

GCE 2004
June Series



Mark Scheme

Mathematics and Statistics B *MBS2*

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available from:

Publications Department, Aldon House, 39, Heald Grove, Rusholme, Manchester, M14 4NA
Tel: 0161 953 1170

or

download from the AQA website: www.aqa.org.uk

Copyright © 2004 AQA and its licensors

COPYRIGHT

AQA retains the copyright on all its publications. However, registered centres for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to centres to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Set and published by the Assessment and Qualifications Alliance.

The Assessment and Qualifications Alliance (AQA) is a company limited by guarantee registered in England and Wales 3644723 and a registered charity number 1073334. Registered address AQA, Devas Street, Manchester. M15 6EX.

Dr Michael Cresswell Director General

Key to Mark Scheme

M	mark is for	method
m	mark is dependent on one or more M marks and is for	method
A	mark is dependent on M or m marks and is for	accuracy
B	mark is independent of M or m marks and is for	accuracy
E	mark is for	explanation
✓ or ft or F		follow through from previous incorrect result
cao		correct answer only
cso		correct solution only
awfw		anything which falls within
awrt		anything which rounds to
acf		any correct form
ag		answer given
sc		special case
oe		or equivalent
sf		significant figure(s)
dp		decimal place(s)
A2,1		2 or 1 (or 0) accuracy marks
-x ee		deduct x marks for each error
pi		possibly implied
sca		substantially correct approach

Abbreviations used in Marking

MC – x	deducted x marks for mis-copy
MR – x	deducted x marks for mis-read
isw	ignored subsequent working
bod	given benefit of doubt
wr	work replaced by candidate
fb	formulae book

Application of Mark Scheme

No method shown:

Correct answer without working	mark as in scheme
Incorrect answer without working	zero marks unless specified otherwise

More than one method / choice of solution:

2 or more complete attempts, neither/none crossed out	mark both/all fully and award the mean mark rounded down
1 complete and 1 partial attempt, neither crossed out	award credit for the complete solution only

Crossed out work	do not mark unless it has not been replaced
------------------	--

Alternative solution using a correct or partially correct method	award method and accuracy marks as appropriate
---	---

Mathematics and Statistics B Statistics 2 MBS2 June 2004

Question Number and Part	Solution	Marks	Total marks	Comments
1(a)	$p = \frac{18}{200} = 0.09$ $0.09 \pm 1.6449 \sqrt{\frac{0.09 \times 0.91}{200}}$ 0.09 ± 0.0333 (0.0567, 0.1233) (0.0567, 0.123)	B1 B1 M1 M1 m1 A1	6	1.6449 (or 1.64, 1.645,....) attempted use of Normal $\sqrt{\frac{0.09 \times 0.91}{200}}$ allow wrong z 0.056 to 0.057 0.123 to 0.124
(b)	CI suggests between 5.67% and 12.3% are faulty. This is greater than 5%. Supplier can return batch.	B1✓ B1	2	
	Total		8	
2(a)	$\frac{24}{8} = 3$ Select a number randomly between 1-3 Select every third name CFILORUX (or DGJMPSVY EHKNQTWZ)	B1 B1 B1 M1 A1	5	Randomly select starting point periodcially select name every third CODPEQFR (or GSHTIUJV KWLXMYNZ)
(b)	Equally likely – each athlete has probability $\frac{1}{3}$	B1 B1	2	
(c)	Not random sample – CD (or equivalent) cannot occur in sample.	B1 B1	2	
	Total		9	

MBS2 (cont)

