General Certificate of Education June 2005 Advanced Subsidiary Examination

MATHEMATICS AND STATISTICS (SPECIFICATION B) Unit Pure 1

MBP1



Monday 23 May 2005 Morning Session

In addition to this paper you will require:

- an 8-page answer book;
- the AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed: 1 hour 15 minutes

Instructions

- Use blue or black ink or ball-point pen. Pencil should only be used for drawing.
- Write the information required on the front of your answer book. The *Examining Body* for this paper is AQA. The *Paper Reference* is MBP1.
- Answer all questions.
- All necessary working should be shown; otherwise marks for method may be lost.
- The **final** answer to questions requiring the use of tables or calculators should normally be given to three significant figures.

Information

- The maximum mark for this paper is 60.
- Mark allocations are shown in brackets.

Advice

• Unless stated otherwise, formulae may be quoted, without proof, from the booklet.

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Answer all questions.

- 1 The line AB has equation 3x + 4y = 2.
 - (a) Find the gradient of AB.

(2 marks)

- (b) The point C has coordinates (5, 3) and the point B is such that BC is perpendicular to AB.
 - (i) Find the gradient of BC.

(2 marks)

(ii) Show that the line BC has equation 4x - 3y = 11.

(2 marks)

(iii) Hence calculate the coordinates of B.

(3 marks)

2 (a) Express $(3+\sqrt{2})^2$ in the form $p+q\sqrt{2}$.

(2 marks)

- (b) Hence express $\frac{98}{(3+\sqrt{2})^2}$ in the form $m+n\sqrt{2}$, where m and n are integers.
- 3 An arithmetic series has *n*th term u_n , where $u_n = 3n + 5$.
 - (a) Find the values of u_1 and u_2 .

(2 marks)

(b) State the common difference of the arithmetic series.

(1 mark)

(3 marks)

- (c) Hence, or otherwise, find $\sum_{n=1}^{30} u_n$.
- 4 The quadratic equation $x^2 + 2kx + 2(k+4) = 0$ has distinct real roots.
 - (a) Show that $k^2 2k 8 > 0$.

(2 marks)

(b) Hence find the possible values of k.

(4 marks)

- 5 The function f has domain $-2 \le x \le 3$ and is defined by $f(x) = x^2 + 1$.
 - (a) (i) Find the values of f(-2) and f(3). (1 mark)
 - (ii) Sketch the graph of y = f(x), indicating clearly the value of the intercept on the y-axis. (3 marks)
 - (iii) Hence find the range of f. (3 marks)
 - (iv) State whether the inverse of f exists, giving a reason for your answer. (2 marks)
 - (b) The function g is defined for all values of x by $g(x) = (x 1)^4$.

Find gf(x), giving your answer in the simplest possible form. (2 marks)

6 (a) Prove the identity

$$\frac{3+\sin^2\theta}{2+\cos\theta} \equiv 2-\cos\theta \tag{2 marks}$$

(b) Use the identity from part (a) to show that the equation

$$\frac{3 + \sin^2 2x}{2 + \cos 2x} = \frac{5}{4}$$

can be written in the form $\cos 2x = \frac{3}{4}$. (1 mark)

(c) Solve the equation

$$\cos 2x = \frac{3}{4}$$

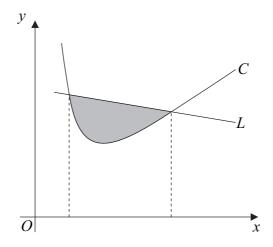
in the interval $0^{\circ} \le x \le 180^{\circ}$, giving your answers to the nearest 0.1° .

(No credit will be given for simply reading values from a graph.) (4 marks)

7 A curve C has equation $y = 2x + \frac{8}{x^2}$.

- (a) (i) Find $\frac{dy}{dx}$. (3 marks)
 - (ii) Hence show that the curve has a single stationary point and find its coordinates.

 (3 marks)
- (b) (i) Find $\int \left(2x + \frac{8}{x^2}\right) dx$. (3 marks)
 - (ii) Hence evaluate $\int_{1}^{4} \left(2x + \frac{8}{x^2}\right) dx$. (2 marks)
- (c) The curve C with equation $y = 2x + \frac{8}{x^2}$ is sketched below.



The line L with equation x + 2y = d intersects the curve C at the points (1, 10) and (4, p).

- (i) Find the values of the constants d and p. (2 marks)
- (ii) Find the area of the shaded region bounded by the curve C and the line L.

 (3 marks)

END OF QUESTIONS