



General Certificate of Education

Mathematics and Statistics 6320

Specification B

MBM4 Mechanics 4

Mark Scheme

2005 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Key to Mark Scheme

M	mark is for	method
m	mark is dependent on one or more M marks and is for	method
A	mark is dependent on M or m marks and is for	accuracy
B	mark is independent of M or m marks and is for	accuracy
E	mark is for	explanation
√ or ft or F		follow through from previous incorrect result
cao		correct answer only
cso		correct solution only
awfw		anything which falls within
awrt		anything which rounds to
acf		any correct form
ag		answer given
sc		special case
oe		or equivalent
sf		significant figure(s)
dp		decimal place(s)
A2,1		2 or 1 (or 0) accuracy marks
-x ee		deduct x marks for each error
pi		possibly implied
sca		substantially correct approach

Abbreviations used in Marking

MC – x	deducted x marks for mis-copy
MR – x	deducted x marks for mis-read
isw	ignored subsequent working
bod	given benefit of doubt
wr	work replaced by candidate
fb	formulae book

Application of Mark Scheme

No method shown:

Correct answer without working	mark as in scheme
Incorrect answer without working	zero marks unless specified otherwise

More than one method / choice of solution:

2 or more complete attempts, neither/none crossed out	mark both/all fully and award the mean mark rounded down
1 complete and 1 partial attempt, neither crossed out	award credit for the complete solution only

Crossed out work	do not mark unless it has not been replaced
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Alternative solution using a correct or partially correct method	award method and accuracy marks as appropriate
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Q	Solution	Marks	Total	Solution
1(a)	Initial $\rightarrow 3u \quad \leftarrow u$ $6m \quad 2m$ Final $\rightarrow V_1 \quad \rightarrow V_2$ C of momentum $6m.3u - 2m.u = 6m.V_1 + 2m.V_2$ $16u = 6V_1 + 2V_2$ Restitution $\frac{1}{4}(3u + u) = V_2 - V_1$ $u = V_2 - V_1$ $14u = 8V_1$ $V_1 = \frac{7}{4}u$	M1 A1 M1A1 M1 A1	6	
(b)	$V_2 = u + \frac{7}{4}u$ $= \frac{11}{4}u$	M1 A1	2	
Total			8	
2	Resolve along AB $R \cos 30 = Q \cos 45$ Resolve perpendicular to AB $R \sin 30 + Q \sin 45 = P$ $\frac{R}{2} + \frac{Q}{\sqrt{2}} = 4\sqrt{2}$ $\frac{R\sqrt{3}}{2} = \frac{Q}{\sqrt{2}}$ $\therefore \frac{R}{2} + \frac{R\sqrt{3}}{2} = 4\sqrt{2}$ $R(1 + \sqrt{3}) = 8\sqrt{2}$ $R = \frac{8\sqrt{2}}{1 + \sqrt{3}} = \frac{8\sqrt{2}(\sqrt{3} - 1)}{2}$ $R = 4(\sqrt{6} - \sqrt{2})$ $Q = \frac{\sqrt{3}}{\sqrt{2}} [4(\sqrt{6} - \sqrt{2})]$ $= 4(3 - \sqrt{3})$	M1A1 M1A1 M1 A1 A1	7	If just substitute given R into one of resolve eq ⁿ s, M1 A1 only.
Total			7	

MBM4 (cont)

