - D = 5 - E$	B1 B1 (2) M1 A1 M1 A1 (4) (6 marks)

Question Number	Scheme	Marks
4. (a)		
		M1 A1 A1
		(3)
	Shortest route $ABFEHI$, length 22 km	B1 B1 (2)
(b)(i)	Odd vertices A and I only, shortest route between them needs to be repeated, hence repeat AB, BF, FE, EH, HI	M1 A1
(ii)	e.g. <u>AB</u> <u>FB</u> <u>EFG</u> <u>GIF</u> <u>EHI</u> <u>IHE</u> <u>CDA</u> <u>ACB</u>	A1 (3)
(ii)	$91 + 22 = 113$ km	M1 A1 (2)
		(Marks 10)

Question Number	Scheme							Marks																																											
5. (a)	<table border="1"> <thead> <tr> <th>a</th><th>b</th><th>c</th><th>d</th><th>e</th><th>f</th><th>$f=0?$</th></tr> </thead> <tbody> <tr><td>645</td><td>255</td><td>2.53</td><td>2</td><td>510</td><td>135</td><td>No</td></tr> <tr><td>255</td><td>135</td><td>1.89</td><td>1</td><td>135</td><td>120</td><td>No</td></tr> <tr><td>135</td><td>120</td><td>1.13</td><td>1</td><td>120</td><td>15</td><td>No</td></tr> <tr><td>120</td><td>15</td><td>8</td><td>8</td><td>120</td><td>0</td><td>Yes</td></tr> <tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr> <tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr> </tbody> </table>	a	b	c	d	e	f	$f=0?$	645	255	2.53	2	510	135	No	255	135	1.89	1	135	120	No	135	120	1.13	1	120	15	No	120	15	8	8	120	0	Yes															M1 A1 M1 A1 A1 A1 A1 (7) M1 A1 A1 (3) B1 (1) (11 marks)
a	b	c	d	e	f	$f=0?$																																													
645	255	2.53	2	510	135	No																																													
255	135	1.89	1	135	120	No																																													
135	120	1.13	1	120	15	No																																													
120	15	8	8	120	0	Yes																																													
The answer is 15																																																			
The first row would be 255 645 0.40 0 0 255 No																																																			
But the second row would then be the same as the first row above, and the solution thereafter would be the same.																																																			
Finds the H.C.F of a and b .																																																			

Question Number	Scheme	Marks
6. (a)	Critical activities B, F, J, K, N (not I); length 25 hours	B1; B1 (2)
(b)	$A = 5 - 0 - 3 = 2$ $E = 9 - 3 - 4 = 2$ $L = 22 - 11 - 4 = 7$ $C = 9 - 0 - 6 = 3$ $G = 9 - 4 - 3 = 2$ $M = 22 - 16 - 2 = 4$ $D = 11 - 3 - 3 = 5$ $H = 16 - 7 - 7 = 2$ $P = 25 - 18 - 3 = 4$ $I = 16 - 9 - 5 = 2$	M1 A1 ft A1 (3)
(c)		M1 A1 A1 ft A1 ft
(d)	 3 workers needed Precedences: <pre> graph TD A --> D A --> E B --> F B --> G C --> H E --> J F --> I F --> J G --> H G --> I G --> J D --> L D --> K J --> L J --> K I --> M I --> N K --> M K --> N H --> M L --> P </pre>	M1 A1 A1 (3) (12 marks)

ft = follow through mark

Question Number	Scheme	Marks
7. (a)		M1 A1 (2)
(b) (i)	$SF_1ABR = 6$	B1
(ii)	$SF_3CR = 8$	B1 (2)
(c)(i)		M1 A1
	e.g. $SF_1BR = 6$, $SF_2BR = 3$, $SF_2CR = 3$, $SF_3R = 4$	A1 A1
	Total flow = 30	A1 (5)
(ii)	Max flow – min cut theorem	M1
	Cut BR, F_2C, F_3C, F_3R	A1 (2)
		(11 marks)

Question Number	Scheme	Marks
8. (a)	$x + y \geq 380$ $y \geq 125$ $2x + 4y \leq 1200$	B1 B1 B1 (3)
(b)	$c = 3x + 2y$	B1 (1)
(c)	<p style="text-align: center;">Feasible region</p>	B1 B1 B1 B1 (4)
	Use of profit line or points testing	M1
	Minimum intersection of $x + y = 380$ and $2x + 4y = 1200$	
	$x = 160, y = 120, \text{ cost} = £920$	A1 A1 (3)
(d)	Maximum at intersection of $y = 125$ and $2x + 4y = 1200$	M1
	$x = 350, y = 125, \text{ cost} = £1300$	A1 A1 (3)
		(14 marks)