



Rewarding Learning

ADVANCED
General Certificate of Education
January 2011

Mathematics

Assessment Unit M2
assessing
Module M2: Mechanics 2

[AMM21]



MONDAY 31 JANUARY, AFTERNOON

TIME

1 hour 30 minutes.

INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number on the Answer Booklet provided.

Answer **all seven** questions.

Show clearly the full development of your answers.

Answers should be given to three significant figures unless otherwise stated.

You are permitted to use a graphic or a scientific calculator in this paper.

INFORMATION FOR CANDIDATES

The total mark for this paper is 75

Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.

Answers should include diagrams where appropriate and marks may be awarded for them.

Take $g = 9.8 \text{ m s}^{-2}$, unless specified otherwise.

A copy of the **Mathematical Formulae and Tables booklet** is provided.

Throughout the paper the logarithmic notation used is $\ln z$ where it is noted that $\ln z \equiv \log_e z$



Answer all seven questions.

Show clearly the full development of your answers.

Answers should be given to three significant figures unless otherwise stated.

- 1 At time $t = 0$ seconds a particle P is passing through a fixed point O with a velocity of $(8\mathbf{i} - 2\mathbf{j}) \text{ m s}^{-1}$
P has a **constant** acceleration of

$$(2\mathbf{i} - 4\mathbf{k}) \text{ m s}^{-2}$$

for $0 \leq t \leq 4$

- (i) Find the velocity of P when $t = 4$ [3]

When $t > 4$ seconds the acceleration of P is given by

$$(t\mathbf{i} + 8t^{-2}\mathbf{j} - 4\mathbf{k}) \text{ m s}^{-2}$$

- (ii) Find the velocity of P when $t = 8$ [6]

- 2 One end of a light inextensible string of length L metres is attached to a fixed point C. A small brass ball, B, of mass 1.5 kg is attached to the other end of the string. B moves in a horizontal circle with constant angular velocity 5 rad s^{-1} as shown in Fig. 1 below.

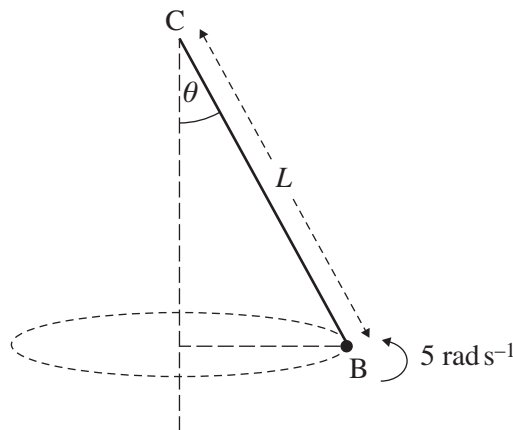


Fig. 1

The tension in the string is 20 N.
The string makes an angle θ with the downward vertical.

- (i) Find θ . [3]

- (ii) Find L . [6]

- 3 Fred, mass 80 kg, uses a smooth zip line to cross a river as shown in **Fig. 2** below. In doing so he drops through a vertical distance of h metres. He lands on the other side of the river with a speed of 16 m s^{-1}

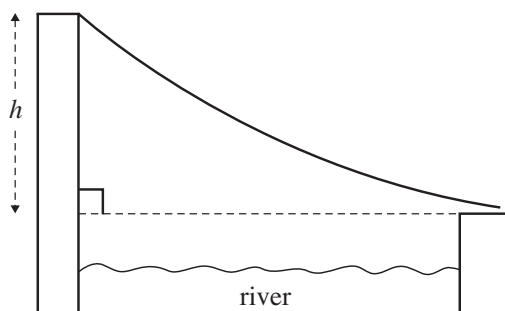


Fig. 2

- (i) Find Fred's kinetic energy on landing. [2]
- (ii) Hence find h . [6]
- (iii) State one modelling assumption you have made when answering this question. [1]

- 4 A lorry of mass 15 tonnes is travelling along a straight horizontal road. The lorry has a constant speed of 16 m s^{-1} and the driving force being developed by its engine is 15 625 N. There is a constant resistance to motion of R newtons. Model the lorry as a particle.