Q	Solution	Marks	Total	Comments
3(a)	$\mathbf{r}_{C \text{ rel } H} = \mathbf{r}_C - \mathbf{r}_H$ $= \begin{pmatrix} -30 \\ -23 \\ -0.3 \end{pmatrix}$	B1	1	
(b)(i)	$\mathbf{v}_{C \text{ rel } H} = \mathbf{v}_C - \mathbf{v}_H$ $= \begin{pmatrix} 4 \\ -58 \\ 0 \end{pmatrix} - \begin{pmatrix} -29 \\ -90 \\ -0.1 \end{pmatrix} = \begin{pmatrix} 33 \\ 32 \\ 0.1 \end{pmatrix}$	M1 A1	2	
(ii)	<p>At time t, $\mathbf{r}_{C \text{ rel } H} = \begin{pmatrix} -30 \\ -23 \\ -0.3 \end{pmatrix} + t \begin{pmatrix} 33 \\ 32 \\ 0.1 \end{pmatrix}$</p> $= \begin{pmatrix} -30 + 33t \\ -23 + 32t \\ -0.3 + 0.1t \end{pmatrix}$ <p>\therefore Distance apart</p> $= \sqrt{\{(-30+33t)^2 + (-23 + 32t)^2 + (-0.3+0.1t)^2\}}$	M1 A1	4	
(iii)	$S^2 = (-30+33t)^2 + (-23 + 32t)^2 + (-0.3+0.1t)^2$ $\frac{dS^2}{dt} = 66(-30+33t) + 64(-23 + 32t) + 0.2(-0.3+0.1t)$ $= 0 \text{ when } 3452.06 = 4226.02 t$ $t = 0.8168..$ <p>Time is 12. 49</p>	M1 A1 M1 A1 A1	5	
(iv)	<p>At 1pm, $S = \sqrt{3^2 + 9^2 + 0.2^2}$</p> $= \sqrt{90.04}$ $= 9.4889..$ <p>Which is less than 10 miles</p>	M1 A1	2	
Total			14	

MBM4 (cont)

Q	Solution	Marks	Total	Comments
4(a)	Moments about B for whole system $20l = P \cdot l \cos 80$ $P = 115 \text{ N}$	M1 A1 A1	3	
(b)	Resolve vertically for the whole system $T = 135 \text{ N}$ Resolve vertically at B $T = T_2 \sin 80$ $T_2 = 137 \text{ N}$	M1A1 M1 A1	4	
(c)	Resolve horizontally at B $T_1 = T_2 \cos 80$ $T_1 = 23.8 \text{ N}$	M1 A1	2	
Total			9	
5(a)(i)	Velocities parallel to the wall $2u \cos \theta = 3u \cos 60$ $\cos \theta = \frac{3}{4}$	M1 A1 A1	3	
(ii)	Restitution : $3u \sin 60 \cdot e = 2u \sin \theta$ $e = \frac{2 \sin \theta}{3 \sin 60}$ $= 0.509$	M1A1 A1	3	
(iii)	Angle is $60 + 41.4$ $= 101.4$	M1 A1	2	
(b)	Impulse = change of momentum which is perpendicular to the wall $= m \cdot 3u \sin 60 + m \cdot 2u \sin \theta$ $= 3.92mu$	M1 M1 A1	3	Needs + for second M1
Total			11	

MBM4 (cont)

Q	Solution	Marks	Total	Comments
6(a)	<p>If \bar{x} is the distance of the centre of mass from the base</p> <p>Moments about plane of the base</p> $\pi r^2 \cdot 2r \cdot \rho + \frac{1}{3} \pi r^2 H (2r + \frac{H}{4}) \cdot 3\rho$ $= (\pi r^2 \cdot 2r\rho + \frac{1}{3} \pi r^2 H \cdot 3\rho) \bar{x}$ $2r^2 + 2Hr + \frac{H^2}{4} = (2r + H) \bar{x}$ $\bar{x} = \frac{8r^2 + 8Hr + H^2}{4(2r + H)}$	<p>M1</p> <p>M1A1</p> <p>A1</p> <p>m1</p> <p>A1</p>	6	Dep both M1
6(b)	<p>If on the point of toppling</p> $\tan \theta = \frac{1}{5} = \frac{r}{x}$ $\therefore 5r = \frac{8r^2 + 8Hr + H^2}{4(2r + H)}$ $40r^2 + 20rH = 8r^2 + 8rH + H^2$ $32r^2 + 12rH - H^2 = 0$ $H^2 - 12rH - 32r^2 = 0$ $H = \frac{12 \pm \sqrt{144 + 128}}{2} r$ $= (6 \pm 2\sqrt{17}) r$ $= (6 + 2\sqrt{17}) r$	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p>	5	for $\frac{r}{5}$ or $5r =$ result in (a)
	Total		11	
	TOTAL		60	