

GCE 2004
June Series



Mark Scheme

Mathematics and Statistics B *MBM2*

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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Dr Michael Cresswell Director General

Key to Mark Scheme

M	mark is for	method
m	mark is dependent on one or more M marks and is for	method
A	mark is dependent on M or m marks and is for	accuracy
B	mark is independent of M or m marks and is for	accuracy
E	mark is for	explanation
✓ or ft or F		follow through from previous incorrect result
cao		correct answer only
cso		correct solution only
awfw		anything which falls within
awrt		anything which rounds to
acf		any correct form
ag		answer given
sc		special case
oe		or equivalent
sf		significant figure(s)
dp		decimal place(s)
A2,1		2 or 1 (or 0) accuracy marks
-x ee		deduct x marks for each error
pi		possibly implied
sca		substantially correct approach

Abbreviations used in Marking

MC – x	deducted x marks for mis-copy
MR – x	deducted x marks for mis-read
isw	ignored subsequent working
bod	given benefit of doubt
wr	work replaced by candidate
fb	formulae book

Application of Mark Scheme

No method shown:

Correct answer without working**mark as in scheme****Incorrect answer without working****zero marks unless specified otherwise**

More than one method / choice of solution:

2 or more complete attempts, neither/none crossed out**mark both/all fully and award the mean mark rounded down****1 complete and 1 partial attempt, neither crossed out****award credit for the complete solution only**

Crossed out work

do not mark unless it has not been replacedAlternative solution **using a correct or partially correct method****award method and accuracy marks as appropriate**

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Question Number and Part	Solution	Marks	Total	Comments
1 (a)(i)	$0 = 8 - 4h$ $h = 2$	B1	1	Correct value of h
(ii)	$a = 8 - 2t$	B1	1	Correct expression
(b)	$v = \int 8 - 2t dt$ $= 8t - t^2 + c$ $2 = 32 - 16 + c$ $c = -14$ $v = 8t - t^2 - 14$	M1 A1 m1 A1	4	Integrating acceleration Correct velocity with or without c Finding c Correct final expression
Total			6	
2 (a)	$\mathbf{v} = 4 \cos t \mathbf{i} - 4 \sin t \mathbf{j} + 6 \mathbf{k}$	M1 A1	2	Differentiating position vector Correct velocity vector
(b)	$\mathbf{a} = -4 \sin t \mathbf{i} - 4 \cos t \mathbf{j}$	M1 A1	2	Differentiating the velocity vector Correct acceleration
(c)	$a = \sqrt{16 \sin^2 t + 16 \cos^2 t}$ $= \sqrt{16(\sin^2 t + \cos^2 t)}$ $= \sqrt{16}$ $= 4$	M1 A1 A1	3	Finding magnitude Correct expression for magnitude ag Using trig identity to get the printed answer with correct working including the k component
(d)	$v = \sqrt{16 \sin^2 t + 16 \cos^2 t + 36}$ $= \sqrt{52}$ $= 7.21$ Or $v^2 = 52$	M1 A1 A1	3	Finding magnitude Correct expression for magnitude $\sqrt{52}$ or equivalent
Total			10	
3 (a) (i)	$\text{KE} = 2 \times 9.8 \times 4 = 78.4 \text{ J}$	M1 A1	2	Use of $\text{KE} = \text{change in PE}$ with $h = 4$ Correct energy
(ii)	$78.4 = \frac{1}{2} \times 2 \times v^2$ $v = \sqrt{78.4} = 8.85 \text{ ms}^{-1}$	M1 A1 A1	3	Use of kinetic energy or constant acceleration formula to form an equation in v based on a fall of 4 metres Correct equation Correct v
(b) (i)	$78.4 + 19.6x = \frac{80}{2 \times 4} x^2$ $0 = 10x^2 - 19.6x - 78.4$	M1 A1 M1 A1	4	Calculation of EPE shown Correct EPE Three term energy equation ag Correct equation from correct working
(ii)	$x = \frac{19.6 \pm \sqrt{19.6^2 - 4 \times 10 \times (-78.4)}}{2 \times 10}$ $= 3.95 \text{ or } -1.99$ Max L = 7.95 m	M1 A1 A1✓	3	Solving the quadratic equation Correct solutions ft Adding 4 to their x
(c)	No air resistance	B1	1	Appropriate assumption
Total			13	

MBM2 (cont)