(i) Find R . [3]

The lorry now **ascends** a hill which is inclined at 3° to the horizontal as shown in **Fig. 3** below. The resistance to motion remains unchanged.

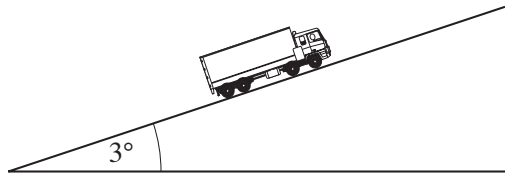


Fig. 3

(ii) Draw a diagram showing the external forces acting on the lorry. [2]

When the lorry is accelerating at 0.1 m s^{-2} it has speed 10 m s^{-1}

(iii) Find the power now being developed by the lorry's engine. [7]

- 5 A lobster pot, mass 20 kg, is placed on the surface of the sea. When the lobster pot has dropped x metres vertically through the water its speed is $v \text{ m s}^{-1}$. The lobster pot experiences an upward resistance of $2v^2$ newtons throughout its motion.

(i) Show that the equation of motion of the lobster pot may be described by the differential equation

$$v \frac{dv}{dx} = \frac{98 - v^2}{10} \quad [4]$$

When the lobster pot has dropped a distance S metres its speed is 6 m s^{-1}

(ii) Find S . [8]

6 [Take $g = 10 \text{ m s}^{-2}$ in this question]

A ball is kicked, with speed 15 m s^{-1} , from a point O on horizontal ground.

The angle of projection is θ , where $\sin \theta = 0.6$, above the horizontal.

A vertical wall is set at right angles to the plane of the trajectory of the ball and is 15 m from O as shown in **Fig. 4** below.

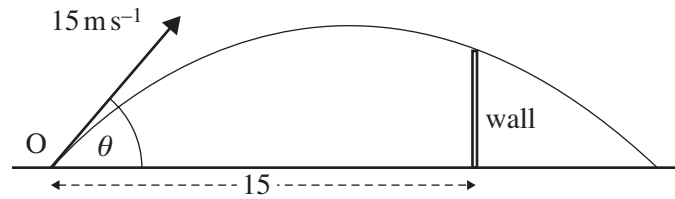


Fig. 4

The ball just clears the wall.

- (i) Find the time taken for the ball to reach the wall. [3]

- (ii) Find the height of the wall. [3]

- (iii) Find the speed of the ball as it clears the wall. [5]

7 [Take $g = 10 \text{ m s}^{-2}$ in this question]

A car, mass m kilograms, climbs a hill 500 m long.

The top of the hill is 25 m vertically above the horizontal level at the bottom of the hill as shown in Fig. 5 below.

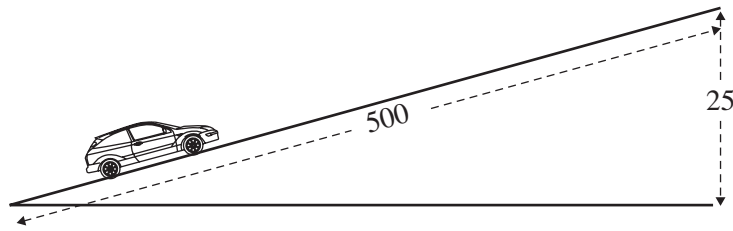


Fig. 5

The car's engine exerts a constant force of 8 kN.

The coefficient of friction between the car and the road surface is 0.2

Model the car as a particle.

(i) Draw a diagram showing all the external forces acting on the car.

[2]

At the bottom of the hill the car has a speed of 4 m s^{-1}

At the top of the hill the car has a speed of 6 m s^{-1}

(ii) Using the work-energy principle, find m .

[11]

THIS IS THE END OF THE QUESTION PAPER

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