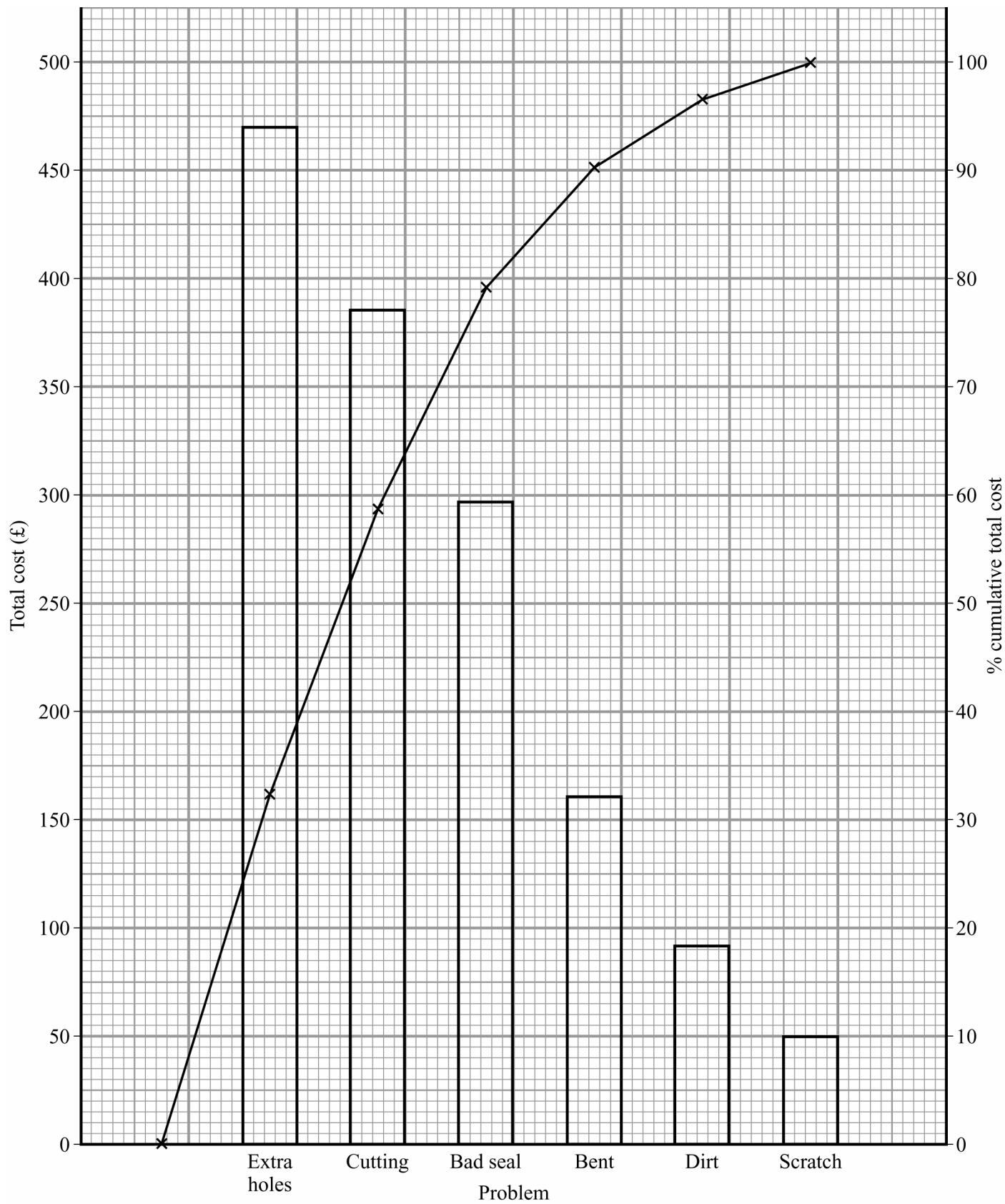
Question Number and Part	Solution	Marks	Total marks	Comments
3(a)	$p = \frac{421+498+366+313}{4} = 399.5$	B1 B1	2	numerator denominator
(b)(i)	$y = -5.747x + 399.892$ $y = -5.75x + 400$	B2 B2	4	m and c correct to 3s.f. sc M1 A1, M1 A1 if eqns used ($y = -7.74x + 427$ B0)
(ii)	When $x = 11.5$ m.a. = 333.8	B1 M1 A1	3	$x = 11.5$
(c)(i)	Line (0, 400) (10, 342.5)	M1 A1	2	
(ii)	$421 - 404 = 17$ $378 - 380 = -2$ $384 - 356 = 28$ $\frac{43}{3} = 14.3$	M1 A1	3	Seasonal effects Average seasonal 13 to 16
(iii)	$333.8 + 14.3 = 348.1$ £348,000	M1 A1	2	b(ii) or graph + c(ii) 343 to 353 (000)
	Total		16	

MBS2(cont)