Question Number and Part	Solution	Marks	Total	Comments
4 (a)	$F = 420 + 1200 \times 9.8 \sin 6^\circ = 1649$	M1		Finding force as the resultant of two forces
	$P = (420 + 1200 \times 9.8 \sin 6^\circ) \times 20$ $= 33000 \text{ W (to 3sf)}$	A1 m1	4	Correct force Use of $P = Fv$ Correct answer from correct expression
(b)	$420 = 20k$ $k = 21$	M1 A1	2	Equation for k involving 420 Correct value of k
(c)	$F = 21v$ $32985 = 21v^2$	M1 M1		Expression for F in terms of v Use of $P = Fv$ to form an equation with v^2
	$v = \sqrt{\frac{32985}{21}} = 39.6 \text{ ms}^{-1}$	A1✓ A1✓	4	ft Correct equation ft Correct v
Total			10	
5 (a)	$R \cos \theta = 1000g$ $R = \frac{9800}{\cos \theta}$	M1 A1	2	Resolving vertically to form a two term equation ag Correct equation from correct working
(b)	$R \sin \theta = m \times \frac{10^2}{40}$ $g \tan \theta = 2.5$ $\tan \theta = \frac{2.5}{9.8} = 0.2551$ $\theta = 14.3^\circ$	M1 A1 M1 A1		Resolving horizontally to get a two term equation Correct equation Substituting for R Correct equation
(c)	$F \cos 3^\circ + R \sin 3^\circ = 1000 \times \frac{10^2}{40}$ $R \cos 3^\circ - F \sin 3^\circ = 9800$ $F(\cos^2 3^\circ + \sin^2 3^\circ)$ $= 2500 \cos 3^\circ - 9800 \sin 3^\circ$ $F = \frac{2500 \cos 3^\circ - 9800 \sin 3^\circ}{1}$ $= 1980 \text{ N (to 3 sf)}$	A1 M1 A1 M1 A1	5	Correct angle Resolve horizontally with three terms Correct equation Resolve vertically with three terms Correct equation
	Or $1000 \times \frac{10^2}{40} \cos 3^\circ = F + 1000g \sin 3^\circ$ $F = 2497 - 513 = 1980$	m1 A1 (M1A1) (M1A1) (m1A1)	6	Solve for F Correct F for RHS for LHS finding F
Total			13	

MBM2 (cont)

Question Number and Part	Solution	Marks	Total	Comments
6	$\bar{x} = \frac{\int_0^5 \sqrt{1 + \left(\frac{1}{5}\right)^2} x^2 dx}{\int_0^5 \sqrt{1 + \left(\frac{1}{5}\right)^2} x dx} = \frac{\int_0^5 x^2 dx}{\int_0^5 x dx}$ $= \frac{\left[\frac{x^3}{3}\right]_0^5}{\left[\frac{x^2}{2}\right]_0^5} = \frac{\frac{125}{3}}{\frac{25}{2}} = \frac{10}{3}$	M1 M1 A1 m1 A1	5	x^2 in numerator x in denominator valid expression Evaluation of integrals ag Correct answer from correct working
	Total		5	
7(a)	$a = 0.05$ $6^2 = \omega^2 (0.05^2 - 0.04^2)$ $\omega = \sqrt{\frac{0.36}{0.0009}} = 20$ $T = \frac{2\pi}{20} = \frac{\pi}{10}$	B1 M1 A1 m1 A1 A1	6	Amplitude = 0.05 Use of SHM equation with $x = 0.04$ Correct equation Solving for ω Correct ω ag Correct period from correct working
(b)	$v = 0.05 \times 20 = 1 \text{ ms}^{-1}$	M1 A1	2	Using $v = a\omega$ Correct v
(c)	$a_{\max} = 0.05 \times 20^2 = 20 \text{ ms}^{-2}$	M1 A1	2	Use of $a_{\max} = a\omega^2$ Correct acceleration Allow ± 20
	Total		10	

MBM2 (cont)

Question Number and Part	Solution	Marks	Total	Comments
8 (a)	$mv \frac{dv}{dx} = -mg - mkv$ $\frac{v}{g + kv} \frac{dv}{dx} = -1$ $\int \frac{v}{g + kv} dv = \int -1 dx$ $\int \frac{v}{g + kv} dv = -x + c$	M1 A1 m1 A1	4	Using Newton's second law to form a differential equation with $v \frac{dv}{dx}$ Correct differential equation Separation of variables ag Correct answer from correct working
(b)	$\int \frac{1}{k} - \frac{g}{k(g + kv)} dv = -x + c$ $\frac{v}{k} - \frac{g}{k^2} \ln g + kv = -x + c$ $x = 0, v = 20 \Rightarrow c = \frac{20}{k} - \frac{g}{k^2} \ln(g + 20k)$ $x = \frac{20 - v}{k} + \frac{g}{k^2} \ln\left(\frac{g + kv}{g + 20k}\right)$	M1 M1 A1 A1 m1 A1 A1	7	Substituting given identity Integration to get v and \ln terms \ln term correct v term correct Finding c Correct c ag Correct final answer from correct working
(c)	$v = 0$ $x = \frac{20 - 0}{k} + \frac{g}{k^2} \ln\left(\frac{g + k \times 0}{g + 20k}\right)$ $x = \frac{20}{k} + \frac{g}{k^2} \ln\left(\frac{g}{g + 20k}\right)$	M1 A1	2	Substituting $v = 0$ Correct height
	Total		13	
	TOTAL		80	