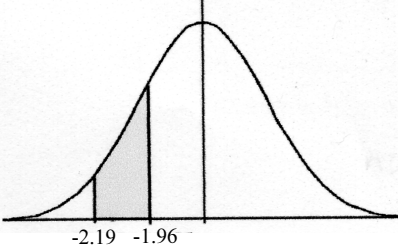
Question Number and Part	Solution	Marks	Total marks	Comments																												
4(a)	Dirt, Cutting and Bad seal	B2,1	2	B1 any two B2 all three correct B1 four answers																												
(b)(i)	<table border="1"> <thead> <tr> <th>Problem</th> <th>Total cost</th> </tr> </thead> <tbody> <tr> <td>Bad seal</td> <td>297</td> </tr> <tr> <td>Bent</td> <td>161</td> </tr> <tr> <td>Cutting</td> <td>385</td> </tr> <tr> <td>Dirt</td> <td>92</td> </tr> <tr> <td>Extra holes</td> <td>470</td> </tr> <tr> <td>Scratch</td> <td>50</td> </tr> </tbody> </table>	Problem	Total cost	Bad seal	297	Bent	161	Cutting	385	Dirt	92	Extra holes	470	Scratch	50	M1 A1	2															
Problem	Total cost																															
Bad seal	297																															
Bent	161																															
Cutting	385																															
Dirt	92																															
Extra holes	470																															
Scratch	50																															
(ii)	<table border="1"> <thead> <tr> <th>Problem</th> <th>Total cost</th> <th>Cum.total cost</th> <th>% cum. Total cost</th> </tr> </thead> <tbody> <tr> <td>Ex.holes</td> <td>470</td> <td>470</td> <td>32.3</td> </tr> <tr> <td>Cutting</td> <td>385</td> <td>855</td> <td>58.8</td> </tr> <tr> <td>Bad seal</td> <td>297</td> <td>1152</td> <td>79.2</td> </tr> <tr> <td>Bent</td> <td>161</td> <td>1313</td> <td>90.2</td> </tr> <tr> <td>Dirt</td> <td>92</td> <td>1405</td> <td>96.6</td> </tr> <tr> <td>Scratch</td> <td>50</td> <td>1455</td> <td>100.0</td> </tr> </tbody> </table>	Problem	Total cost	Cum.total cost	% cum. Total cost	Ex.holes	470	470	32.3	Cutting	385	855	58.8	Bad seal	297	1152	79.2	Bent	161	1313	90.2	Dirt	92	1405	96.6	Scratch	50	1455	100.0	M1 M1 M1 A1	4	Ranking Cum. total cost % cum. total cost
Problem	Total cost	Cum.total cost	% cum. Total cost																													
Ex.holes	470	470	32.3																													
Cutting	385	855	58.8																													
Bad seal	297	1152	79.2																													
Bent	161	1313	90.2																													
Dirt	92	1405	96.6																													
Scratch	50	1455	100.0																													
(iii)	(see diagram on next page) Bar chart % cumulative total costs polygon	M1 A1 M1 A1	4																													
(iv)	Extra holes, cutting, bad seal	B1 B1	2	Any two All three																												
(c)	Cutting	B1	1																													
	Total		15																													

MBS2 (cont)

Diagram for Question 4



MBS2 (cont)

Question Number and Part	Solution	Marks	Total marks	Comments
5(a)	$n = 300$ $p = 0.006$ $np = 1.8$ Use Poisson $P(X \leq 6) = 0.9974$ $P(X \leq 2) = 0.7306$ $P(3 \leq X \leq 6) = 0.2668$ ≈ 0.267 (3 sig. fig.)	B1 M1 M1 M1 A1	5	0.266 to 0.267
(b)	$n = 90$ $p = 0.3$ $np = 27$ $npq = 18.9$ use Normal $\frac{17.5 - 27}{\sqrt{18.9}} = \frac{-9.5}{\sqrt{18.9}} = -2.185$ ≈ -2.19 $\frac{18.5 - 27}{\sqrt{18.9}} = -1.955$ ≈ -1.96  $\frac{0.98574}{-0.97500}$ $\frac{0.01074}{}$ $P(X = 18) = 0.0107$	B1 B1 M1 M1 A1 m1 A1	7	Method z Continuity correction Both correct -2.18 to -2.19 -1.95 to -1.96 Must have 27, $\sqrt{18.9}$ 0.0103 to 0.011
	Total		12	
	TOTAL		60	